

IDENTIFICATION OF URBAN
WATERSHED UNITS USING REMOTE
MULTISPECTRAL SENSING

by

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June 1971

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Completion Report
OWRR Project No. A-012-COLO

by

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submitted to

Office of Water Resources Research
U. S. Department of Interior
Washington, D. C. 20240

January 31, 1972

The work upon which this report is based was supported by a grant of \$12,000 provided by the United States Department of Interior, Office of Water Resources Research, as authorized by the Water Resources Research Act of 1964, and pursuant to Grant Agreement No. 14-30-0001-3006.

Colorado Water Resources Research Institute
Colorado State University
Fort Collins, Colorado

Norman A. Evans, Director

It is agayns the process of nature. CHAUCER



FRONTPiece - EKTACHROME INFRARED AIRPHOTO OF THE RAPIDLY URBANIZING AREA SURROUNDING THE NORTHGLENNS SHOPPING CENTER. Flown by Colorado State University on 28 April 1971. Scale approximately 1/20,000. The asphalted shopping center is the dark area in the center right. Green, healthy lawns are red. A trailer park shows as white in the lower left corner. The photo was taken in the spring and some agricultural fields are the reds and pinks of early crops, while others are the blues and greens of fallow or just-plowed fields.

ACKNOWLEDGEMENTS

The work upon which this report is based was supported by a grant of \$12,000 provided by the United States Department of Interior, Office of Water Resources Research, as authorized by the Water Resources Research Act of 1964, and pursuant to Grant Agreement No. 14-31-0001-3006.

Appreciation is extended to the Water Resources Division of the United States Geological Survey and to G. Louis Ducret for cooperation with respect to their Denver urban watershed modeling study which provided the watershed framework of this study.

Appreciation is also extended to the National Science Foundation, International Biological Program, Grassland Biome, Colorado State University, Fort Collins, Colorado, for the use of the field spectrometer system.

Special personal appreciation is extended to Dr. James Smith for his assistance with the optimization logic, Mr. Robert Pearson for his help with the field spectrometer measurements, and Mrs. Carol Hunsicker for report typing. All of these collaborators are with the Department of Watershed Sciences, Colorado State University, Fort Collins, Colorado.

ABSTRACT

The rapid pace of development in the urban fringe has significant hydrologic effects. Changes due to urban development of natural watersheds are shown by an areal analysis of thirteen small watersheds from 40 to 600 acres located in the Denver suburbs. Airphotos for each of the watersheds were obtained at 5 to 10 year intervals for as far back as 1935. The surface composition of each watershed was determined from the airphotos, in terms of common urban surface materials such as rooftops, asphalt, and lawns. Examination of the results shows the developmental trends in changes in the impervious cover of each watershed and the effects on this imperviousness of different seasonal characteristics.

New urban hydrology analysis methods are necessary to keep pace with such rapid changes in surface cover. Recent progress in urban watershed modeling is a partial answer but further progress in relating changing surface cover to urban hydrology requires refined and timely measurements of the surface cover. This study illustrates the use of remote multispectral imagery to provide the more detailed analysis of surface characteristics which can, in turn, be related to hydrologic effects and input into watershed models.

A method is proposed for determining the optimum wavelength bands to be used for differentiating ten types of urban surface materials via automatic image processing based on measured spectral curves of the materials. The results can be used in the design or use of instruments to map urbanizing areas. Suggestions for further research are given, including the collection of multispectral imagery over the thirteen watersheds included in the study, and comparison of the automatic image processing results with areal analysis or "ground truth" obtained from low altitude color and color IR photography.

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INTRODUCTION

The rapid development of rural terrain into urban areas has created special problems which challenge city officials and hydrologists concerned with managing urban water resources. Hydrologic changes in rapidly urbanized watersheds are a complex phenomena and have been studied by increasingly complex mathematical methods to determine the effects of urban development on runoff. At present many computerized water yield simulation models have been and are being developed which predict the character of runoff from a given rainfall as a function of surface material, surface topography, antecedent moisture conditions, and overall area of the watershed, among others. A significant and somewhat difficult and time consuming parameter to measure is the type and distribution of the surface materials in these rapidly changing watersheds. In-the-field mapping of surface material is a time consuming process, and has largely been replaced by the interpretation of aerial photographs. However, it is now becoming possible to use automated techniques, both for the interpretation of aerial photographs and for interpretation of imagery from non-photographic remote sensing devices.

A technique for using computer-interpreted remotely sensed imagery has been proposed as an input into computerized watershed models. The purpose of this study is to document the need for frequent analysis of urbanizing watersheds, and to illustrate how the computer mapped surface materials can be interfaced for input into urban hydrological models.

THE URBANIZING WATERSHED

Alteration of natural watersheds by the process of urbanization causes significant hydrologic changes. Flooding and excessive erosion can result since peak discharge occurs sooner and is of greater volume, due to the extensive areas of impervious cover so characteristic of urban areas.

Urbanization of natural watersheds also effects significant changes in water quality. Erosion of large amounts of soil exposed by construction activities causes deleterious removal of topsoil and results in excessively turbid runoff. Once the watershed is fully developed, problems can still exist with residential, commercial and industrial wastes polluting surface runoff, such as pesticides, herbicides, and effluent chemicals discarded from commercial and industrial firms.

Lull and Sopper (1969) studied several small forested watersheds in south-eastern Pennsylvania and found that urbanization caused a reduction in evapo-transpiration in addition to increasing runoff and peak flows. During a period of 25 years as these watersheds were urbanized, annual ratios of stormflow to precipitation appeared to be the most sensitive indicator of urbanization.

The stormflow resulting from a given amount of precipitation depends on a large number of variables in the watershed such as area, character of surface materials, antecedent moisture, topography, etc. In past years the problem of predicting runoff from rainfall and these watershed characteristics was too complicated to treat rigorously, but with today's computerized techniques, it has become possible to simulate hydrologic processes mathematically.

URBAN WATERSHED MODELING

Both analog and digital models have been designed to predict runoff as a function of rainfall and the many hydrologic processes within an urbanized watershed. Narayana, et.al. (1970) have developed an analog model which analyzes a given watershed in terms of its subareas. The watershed is divided into a manageable number of subzones and the hydrologic parameters determined for each subzone. Losses from precipitation on the watershed due to interception, infiltration, and depression storage are chronologically deducted for each subzone and the remaining runoff is routed through surface subzones and channel storages. Outflow hydrographs are then routed through succeeding downstream subzones to the gaging point on the watershed. Such a model makes it possible to simulate runoff for subzones within the urban watershed, to account for spacial variation of storm and watershed characteristics, and to predict outflow hydrographs from subzones within the watershed for improved storm sewer design.

A study using a digital computer to estimate effects of urban development on flood peaks (James, 1965) used the Stanford Watershed Model (Crawford and Linsley, 1962), which uses mathematical algorithms to simulate the runoff cycle. The equations account for all moisture entering, stored within, and leaving the watershed via the various hydrologic processes. Runoff is routed from the point it enters tributary channels to the location downstream where a simulated hydrograph is desired. Input to the Stanford Watershed Model consists of hourly precipitation, average daily evaporation by ten-day periods, a translation histogram for channel routing, an array describing the interflow characteristics of the basin, an array describing infiltration characteristics, 28 constants describing physical characteristics of the watershed, and four constants describing initial moisture conditions. Values of the arrays and constants are determined by a

trial and error process which matches a synthesized hydrograph to an actual recorded hydrograph. The computer output provides a continuous synthetic hydrograph for the entire period of analysis, from which interpretations can be made for flood control measures.

Gonzalez and Ducret (1971) are currently using a variant of the Stanford Watershed Model as an aid in defining the magnitude and frequency of floods in small urbanized watersheds in the Denver, Colorado metropolitan area. A total of 30 small watersheds in the Denver and Boulder area are being measured by dual digital stage rainfall gauges with a five-minute recording interval. Short-term rainfall runoff data is collected from each of these watersheds and is used to calibrate the coefficients in the watershed model which represent the physical watershed characteristics. Once a model is calibrated for each of the watersheds, long-term U. S. Weather Bureau rainfall records are input to obtain long-term synthetic hydrographs for each of the watersheds. Flood frequency is then determined from the long-term synthetic hydrographs, and by statistical methods the flood frequency and magnitude are defined over the entire Denver metropolitan area.

Computer simulation of hydrologic processes is continually becoming more sophisticated and increasing numbers of watershed models are appearing in the literature, both for urban and natural watersheds alike. The reader is referred to the two sections in the bibliography (Appendix A) dealing with watershed modeling for further references.

REMOTE SENSING RELATED TO URBAN STUDIES

The value and potential of using remote sensing methods in studying the urban environment is rapidly being realized. A study is currently under way in the Geologic Applications Division of the United States Geological Survey to test the feasibility of monitoring urban dynamics from earth orbiting satellites (Gerlach, 1971). Twenty-six cities are being photographed from altitudes in excess of 50,000 feet in color, color infrared, multiband, and black and white. The goals of the project are to develop techniques for detecting and identifying urban change and evaluating its significance from ERTS-A (Earth Resources Technology Satellite) imagery.

A method for interpreting housing quality data from multiband aerial photographs has been developed (Wellar, 1970) based on the unique characteristics of low quality housing, namely the presence of litter, garbage, junked

cars, rubbish piles, the lack of landscaping in yards, presence of weeds in vacant lots, and the degree of crowding of houses on lots. Analysis of high resolution imagery for estimating urban residential housing quality (Marble, 1969), although not a replacement for ground surveys, was found to permit ground surveys to function more efficiently, and at lower cost.

High resolution remote sensor imagery can be used in a similar fashion for detecting surface characteristics of urban watersheds, which is a significant input into any watershed model. Colwell (1970) investigated the potential of using 18 channels of multispectral scanner imagery and its computer reduction to delineate different types of urban materials, namely bare soil, several vegetation types, concrete, asphalt, gravel, and a variety of roofing materials. This multispectral imagery obtained in the visible, photographic infrared and thermal infrared regions of the electromagnetic spectrum was originally recorded on analog tape and subsequently analyzed with an analog computer system using a spectrum matching technique.

A simple explanation of spectrum matching will assist the reader in understanding the results which follow. The computer is given a representative sample of known image points (data points) from the multispectral imagery tape for the surface material to be identified. It calculates and stores average spectral curves for these several hundred identified image points. This is the process of selecting and computing a training set. The computer then examines all the millions of unknown image points on the data tape attempting to match each unknown point's spectral curve with the stored, known training set's curve for the particular material. If a reasonable match is found, the unknown image point is identified as the material sought and a black and white film is exposed with a dot of light at that geographic position. If a match is not found, the film is not exposed. The resulting black and white, i.e., no gray, decision image (recognition map) is exposed in those portions representing the location of the surface material sought while the unexposed areas represent all other materials. This process can be repeated to obtain recognition maps of each material of interest. In practice, a more complex image processing approach is used. It checks the unknown image point simultaneously against all surface materials previously defined by training sets and identifies the point as 'most probably' being one of these materials or sufficiently different in spectra to be none of them. A black and white recognition map for each material is still output as noted above. Each of these transparencies can be reproduced in a different color and superimposed to produce a composite color-coded identification map of all the materials

in the urban scene.

A simple spectrum matching analysis of multispectral imagery can be used to automatically subdivide the urban watershed into areas of vegetation, non-vegetation, and water (Fig. 1b). This simple breakdown very nearly represents a pervious versus impervious analysis of a watershed, obviously of great interest in urban hydrology. Unfortunately, bare soil and gravel which are pervious most of the year are classified with the other predominantly impervious non-vegetation areas such as concrete, asphalt, roofs, etc. A considerably more complex analysis shows the potential for an accurate automated analysis of urban surface materials (Fig. 1c). The same area is now automatically broken down into lawns, trees, water, rooftops, bare soil, gravel, and asphalt and the areal extent of each of these urban materials can also be calculated during the imagery processing. Colwell's study shows the feasibility for developing a computer analysis technique to accurately identify and map the areal extents of the surface materials in an urban scene. This technique will aid urban hydrologists by providing the important spatial input into urban watershed models. Currently most watershed simulation models use only a pervious-impervious classification of surface material. As these models become increasingly sophisticated, urban hydrologists are becoming more concerned with the degree of perviousness of surface materials from an input point of view. Rather than approximating this information by adjustment of physical parameters within the model, advanced process models will require a more detailed input of areal surface characteristics to reduce or eliminate the trial and error process. Computerized analysis of multispectral scanner imagery is capable of providing such an input, rapidly, over large areas, and repeatedly in a timely fashion and at short time intervals.

THE DYNAMIC NATURE OF URBAN WATERSHEDS

Thirteen of the small urbanized watersheds in the aforementioned USGS program by Gonzalez and Ducret were chosen for analysis in this study to show how the types of surface material in urbanizing watersheds change with time. These 13 watersheds are located in the residential suburbs surrounding Denver (Appendix B) and were chosen because of their well-delineated boundaries and because they are currently gaged for simultaneous measurement of rainfall and runoff. A historical sequence of aerial photographs was obtained for these watersheds, where available, since 1935 (Table 1). The most current set

TABLE 1. PERCENT PERVIOUS (P) AND IMPERVIOUS (I) COVER FOR 13 DENVER AREA WATERSHEDS, 1935-1970

WATERSHED PHOTO SOURCE AND DATE	1935 ¹		1949 ²		1954 ⁴		1956 ⁵		1959 ⁶		1963 ⁷		1968 ⁸		1970 ⁹	
	P	I	P	I	P	I	P	I	P	I	P	I	P	I	P	I
Arvada - N	np*	np	100	0	100	0	np	np	100	0	88	12	84	16	75	25
Arvada - S	np	np	100	0	99	1	np	np	99	1	87	13	np	np	62	38
Federal Heights	np	np	np	np	99	1	np	np	98	2	96	4	92	8	92	8
Northglenn 7204	np	np	np	np	100	0	np	np	100	0	100	0	48	52	45	55
Northglenn 7203	np	np	np	np	100	0	np	np	98	2	68	32	57	43	54	46
Northglenn 7201	np	np	np	np	100	0	np	np	100	0	86	14	53	47	50	50
Stapleton Airport	85	15	77	23	77	23	78	22	75	25	53	47	np	np	0	100
Stapleton - S	np	np	(1950) ³	62	38	np	np	64	36	65	35	np	np	61	39	
Aurora	np	np	98	2	100	0	np	np	99	1	94	6	np	np	63	37
Littleton	np	np	np	np	100	0	np	np	98	2	82	18	np	np	72	28
Fort Logan	np	np	100	0	100	0	np	np	100	0	84	16	np	np	51	49
Hyatt Lake - N	np	np	np	np	np	np	np	np	100	0	98	2	np	np	98	2
Hyatt Lake - S	np	np	np	np	np	np	np	np	98	2	98	2	np	np	96	4

1 - City Planning Office, Denver, 1935

2 - Colorado Aerial, Denver, June, 1949

3 - American Soil Conservation Service, Salt Lake City, 1950

4 - Colorado Aerial, Denver, April, 1954

5 - American Soil Conservation Service, Salt Lake City, 1956

6 - Colorado Aerial, Denver, July, 1959

7 - American Soil Conservation Service, Salt Lake City, August, 1963

8 - Hotchkiss, Inc., Denver, August, 1968

9 - E. M. Clark and Associates, June, 1970

* - No photographs available

of photographs of these watersheds (1970) was analyzed to determine the types of materials present and a list of ten surface materials, hereafter called watershed units, resulted. These materials in aggregate constitute all the different surface materials whose areas are greater than .5 percent of the total area of the watershed. The ten units are

1. concrete,
2. natural and fallow fields, abandoned land, pasture,
3. asphalt,
4. gardens, agricultural crop areas,
5. rooftops,
6. forested areas,
7. gravel,
8. exposed soil,
9. lawns, and
10. water

and it is into these units that these watershed should be classified by multispectral sensing.

All the photographs obtained in each historical sequence for each watershed were analyzed to determine the areas of the surface units in terms of percent of total area. Appendix C contains an explanation of the interpretive technique used on the photographs for areal analysis. Appendix D contains the tabulation of the results of this analysis. The percentage obtained for the impervious materials (concrete, asphalt, and rooftops) can be summed for each watershed and year as well as the percentage of pervious materials (Table 1). The percent imperviousness or perviousness as a function of year provides a simple index of urbanization of each watershed. This simple summary classification into impervious versus pervious areas is the current areal input into the simulation models used by the USGS to synthesize the runoff from these basins.

The progress of the urbanization of each watershed is shown graphically by plotting percent impervious cover as a function of calendar year for each of the thirteen watersheds, hereafter called imperviousness development curves. Several imperviousness development curves are accompanied by a selected sequence of the available historical airphotos to pictorially illustrate the urban development. Note that the Fort Logan Watershed was virtually undeveloped in 1959, but by 1970 was completely developed with most of the construction occurring between 1963 and 1970 (Figs. 2 and 3d). The Stapleton Airport Watershed passed through two major developmental stages, the first reaching approximately 22 percent impervious cover by about 1945, and remaining essentially static (Figs. 4 and 5a). The advent of jet aircraft in the 1960s necessitated further development and by 1970 the watershed was completely covered

by impervious material as airport runway aprons, hangar space, and terminal sizes increased. Three watersheds in Northglenn provide typical examples of the rapid growth of the Denver suburbs beginning in the 1960s (Figs. 6 and 7). Northglenn Shopping Center is partially in the Northglenn 7204 Watershed (Fig 6d). Extensive areas of impervious cover rapidly laid over large areas in this Center in parking lots and rooftops contributed significantly to the abnormally high rate of increase in imperviousness of this watershed (Fig. 7c).

The imperviousness development curve for each of the thirteen watersheds analyzed in this study provide an index of urbanization rates in and about Denver over the past 30 years (Figs. 3, 5, 7, and 8). As expected, such curves are quite sensitive to the type of development taking place which in turn regulates the hydrologic surface characteristics of the basin. A comparison of several imperviousness development curves demonstrates that the conversion of a natural watershed to an urban watershed can proceed at greatly differing rates (Fig. 9). Similarly, the degree to which a watershed has developed is reflected in its impervious cover and differs greatly, depending upon its particular type of urban use (Fig. 10a). Imperviousness development curves approaching an asymptote imply a steady-state land use which may range from 100 percent for a metropolitan jet airfield to 30 or 40 percent for an urban subdivision and to less than 10 percent for a natural watershed (Fig. 10a). A curve asymptotically approaching an imperviousness of 25 to 50 percent indicates an urban dwelling land use with relatively complete occupancy of the land. It is important from a hydrologic viewpoint to note that the difference in amount of impervious cover can vary more between two different urban land uses than between natural and subdivided land. Thus the urban hydrologist is as concerned about the water yield effects of the conversion of suburban watersheds to commercial use as he is about the conversion from natural or agricultural to suburban land use. A review of all thirteen imperviousness development curves show that the conversion from natural to suburban land use proceeds most rapidly taking only two to three years while the conversion from suburban to commercial land use proceeds at much slower rates.

Finally, the point at which a natural watershed was converted to urban land use is clearly reflected in its imperviousness development curve (Fig. 10b). Again, the curves approach asymptotes commensurate with their new land use. The point in time at which the conversion takes place relates

to the distance from the city core or local cores of commercial development. One consistent difference in impervious is apparent. The level approached is slightly higher for each successively new subdivision due to the trend toward larger dwellings, wider sidewalks, paved driveways, etc. (Fig. 10b).

The purpose of this historical analysis of imperviousness development of urban watershed surfaces was to clearly indicate the rapid and differing changes that occur and to highlight that a need exists for rapid and frequent analysis of the distribution of surface materials in urbanizing areas. This is not a need of the urban hydrologist alone but also of the city planner and other concerned municipal and county agencies. Annual or biannual analysis of the distribution of surface materials in urban areas can be based on small watersheds or other geographic cells. Remote sensing methods used together with the interpretation of historic airphotos of these units would produce well-defined development curves for all of a metropolitan area and its environs from which urban growth dynamics can be interpreted. Methods for collecting and interpreting remote multispectral imagery are becoming more sophisticated and the possibility of relatively low-cost yearly surveys and indexing of urban watersheds are imminent. Therefore, the question posed in this study is what kind of a remote multispectral mapping system would best map the ten key watershed units identified by the airphoto interpretation.

CLASSIFICATION OF URBAN WATERSHED UNITS BY REMOTE MULTISPECTRAL SENSING

The non-photographic multispectral mappers currently in operation are line scanning devices. They measure electromagnetic energy simultaneously from the air in a number of discrete wavelength bands at each instant of time for a small spot on the ground. This spot is swept or scanned perpendicular to the aircraft's forward motion to form a simultaneous image in each wavelength band. The level of energy (radiance*) received in each of these wavelength bands is dependent upon the reflectance** (or emissance) characteristics of the material under surveillance. All the simultaneous measurements made in the various wavelength bands taken together define a discrete spectral

*radiance is the electromagnetic energy coming from the surface by reflection or emission.

**reflectance is the ratio of the energy reflected from a surface to that incident upon it.

curve for the surface imaged at that particular instant, namely a curve of surface radiance as a function of wavelength, a spectroradiance curve. This curve is called the spectral signature of the ground point observed. Each type of surface material reflects electromagnetic energy with a reasonably consistent level in each wavelength band sensed giving a characteristic spectral signature for that surface. These levels vary, however, between different types of surface materials producing characteristic spectral signatures for each.

The output of a multispectral scanning device is recorded on parallel analog tape tracks (or digitally) as the ground is scanned and any slice across these parallel recording tracks represents the spectroradiance curve received from the scene at that instant of time. This method of recording multispectral images readily lends itself to rapid automatic analysis by computer to map the materials in the scene that are of particular interest.

The early identification by air photo interpretation of the ten surface units whose areas are each greater than .5 percent of the total area of the thirteen study watersheds had a dual purpose. These units must be sufficiently different in spectral signature so that they can be individually mapped by automatic computer processing of remote multispectral imagery. The same units must also contain as a subset the classification of the watersheds into their important hydrologic surface units. The object of the use of remote multispectral imagery is to map the surface materials in the watersheds automatically according to their spectral signature and determine their respective area and location. The resulting surface classifications in a remote sensing sense can then be logically combined according to the input requirements of the watershed model (Fig. 11). For example, asphalt and concrete are very different in spectral signature and must be mapped by remote multispectral sensing as two entirely different surface materials and yet they have identical surface hydrology. After their separate classification in automatic image reduction they can be combined into one area. This area is, in turn, refined by referring its location to a topographic model of the basin to account for depression storage. rooftops are also separately mapped and entered into this same impervious hydrologic unit but require refinement to account for pitch slope (not to be confused with topographic slope). The final summation of all three surface materials yields the area and location of the impervious surfaces within the watershed for entry into the simulation model (Fig. 11).

Lawns, bare soil, and the other semipervious surface material units need individual refinement for interception rate, infiltration capacity, and antecedent soil moisture level (Fig. 11). The values of these hydrologic characteristics to be assigned to each surface material unit can be obtained by statistical field sampling in each surface unit, i.e., ground control measurements with reference to remote sensing. For example, interception rate, infiltration capacity, and antecedent soil moisture level can be measured from randomly selected lawns within the area mapped. The results can be combined to yield mean and variance levels for the soil hydrologic parameters needed for the lawn area at the time of water yield simulation. These hydrologic characteristics for each surface unit could also be simulated by 'process' subroutines in the simulation model. These subroutines would predict the needed hydrologic characteristics of the surface material unit, i.e., lawns, bare soil, etc., from limited field measurements, input precipitation, potential E-T, and topography, to be used with the areal classifications produced by the multispectral mapping.

The topographic data base used in the refinement of the surface units can be a topographic model (Oliver and Miller, 1971). This approach associates slope, aspect, and elevation values in a computer framework with each surface material cell classified by remote multispectral imaging. The topographic model can also be used in connection with the routing of surface flow in the main water yield simulation model.

The reader is cautioned that this explanation and associated diagram is generally conceptual. The specific input refinements needed for each surface unit mapped are the responsibility of the watershed simulation model and depend to a large extent on the type of modeling approach applied, i.e., process, empirical, static, dynamic, etc.

ANALYSIS OF URBAN WATERSHED SPECTRAL CHARACTERISTICS

Multispectral imaging hardware is constantly being improved and is sampling in a larger number of wavelength bands, in narrower bands, and over a wider range of the electromagnetic spectrum. Computerized analysis of multispectral imagery utilizing many selected wavelength bands simultaneously can distinguish the surface materials in the scene (Figs. 1b and 1c). It is possible to achieve satisfactory, even improved, classification with considerable economy in computer time by using a properly selected subset of the total available wavelength bands. The balance of this report is devoted to the procedure developed

for optimizing the selection of the wavelength bands best suited to map the ten surface materials which define the Denver watersheds from an areal importance and multispectral imaging viewpoint.

The core of the optimization process used is the Euclidean distance algorithm which mathematically describes the distance between any two spectral curves in specified wavelength bands.

This Euclidean distance is

$$d = \left(\sum_{i=1}^n \frac{(B_i - A_i)^2}{S_p^2} \right)^{1/2}$$

where d = Euclidean distance,

A = average reflectance for material A in the i^{th} wavelength band,

B = average reflectance for material B in the i^{th} wavelength band,

n = number of optimum wavelength bands,

S_p^2 = pooled variance for N samples each for materials A and B in the i^{th} wavelength band where

$$S_p^2 = (S_{A_i}^2 + S_{B_i}^2)/2$$

and where N is the number of samples, i.e., the number of spectral curves used. N is constant for all materials, thus the simplified expression for pooled variance. The application of this technique can be outlined in five steps.

- 1) Determine the total number of wavelength bands over which the scene (watershed) can be simultaneously imaged by a particular multispectral scanner.*
- 2) The average reflectance (ρ) and its variance (S^2) are calculated in each of the wavelength bands determined above for each of the materials in the scene. Each value is assigned a position in a matrix in Table 2 where rows = curve numbers of surface materials and columns = wavelength bands. One matrix [AVE(i,j)] contains reflectance averages, and another [VAR(i,j)] contains the variance.

* this could be either an existing device such as the University of Michigan 12 band scanner or the NASA-Bendix 24 band scanner or it might be a conceptual device yet to be constructed such as a special, simplified scanner optimized exclusively for urban mapping.

TABLE 2. MEAN REFLECTANCE (ρ) AND VARIANCE (S^2) MATRICES [$AVE(i,j)$] AND [$VAR(i,j)$] RESPECTIVELY. These matrices of mean reflectance and variance over each wavelength band are all the data used in the Euclidean distance (d) computations.

SURFACE MATERIAL		SPECTRAL BAND			
		1	2	3	4
1 GRASS		ρ_{11} S^2_{11}	ρ_{12} S^2_{12}	ρ_{13} S^2_{13}	ρ_{14} S^2_{14}
2 BARE SOIL		ρ_{21} S^2_{21}	ρ_{22} S^2_{22}	ρ_{23} S^2_{23}	ρ_{24} S^2_{24}
3 CONCRETE		ρ_{31} S^2_{31}	ρ_{32} S^2_{32}	ρ_{33} S^2_{33}	ρ_{34} S^2_{34}
4 ASPHALT		ρ_{41} S^2_{41}	ρ_{42} S^2_{42}	ρ_{43} S^2_{43}	ρ_{44} S^2_{44}

- 3) In each wavelength band, all combinations of surface materials taken two at a time are determined. The difference in reflectance of the two average reflectance values for each combination is calculated, squared, and divided by the pooled variance of the average reflectance of the two materials. The results of this operation are stored in a matrix $[U(IE,I)]$ in Table 3 where rows represent the two-curve combinations and columns represent wavelength bands. This step calculates and lays aside all the values within the summation sign in the Euclidean distance formula.
- 4) The rows of the $[U(IE,I)]$ matrix are summed and raised to the $1/2$ power giving d , the Euclidean distance, for all possible unique combinations of the number of wavelength bands chosen for optimization. The first value calculated is the Euclidean distance for the first two-material combination, e.g. concrete and asphalt. The operation is repeated for all two-material combinations, e.g. concrete and asphalt, concrete and lawns, etc., saving the highest and lowest Euclidean distances, and calculating the average Euclidean distance. These three values are printed out, for the first wavelength band combination, and the entire process is repeated for each subsequent wavelength band combination.
- 5) The average, minimum, and maximum Euclidean distances for each combination of wavelength bands are compared to select the best combination showing a high average, high minimum, and a high maximum, with the greatest emphasis given to the average Euclidean distance.

A further refinement of the Euclidean distance method, although not used in this study, would be to multiply each two-curve (material) combination value calculated in step 2 by a weighting factor indicating the importance, from a hydrologic viewpoint, of differentiating the two materials in question. For example, asphalt and concrete are easy to separate spectrally but should not heavily influence this spectral band optimization procedure as they are hydrologically identical in behavior and, therefore, their spectral separation is not important. On the other hand, concrete and bare soil are dissimilar in surface hydrology while their spectroreflectance might be similar, especially for old and dirty concrete. Thus, their spectral separation should be more heavily weighted in the optimization computation. The concrete-asphalt

TABLE 3. INTERMEDIATE MATRIX [U(IE,I)] USED IN CALCULATING THE EUCLIDEAN DISTANCE (d) FOR THE BEST 1, 2, 3, OR 4 OUT OF 4 WAVELENGTH BANDS. The matrix contains the squared differences in the mean reflectances and squared sums of the pooled variance from Table 2 for all possible combinations of four surface materials taken two at a time in each of the four spectral bands.

SPECTRAL BAND	1	2	3	4
SURFACE MATERIAL COMBINATION				
1 - 2	$\frac{(\rho_{11} - \rho_{21})^2}{(S_{11}^2 + S_{21}^2)/2}$	$\frac{(\rho_{12} - \rho_{22})^2}{(S_{12}^2 + S_{22}^2)/2}$	$\frac{(\rho_{13} - \rho_{23})^2}{(S_{13}^2 + S_{23}^2)/2}$	$\frac{(\rho_{14} - \rho_{24})^2}{(S_{14}^2 + S_{24}^2)/2}$
1 - 3	$\frac{(\rho_{11} - \rho_{31})^2}{(S_{11}^2 + S_{31}^2)/2}$	$\frac{(\rho_{12} - \rho_{32})^2}{(S_{12}^2 + S_{32}^2)/2}$	$\frac{(\rho_{13} - \rho_{33})^2}{(S_{13}^2 + S_{33}^2)/2}$	$\frac{(\rho_{14} - \rho_{34})^2}{(S_{14}^2 + S_{34}^2)/2}$
1 - 4	$\frac{(\rho_{11} - \rho_{41})^2}{(S_{11}^2 + S_{41}^2)/2}$	$\frac{(\rho_{12} - \rho_{42})^2}{(S_{12}^2 + S_{42}^2)/2}$	$\frac{(\rho_{13} - \rho_{43})^2}{(S_{13}^2 + S_{43}^2)/2}$	$\frac{(\rho_{14} - \rho_{44})^2}{(S_{14}^2 + S_{44}^2)/2}$
2 - 3	$\frac{(\rho_{21} - \rho_{31})^2}{(S_{21}^2 + S_{31}^2)/2}$	$\frac{(\rho_{22} - \rho_{32})^2}{(S_{22}^2 + S_{32}^2)/2}$	$\frac{(\rho_{23} - \rho_{33})^2}{(S_{23}^2 + S_{33}^2)/2}$	$\frac{(\rho_{24} - \rho_{34})^2}{(S_{24}^2 + S_{34}^2)/2}$
2 - 4	$\frac{(\rho_{21} - \rho_{41})^2}{(S_{21}^2 + S_{41}^2)/2}$	$\frac{(\rho_{22} - \rho_{42})^2}{(S_{22}^2 + S_{42}^2)/2}$	$\frac{(\rho_{23} - \rho_{43})^2}{(S_{23}^2 + S_{43}^2)/2}$	$\frac{(\rho_{24} - \rho_{44})^2}{(S_{24}^2 + S_{44}^2)/2}$
3 - 4	$\frac{(\rho_{31} - \rho_{41})^2}{(S_{31}^2 + S_{41}^2)/2}$	$\frac{(\rho_{32} - \rho_{42})^2}{(S_{32}^2 + S_{42}^2)/2}$	$\frac{(\rho_{33} - \rho_{43})^2}{(S_{33}^2 + S_{43}^2)/2}$	$\frac{(\rho_{34} - \rho_{44})^2}{(S_{34}^2 + S_{44}^2)/2}$

combination should have a low weighting factor, say 0.3, while the concrete-bare soil combination should be fully weighted to 1.0. This emphasizes the hydrologic behavior of each of the materials in the spectral optimization procedure and underscores the needed intercoupling of watershed modeling objectives and remote sensing methods. The subjective selection of the numeric weighting factors is the delicate, fine tuning of the optimization procedure done jointly by the hydrologist and the remote sensing specialist.

Another improvement in the optimization would be to account for the cross-overs or intersections in spectroreflectance curves of the surface materials. This requires the calculation of correlations for each two-material combination for comparison in each of the possible wavelength band combinations generated in the optimization process.* The presence of crossovers in the spectroreflectance curves of materials represents a greater dissimilarity of the materials and, therefore, leads to a more powerful optimization solution. However, the differentiation of asphalt from concrete from lawns, etc., is simpler due to their greatly differing spectroreflectances than the differentiation of materials in natural land areas such as the various prairie vegetation types whose classification has also been attempted using remote multispectral imaging. Thus, the simpler Euclidean distance method outlined is believed to be sufficiently accurate at present to select the wavelength bands to best map the surface materials in urban watersheds.

SPECTROREFLECTANCE MEASUREMENTS OF URBAN SURFACE MATERIALS

The input data for the optimization routine was obtained by field measurements of the ten significant surface materials present in the thirteen Denver watersheds. A field spectrometer was used to produce statistically significant spectroreflectance curves for each material. The principle components of this field spectrometer are a mini computer system (Fig. 12a) and associated FORTRAN data acquisition programs, a spectroradiometer (Fig. 12b), and a field trailer and ancillary equipment (Fig. 12c). Using this system, the in situ spectroreflectance of natural materials can be measured in the field at any view angle for all .005 μm wavelength intervals between .3 and 1.6 μm (Pearson and Miller, 1971). All spectroreflectance curves used in this study were measured by this device under natural sunlight in the field and normal to the surface of the material.

*this computational procedure has been designed but was not implemented in time to be used in the sample computations in this report.

The spectrometer system measures the total spectroreflectance curve in three segments, the ultraviolet, the visible, and the near infrared and punches these three segments on paper tape and simultaneously plots them (Fig. 13a) using a FORTRAN program called SAMPL (Pearson and Miller, 1971). A FORTRAN program called JOIN (Appendices E and F) re-reads the original punched tapes back into the mini computer and forms one composite spectroreflectance curve (Fig. 13b) and punched tape for each measurement of each material. Each of the ten surface materials were duplicated three times to represent the expected natural variability in them. Two spectroreflectance curves were measured at different positions on the three samples of each surface material giving six spectroreflectance curves for each of the ten materials defining the urban watershed (Fig. 14). The samples used were:

- 1) concrete (two curves of each of new, old but clean, and old and dirty (Fig. 14a),
- 2) asphalt (two curves of each of new, old but clean, and old and dirty),
- 3) rooftops (six curves of various colors and ages),
- 4) bare soil (two curves of each of three types differing in surface color),
- 5) gravel (two curves of each of three natural samples differing in particle size and type),
- 6) lawns (two curves on each of sparse, medium, and thick Kentucky Bluegrass (Fig. 14b),
- 7) trees (six curves on small Cottonwood trees),
- 8) pasture and fallow fields (two curves on each of three samples of natural grassland),
- 9) agricultural (six curves of wheat stubble and six of sugar beets used separately), and
- 10) water (two curves on shallow water in a blackened container with three types of bottom materials).

The six curves taken for each of the ten materials were averaged at .005 μm intervals by a FORTRAN program, AVER (Appendices E and F) which reads in the paper tape versions of the JOINed data curves and calculates the average spectroreflectance and its variance at each wavelength. AVER plots these mean

spectroreflectance curves for each material together with a curve envelope of $\pm 1 \sigma$ and simultaneously punches a new paper tape with the mean and variance values at .005 μm intervals (Fig. 15). In this fashion, mean spectroreflectance and variance curves were produced for each of the materials which can now be compared in terms of their statistically significant spectral differences (Fig. 16).

QUALITATIVE INTERPRETATION OF THE SPECTROREFLECTANCE CURVES WITH REFERENCE TO MULTIBAND PHOTOGRAPHY

Water was so different from the other nine surface classes that it was dropped from the further analysis as it is readily identifiable at virtually all wavelengths and combinations of wavelengths due to its unique spectroreflectance. The agricultural unit was divided into the two predominant crops present in larger areas in the early summer. These materials, wheat stubble and green sugar beet foliage, could not be lumped as one spectral unit. The natural breakdown of these ten materials into the two general classes of vegetation and non-vegetation is readily apparent (Fig. 17). All the mean curves for vegetation have a rise in spectroreflectance at .55 μm or green portion of the spectrum and an even greater rise at .7 μm or the beginning of the photo-infrared. However, the two drier vegetation surfaces of wheat stubble and fallow field do not have the high reflectance plateau in the photo infrared characteristic of healthy green vegetation nor the low reflectance at .68 μm resulting from chlorophyll absorption. All curves show a significantly steady decrease at wavelengths greater than .9 μm . Non-vegetation shows a higher reflectance in the red (.6 μm to 7 μm) than the vegetation and continues to increase rather than decrease above .9 μm . It should be clear that the best single band in which to differentiate these two material classes would be between 1.1 and 1.3 μm .

A more meaningful single breakdown for the urban hydrologist would be into pervious versus impervious surfaces (Fig. 18). Unfortunately, this is not the same situation as the natural and easy spectroreflectance separation of vegetation and non-vegetation (Figs. 1b and 17) as the non-vegetation surfaces of concrete, asphalt, and shingles are impervious while bare soil and gravel are not. While the five non-vegetation surfaces were spectrally similar to a first approximation, the collection of vegetative materials into one class of pervious land together with bare soil and gravel areas is clearly not

spectrally similar (Fig. 18b). Thus, clearly the urban watershed cannot be separated directly into pervious and impervious surface areas based on spectral signature but must first be mapped into the ten different surface materials which can subsequently be recombined into two classes if desired (Figs. 1c and 11).

Eight of the thirteen small watersheds studied in Denver were photographed from the air during April, 1971, by a nine-inch format aerial camera using Ektachrome Aero IR film and a four-band multiband camera. The eight watersheds photographed were Northglenn (all three), Federal Heights, Arvada-N, Arvada-S, Hyatt Lake-N, and Hyatt Lake-S (Appendix B). The multiband camera yielded four separate photographs covering the same identical scene, in the blue, green, red, and photographic infrared portions of the spectrum (Fig. 19). These individual black and white film frames can be colored in any color and superimposed in varying intensities by a special color projection device yielding a color enhanced image. The important difference in spectral contrasts just noted between vegetation and non-vegetation versus impervious and pervious materials can be clearly shown in this fashion with the multiband imagery. Two of the frames, the red (.6 to .7 μm) and infrared images (.7 to .9 μm) are color coded red and blue respectively and superimposed to show the Northglenn 7201 watershed in false color (Fig. 20). The red colored image shows non-vegetative areas clearly as a red or pink color, while healthy green vegetation, having a high reflectance in the photographic infrared is color coded as blue. The red and blue areas, therefore, resemble an impervious-pervious classification of surface materials, with the exception of gravel and bare soil which, as predicted from the spectroreflectances, are incorrectly coded the color of impervious areas. Thus, these multiband photos show in specially enhanced pictures the degree to which nature provided a significant spectral difference between pervious and impervious materials.

The Ektachrome infrared air photos were obtained for the eight watersheds to provide detailed high resolution imagery (Frontpiece). The areas coded in red on these photos represent high reflectance in the photographic infrared and can be noted wherever healthy vegetation is present, especially in the lawns and open fields. This photography can be used for accurately preparing a map by conventional photo interpretation methods of the ten surface materials for comparison with the enhanced multiband imagery. More importantly, these accurate maps of surface materials can be compared with the results of automatic

image processing of multispectral imagery of these basins when such imagery becomes available.*

OPTIMIZATION OF THE DEVICE AND/OR IMAGE PROCESSING
FOR MULTISPECTRAL MAPPING OF URBAN WATERSHEDS

The curves output by AVER for each of the ten materials excluding water were input into a FORTRAN computer program, OPTIM (Appendices E and F), which performs all but the last step in the optimization procedure outlined in the earlier section. The mean curves and their variance are read by OPTIM and the average reflectance and variance is calculated for each wavelength band used in the multispectral scanner being analyzed. One analysis by OPTIM sought the best single band and best four bands of the 12 wavelength bands used on the 12 channel University of Michigan multispectral scanner, a device widely used for remote multispectral imaging. The 12 spectral bands used on this device occur in Table 4. Table 5 shows in abbreviated form how the data is stored in OPTIM. The mean reflectance values and the corresponding averaged variances in the 12 wavelength intervals are stored in separate matrices $[AVE(i,j)]$ and $[VAR(i,j)]$ respectively where i represents the number of the material, and j represents the wavelength interval number. For simplicity both the mean reflectance over each wavelength band (ρ) and the corresponding mean variance (S^2) are shown in Table 5. The matrix of squared differences of two-material combinations $[U(IE,I)]$ in Table 6 gives the values within the summation sign of the Euclidean distance equation as outlined in step 3 of the optimization process. The operations on the proper ρ and S^2 values are in the appropriate locations of this matrix, where rows represent the two material combinations, consecutively numbered in the order they are generated, and columns again represent band numbers. Calculations of minimum, maximum, and average Euclidean distances were made for optimally selecting the best 1, 2, 3, ..., 12 wavelength bands in the manner outlined in step 4 of the optimization procedure using numerical data from the spectroreflectance measurements in the $[U(IE,I)]$ matrix. The proper band combinations are generated and the corresponding proper elements of the $[U(IE,I)]$ matrix are selected, summed, and raised to the 1/2 power for each of the two material combinations for each particular band combination. The minimum and maximum Euclidean distance between each two materials is listed under the band

*working computer programs for automatic multispectral image processing are available at Colorado State University (Smith, Miller, and Ells, 1972).

TABLE 4. TWELVE SPECTRAL BANDS OF TYPICAL SIMULTANEOUS MULTISPECTRAL SCANNER

Spectral Band (Channel No.)	Wavelength Interval	Spectral Band (Channel No.)	Wavelength Interval
1	.40-.44μm	7	.55-.58μm
2	.44-.46μm	8	.58-.62μm
3	.46-.48μm	9	.62-.66μm
4	.48-.50μm	10	.66-.72μm
5	.50-.52μm	11	.72-.80μm
6	.52-.55μm	12	.80-1.0μm

TABLE 5. MEAN REFLECTANCE (ρ) AND VARIANCE (S^2) MATRICES [$AVE(i,j)$] AND [$VAR(i,j)$], RESPECTIVELY. These matrices of mean reflectance and pooled variance over each of twelve wavelength bands are the data used in the Euclidean distance (d) computation.

SPECTRAL BAND		1	2	3	--	--	11	12
SURFACE MATERIAL		ρ_{11}	ρ_{12}	ρ_{13}	--	--	ρ_{111}	ρ_{112}
1 GRASS	S^2_{11}	S^2_{12}	S^2_{13}	--	--		S^2_{111}	S^2_{112}
	ρ_{21}	ρ_{22}	ρ_{23}	--	--		ρ_{211}	ρ_{212}
2 CONCRETE	S^2_{21}	S^2_{22}	S^2_{23}	--	--		S^2_{211}	S^2_{212}
	ρ_{31}	ρ_{32}	ρ_{33}	--	--		ρ_{311}	ρ_{312}
3 BARE SOIL	S^2_{31}	S^2_{32}	S^2_{33}	--	--		S^2_{311}	S^2_{312}
	:	:	:	:			:	:
10 ASPHALT	ρ_{101}	ρ_{102}	ρ_{103}	--	--		ρ_{1011}	ρ_{1012}
	S^2_{101}	S^2_{102}	S^2_{103}	--	--		S^2_{1011}	S^2_{1012}

TABLE 6. INTERMEDIATE MATRIX [$U(IE, I)$] USED IN CALCULATING THE EUCLIDEAN DISTANCE (d) FOR THE BEST 1, 2, 3, ..., 12 OUT OF 12 WAVELENGTH BANDS. The matrix contains the squared differences in mean reflectances and squared sums of pooled variance from Table 4 for all possible combinations of ten surface materials taken two at a time in each of the twelve available spectral bands.

SURFACE MATERIAL COMBINATION	SPECTRAL BAND	1	2	12	
		$(\rho_{11} - \rho_{21})^2$ $(S_{11}^2 + S_{21}^2)/2$	$(\rho_{12} - \rho_{22})^2$ $(S_{12}^2 + S_{22}^2)/2$	-- --	$(\rho_{112} - \rho_{212})^2$ $(S_{112}^2 + S_{212}^2)/2$
1 - 2					
1 - 3		$(\rho_{11} - \rho_{31})^2$ $(S_{11}^2 + S_{31}^2)/2$	$(\rho_{12} - \rho_{32})^2$ $(S_{12}^2 + S_{32}^2)/2$	-- --	$(\rho_{112} - \rho_{312})^2$ $(S_{11}^2 - S_{112}^2)/2$
1 - 4		$(\rho_{11} - \rho_{41})^2$ $(S_{11}^2 + S_{41}^2)/2$	$(\rho_{12} - \rho_{42})^2$ $(S_{12}^2 + S_{42}^2)/2$	-- --	$(\rho_{112} - \rho_{412})^2$ $(S_{112}^2 + S_{412}^2)/2$
.		.	.		.
.		.	.		.
.		.	.		.
9 - 10		$(\rho_{91} - \rho_{101})^2$ $(S_{91}^2 + S_{101}^2)/2$	$(\rho_{92} - \rho_{102})^2$ $(S_{92}^2 + S_{102}^2)/2$	-- --	$(\rho_{912} - \rho_{1012})^2$ $(S_{912}^2 + S_{1012}^2)/2$

combination, and the average Euclidean distance for all two-material combinations is calculated, and also listed under the wavelength combination. This entire process is repeated for all wavelength interval combinations providing the data from which the best wavelength band combinations will be selected.

OPTIM computations were made for the Euclidean distances with which to select the best single wavelength interval for differentiating the urban materials from the 12 available on the University of Michigan multispectral scanner (Fig. 21). It can be deduced from this data that wavelength interval 2 or .44 to .46 μm is the best single band in which to simultaneously differentiate all ten surface materials because it shows the largest minimum (meaning that the closest 2 materials' spectroreflectance curves are further apart than in any other of the 12 wavelength bands), the largest maximum (greatest separation of curves farthest apart) and the largest average (greatest overall separation of all combinations of the ten curves). Visual inspection of the mean spectroreflectance curves for the materials (Fig. 21) indicates that the wavelength interval 2 is not the apparent position of maximum reflectance separation. This visual interpretation of only mean curves without regard to their statistical variance is misleading. The mean curves for these materials appear (Fig. 21) to be separated more greatly in wavelength interval 12 or 0.8 -1.0 μm , but the statistical variation is much greater in this band. The Euclidean distance calculations using the statistical variation therefore gives a more correct optimization result than would be determined by visual inspection of mean spectroreflectance curves, even for the simple selection of the single wavelength band in which to separate the ten materials.

The selection of the proper combination from the Euclidean distance calculations becomes more complex when optimizing for a choice of several best spectral bands taken simultaneously. For example, consider the selection of 4 spectral bands out of the 12. There are a total of 495 possible combinations of 12 items taken 4 at a time.* Examination of the 10 highest and 3 lowest combinations are listed from which the selection of the best 4 simultaneous wavelengths to map the urban scene may be made (Fig. 22). The 3 lowest values are listed solely for indicating the total range of Euclidean distance statistics calculated. From this data, it becomes apparent that the selection of the best one of the 4 band combinations is still a subjective value judgment. In selecting the one optimum combination the average should be weighted most

*the solution for the best 4 of the 12 bands for the 10 materials including all the numerical matrices involved occur in Appendix E on pages E-6 and E-7.

heavily, since it reflects the overall distribution of the curves. The best combination, therefore, would be intervals 1, 2, 3, and 4 from a purely numeric viewpoint. However, since curve crossovers are not accounted for by this technique, visual inspection of all of the mean curves suggests the selection of intervals 1, 2, 4, and 9 as the best combination since it occurs high up in both average and maximum Euclidean distances. To emphasize curve crossovers (intersections) at the expense of the Euclidean distance optimization calculations, the combination 1, 2, 4, and 12 is selected to utilize the vegetation-non-vegetation contrasts in the visible to the infrared regions. The selection of combination 1, 2, 4, and 9 does account for some mean curve crossovers in the green portion of the visible spectrum and is one of the optimal sets based solely on the Euclidean distance optimization calculations. This optimum combination for the ten materials defining the scene in the available 12 wavelength intervals could now be implemented in a simple 4 band multiband camera or processed from amongst the 12 available by the spectrum matching technique.

CONCLUSIONS

The choice of the optimum wavelength bands with which to map the urbanizing watershed is a complex process from a spectral point of view, still requiring subjective decisions. Equally important is the determination of the materials which are to define the scene together with the variation in these materials both spectrally and hydrologically, throughout the different seasons of the year. Ground measurements of the spectral properties of more of the important surface materials is recommended. This should include a thorough analysis of changes in the spectral and hydrological properties throughout the different seasons of the year. Seasonal data may be used to optimize the mapping operation spectrally and temporally. Spectral-time surfaces could be examined in 3 space with reflectance plotted as a function of both wavelength and time. Some curves will remain constant throughout the year, but others change, particularly vegetation, therefore providing another variable that can be used to distinguish and map urban materials. The measurements and results obtained in one urbanizing fringe such as that around Denver are generally applicable throughout the U. S. with the exception that spectroreflectance curves of some natural materials, especially vegetation, must be remeasured as a function of season for each metropolitan area.

The Euclidean distance method has been shown to effectively indicate the amount of minimum and maximum curve separation and overall curve distribution within any combination of wavelength bands while at the same time accounting for statistical variation within the spectral characteristics of the classes of materials to be imaged. The method has also been shown to be superior to inspection of mean curves by eye, but its most serious drawback is its failure to account for the information contained in curve crossovers or intersections. However, a more complicated optimization routine has been designed which will consider these crossovers by using correlation statistics. The most significant spectral difference in vegetation and non-vegetation is the contrast between the two surface classes in the red and infrared portions of the spectrum, resulting in a large number of curve crossovers (Figs. 16, 17, and 18). Therefore, future efforts for wavelength band optimization of vegetation and non-vegetation materials must utilize these techniques for recognizing curve crossovers such as the comparison of correlations from one band or band combinations to other bands.

Once the method for data collection has been optimized and multispectral imagery obtained over the urban fringe areas of interest, it is possible to analyze the data automatically using spectrum matching techniques to accurately calculate the area and distribution of each significant watershed surface material. The multispectral imagery can be analyzed for any combination of surface materials depending upon the requirements of the watershed model in question, and the results can be converted to hydrologic units and used as a direct input into the simulation model. This approach will bypass the subjective, laborious air photo interpretation of the surface cover types of the watershed. It should thus be possible to produce yearly maps of surface materials in urbanizing watersheds to keep simulation models current for flood prediction, etc. The computer mapping of surface materials could also produce the simple pervious-impervious classification, which many hydrologic models presently operating use as an input, or it could provide the more complicated breakdown of surface materials as input into the more complex research models. The detailed breakdown of surface cover required by these sophisticated process models rules out the practicability of human photo interpretation which could not keep pace with the yearly changes in the urbanizing areas. The use of remote multispectral sensing mapping methods by hydrologists involved in urban watershed modeling is therefore suggested to determine if "limiting

factor" such as accurate, timely surface material maps are, in fact, limiting in process model design.

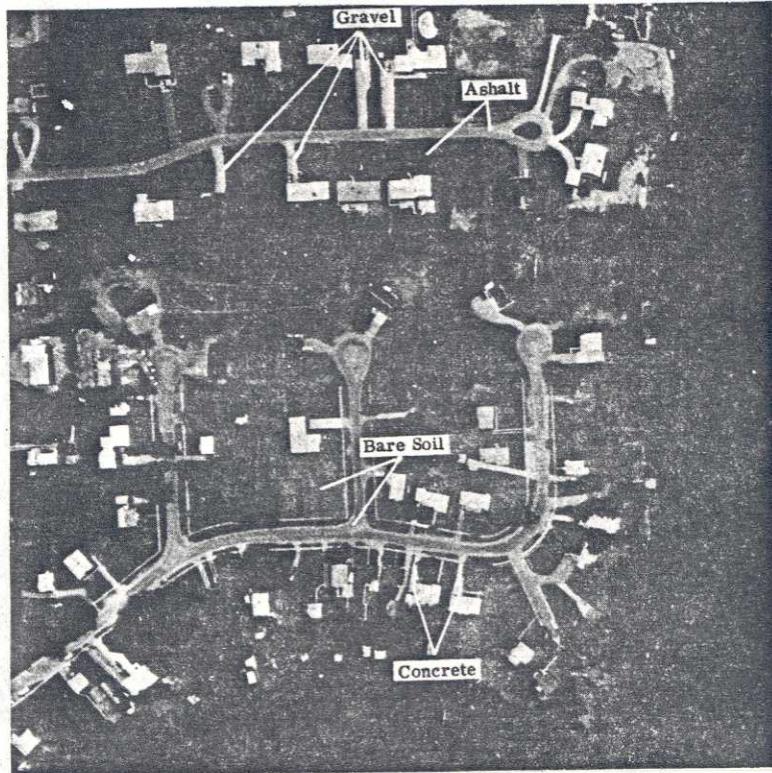
The next logical research step in this investigation is the expanded study of the eight Denver watersheds that have been analyzed and photographed. After more detailed ground study of spectral properties of the urban materials, including variation with seasons, actual multispectral scanner imagery should be flown over the watersheds at several times during the year. The multispectral imagery should be interpreted by computer and the accuracy of identifications of the watershed units and their calculated surface areas should be compared for accuracy with human identification and areal measurement of these same units. This could be accomplished by interpretation of blown up prints of color and color infrared photographs taken concurrently with each multispectral image collection mission.

After the degree of accuracy of the computer interpretation by spectrum matching is determined, experiments should be conducted for identifying three-dimensional spectroreflectance surfaces by including the time element for each curve to see if using three-dimensional spectral surfaces results in a greater mapping accuracy than the examination of the current spectroreflectance curves of the materials. In any further study, emphasis would be placed on additional collaboration with hydrologists involved in urban watershed modeling, especially those researching advanced models in order that both disciplines might effectively communicate and test their current requirements and objectives.

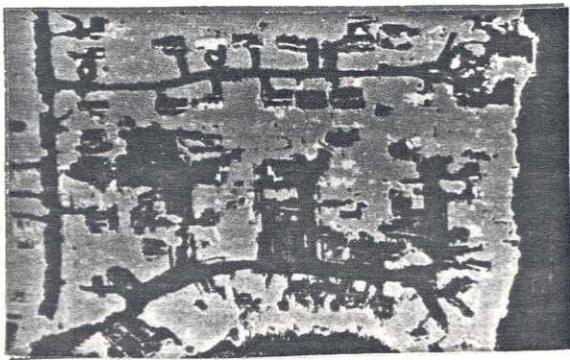
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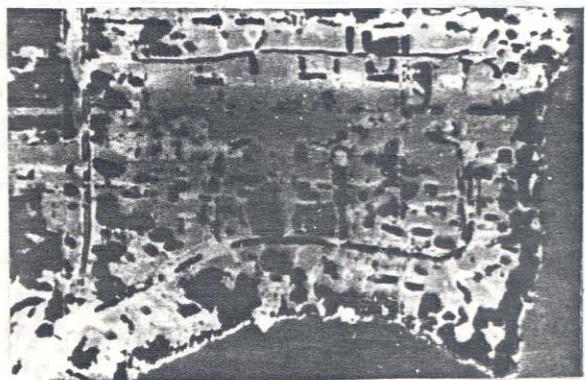


(a) reference airphoto - Belleville, Michigan area



(b) simple color-coded
recognition map

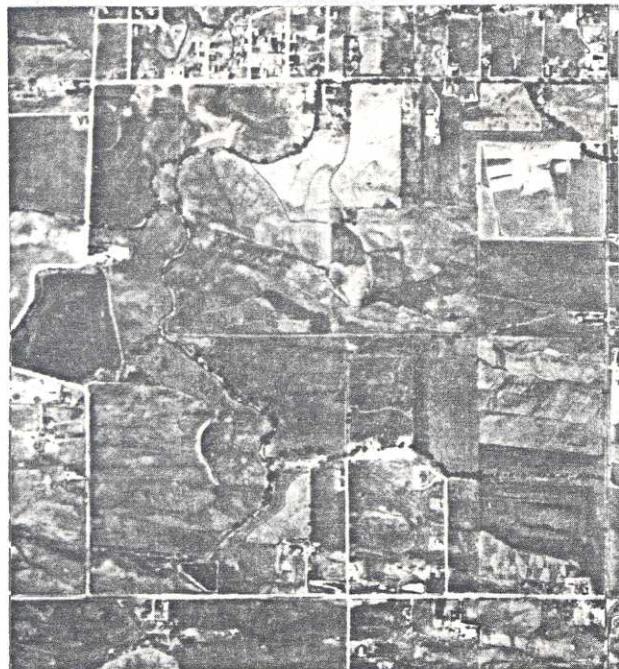
blue = water
green = vegetation
brown = nonvegetation



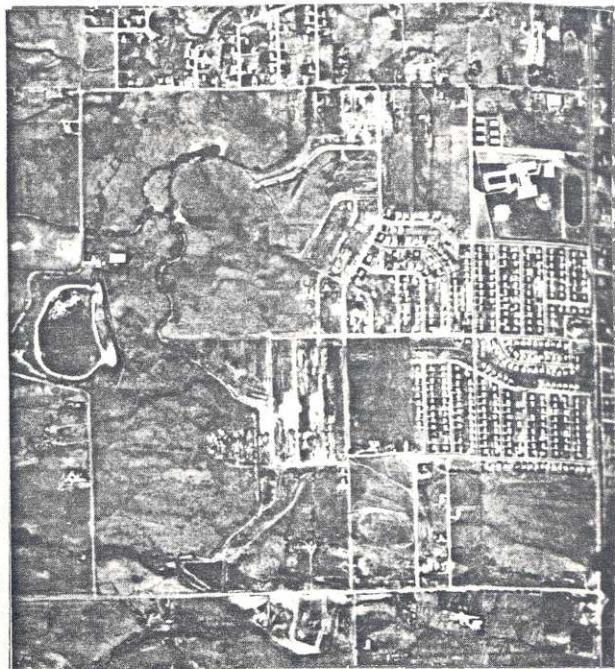
(c) complex color-coded
recognition map

blue = water	red = roofs
cyan = lawns	green = trees
dark brown = bare soil	
yellow brown = asphalt	

FIGURE 1. RECOGNITION MAPS OF A SUBURBAN SCENE AUTOMATICALLY PREPARED FROM REMOTE MULTISPECTRAL IMAGERY. The areal features were classified on an analog computer using techniques of automatic image interpretation by the University of Michigan. (b) Using ten spectral bands between .4 μm and 1.0 μm . (c) Using six spectral bands between .4 μm and 1.0 μm . (J. E. Colwell, 1970)



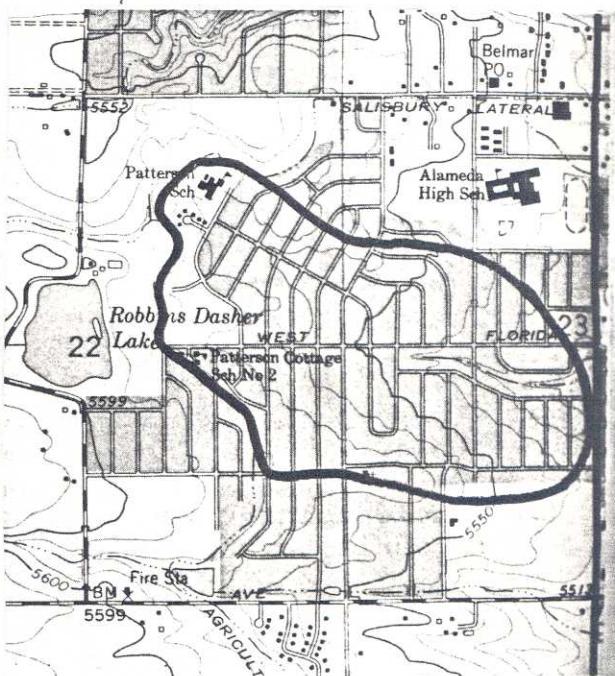
(a) 1959



(b) 1963



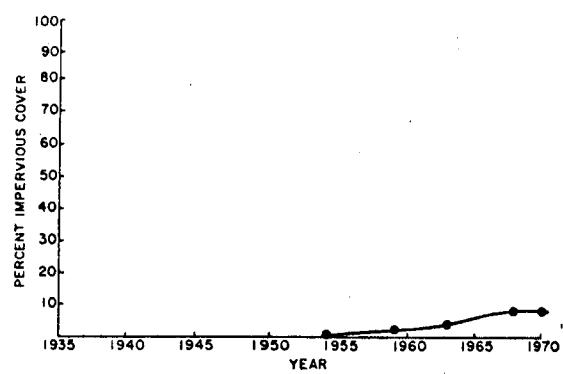
(c) 1970



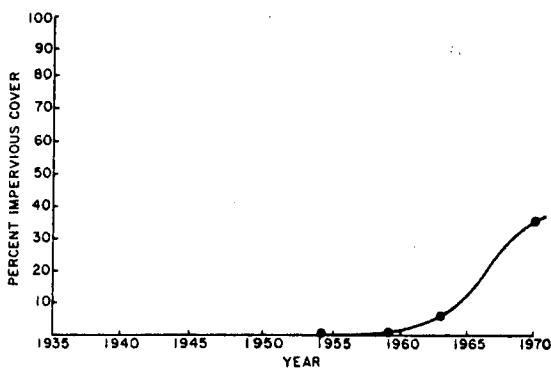
(d) topographic map

FIGURE 2. URBANIZATION OF FORT LOGAN WATERSHED, DENVER, COLORADO.
 This historical aerial photography sequence illustrates the rapid development of the Fort Logan watershed from 1959 to 1970. Scale 1/24,000. See Figure 3d for imperviousness development curve.

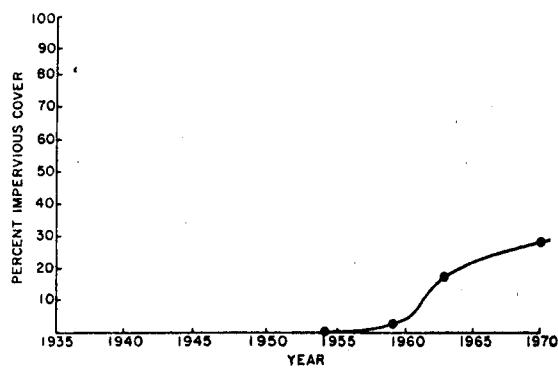
(a) FEDERAL HEIGHTS
1954-1970



(b) AURORA
1954-1970



(c) LITTLETON
1954-1970



(d) FORT LOGAN
1949-1970

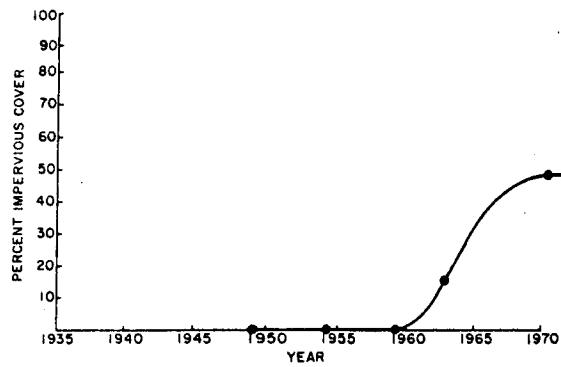
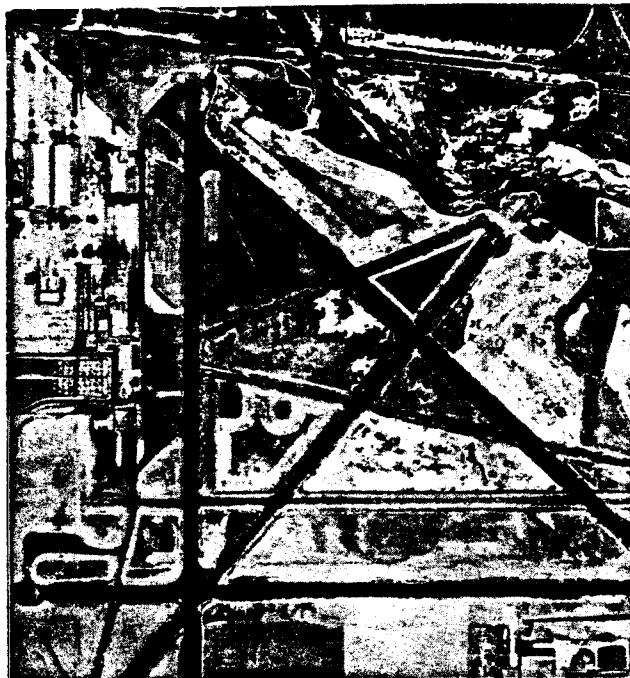
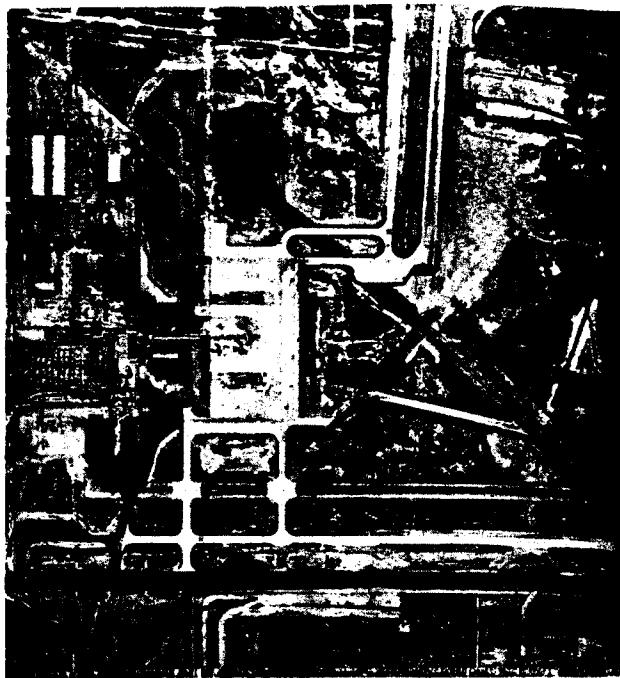


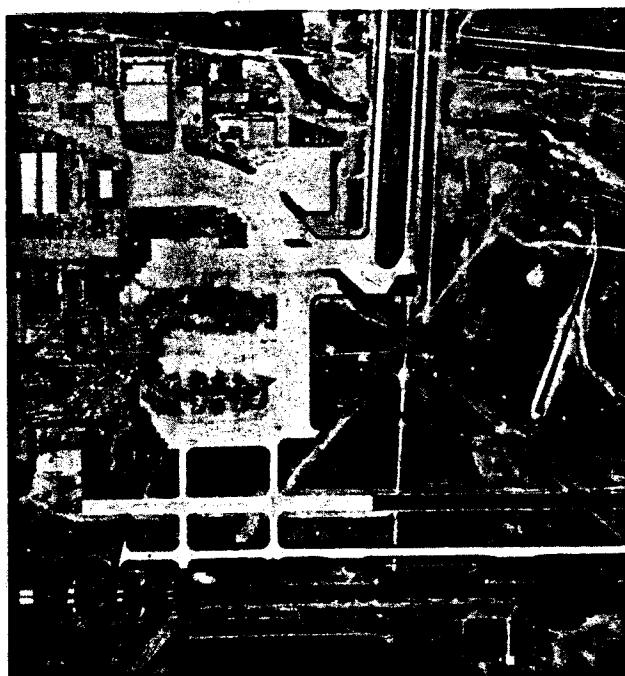
FIGURE 3. IMPERVIOUSNESS DEVELOPMENT CURVES FOR SEVERAL DENVER AREA WATERSHEDS. Percent of impervious material is plotted as a function of time in years. Figure 2 contains some of the historical photographs interpreted to form the curve for the Fort Logan watershed.



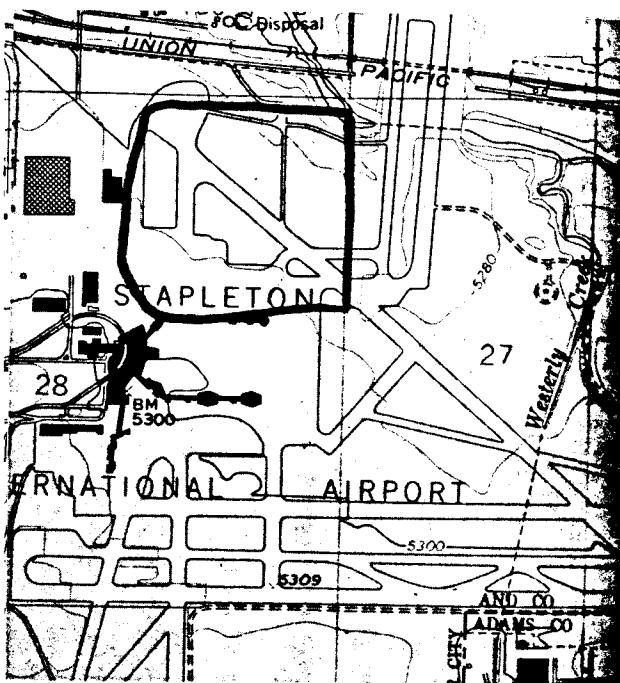
(a) 1959



(b) 1963



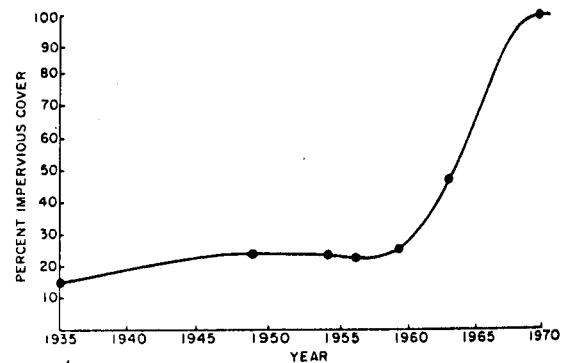
(c) 1970



(d) topographic map

FIGURE 4. URBANIZATION OF STAPLETON AIRPORT WATERSHED, DENVER, COLORADO. This historical aerial photography sequence illustrates the rapid development of the Stapleton Airport watershed from 1959 to 1970. Scale 1/24,000. See Figure 5a for development curve.

(a) STAPLETON AIRPORT
1936-1970



(b) STAPLETON-S
1950-1970

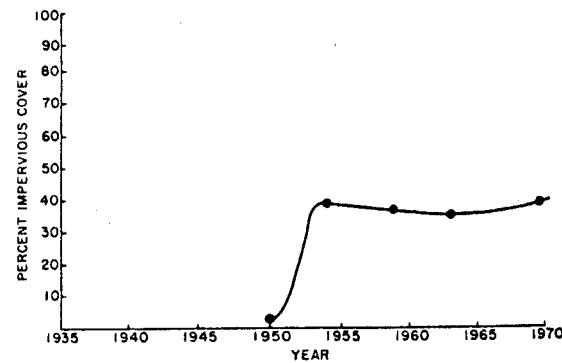


FIGURE 5. IMPERVIOUSNESS DEVELOPMENT CURVES FOR THE STAPLETON WATERSHEDS. Percent of impervious material is plotted as a function of time in years. Figure 4 contains some of the historical photographs interpreted to form the curve for the Stapleton Airport watershed.



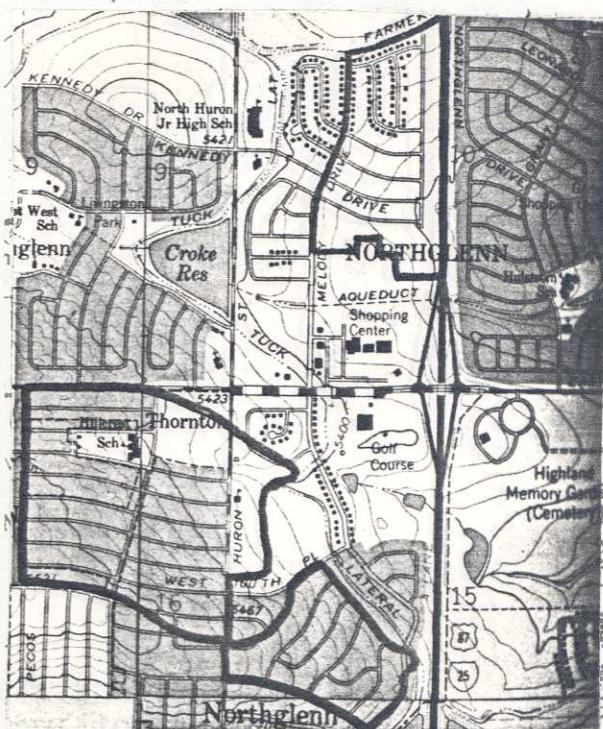
(a) 1959



(b) 1963



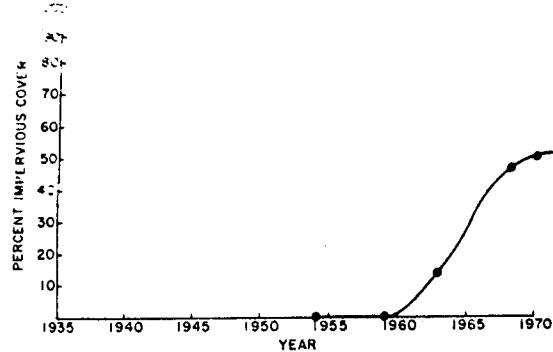
(c) 1968



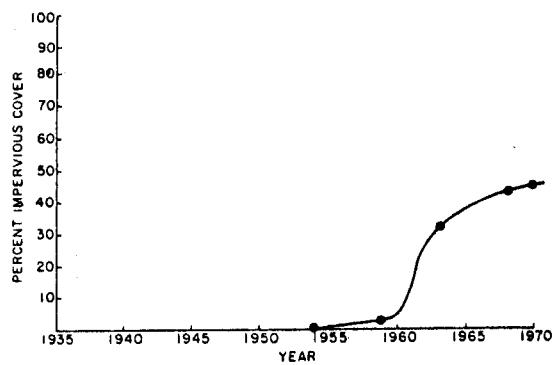
(d) topographic map

FIGURE 6. URBANIZATION OF THREE NORTGLENN WATERSHEDS, NORTH OF DENVER, COLORADO. This historical aerial photography sequence illustrates the rapid development of three watersheds in the Northglenn area from 1959 to 1968. Scale 1/20,000. See Figure 7 for development curves.

(a) NORTHGLENN
1954-1970
Basin 7201



(b) NORTHGLENN
1954-1970
Basin 7203



(c) NORTHGLENN
1954-1970
Basin 7204

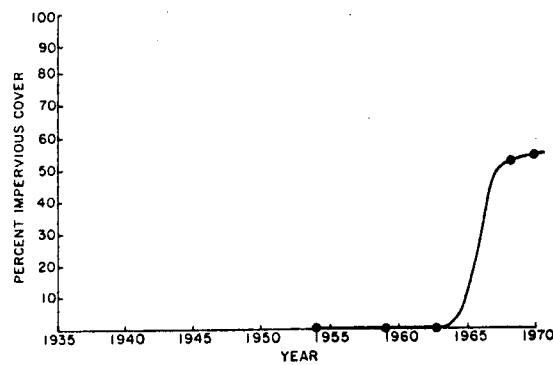


FIGURE 7. IMPERVIOUSNESS DEVELOPMENT CURVES FOR THE NORTHGLENN WATERSHEDS. Percent of impervious material is plotted as a function of time in years. Figure 6 contains some of the historical photographs interpreted to form these three curves.

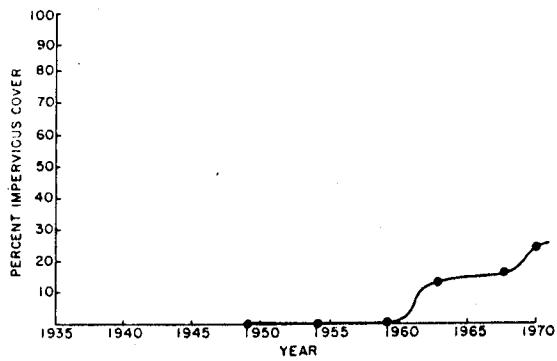
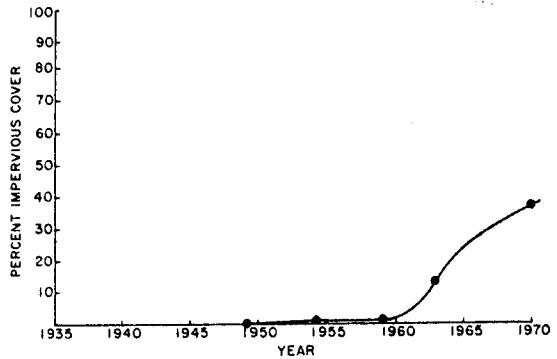
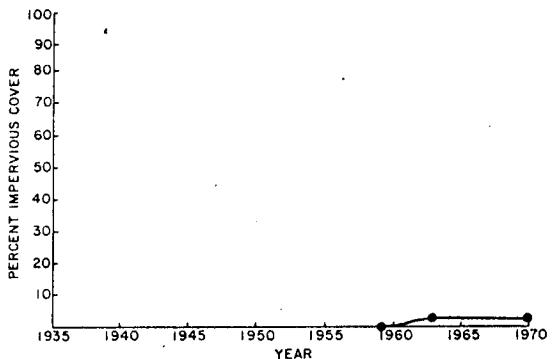
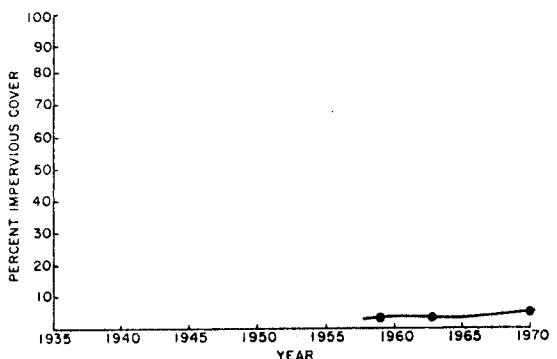
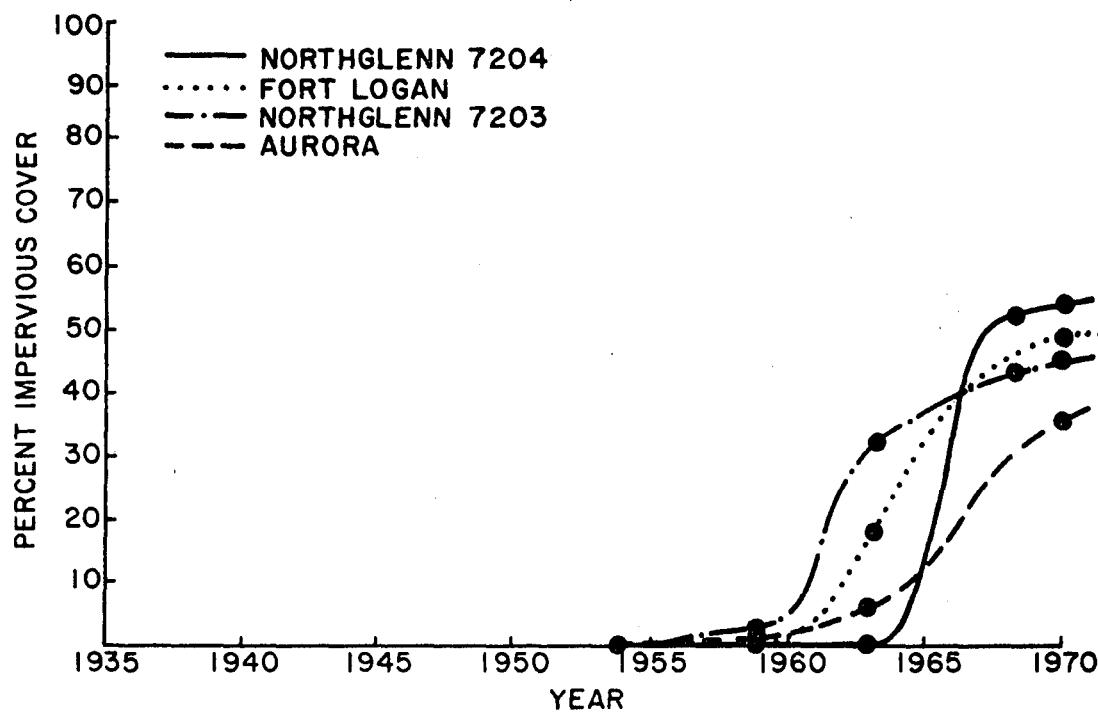
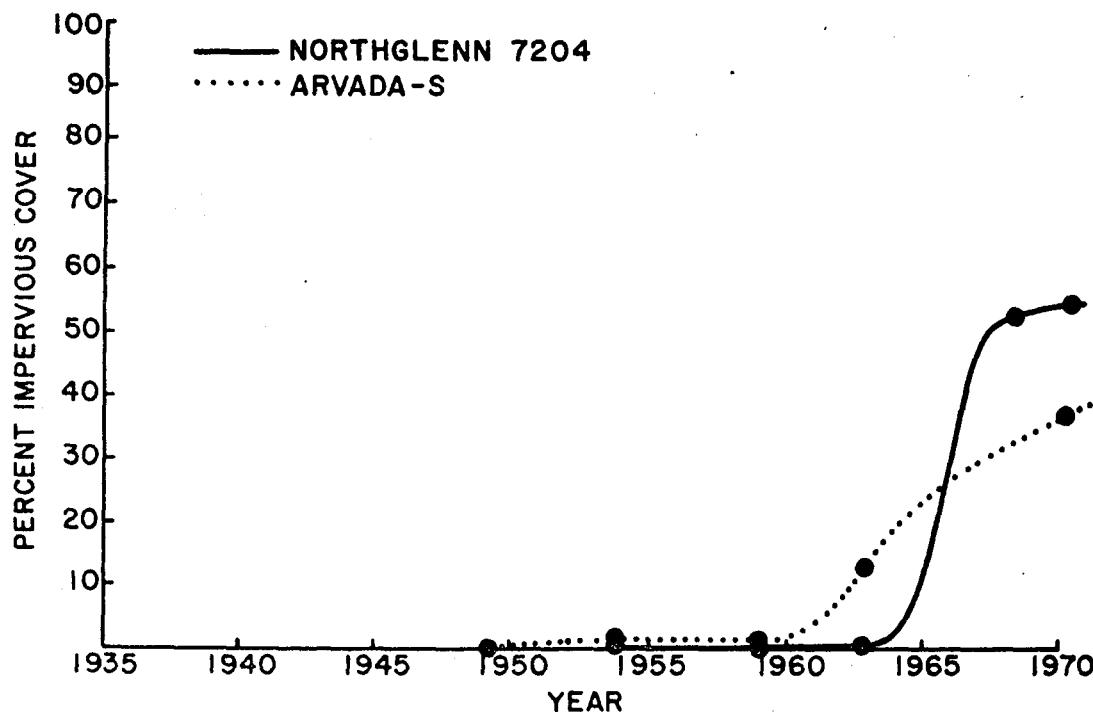
(a) ARVADA-N
1949-1970(b) ARVADA-S
1949-1970(c) HYATT LAKE-N
1959-1970(d) HYATT LAKE-S
1959-1970

FIGURE 8. IMPERVIOUSNESS DEVELOPMENT CURVES FOR SEVERAL DENVER AREA WATERSHEDS. Percent of impervious material is plotted as a function of time in years.

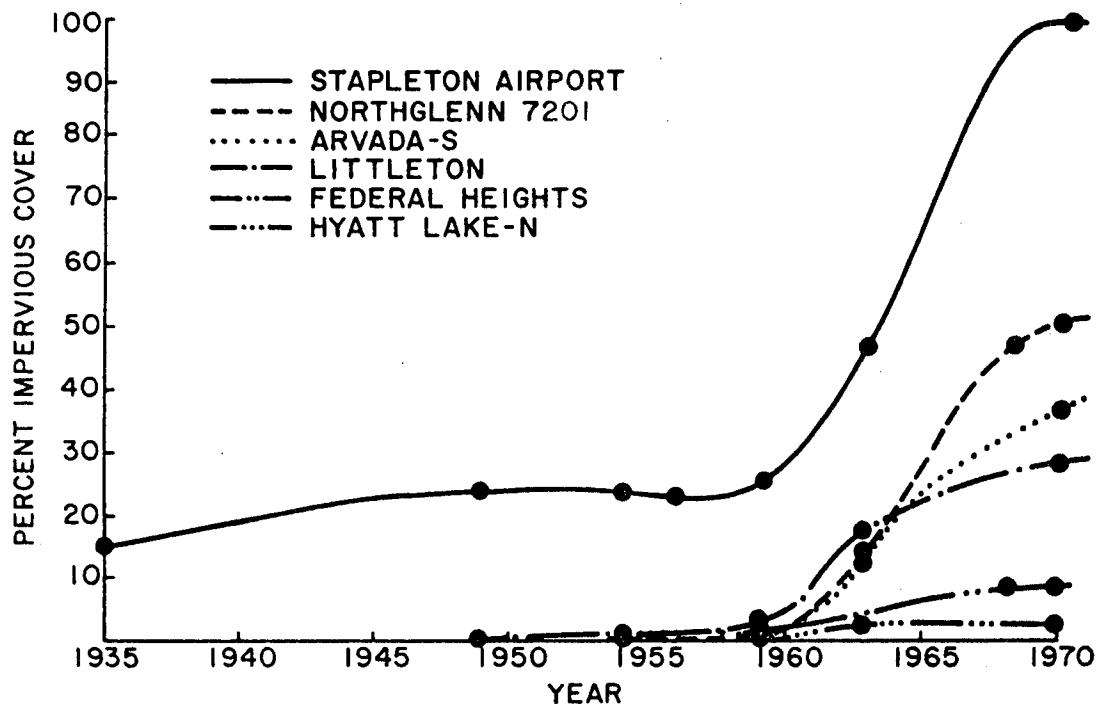


(a) different rates of urbanization

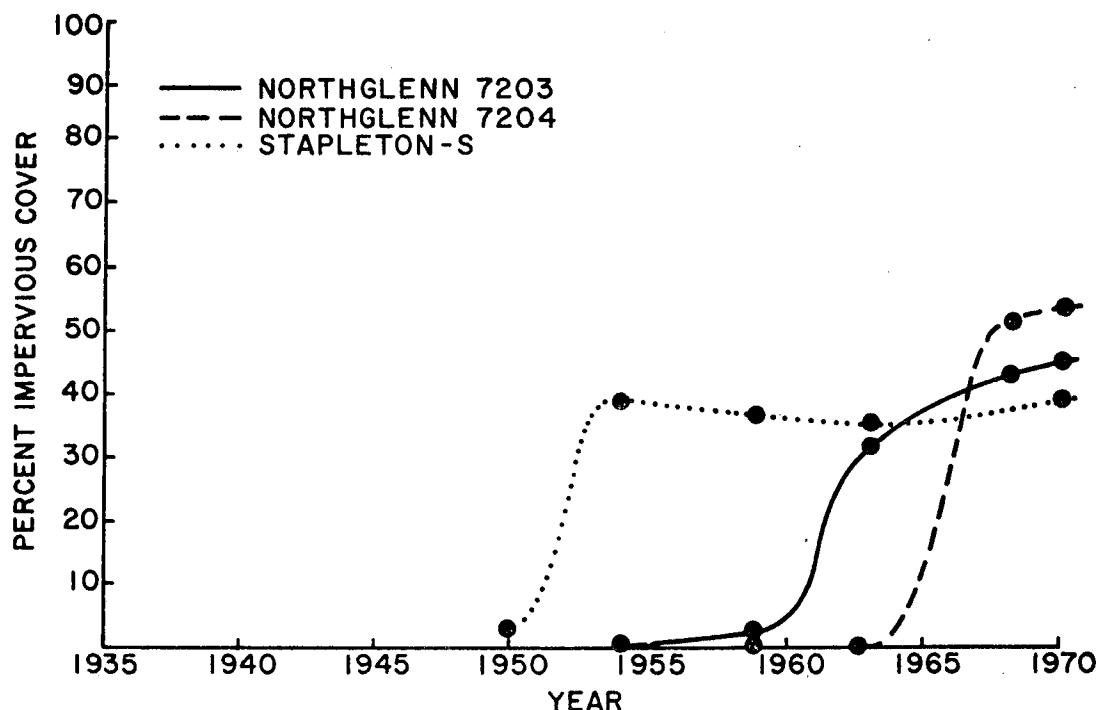


(b) rapid versus gradual urbanization

FIGURE 9. VARYING RATES OF DENVER URBANIZATION MEASURED BY PERCENT CHANGE IN IMPERVIOUS COVER. The individual imperviousness development curves used occur in Figures 3, 5, 7, and 8.



(a) different degrees of urbanization



(b) rapid urbanization beginning at different dates

FIGURE 10. VARYING DEGREES AND TIMES OF DENVER URBANIZATION MEASURED BY PERCENT CHANGE IN IMPERVIOUS COVER. The individual imperviousness development curves used occur in Figures 3, 5, 7, and 8.

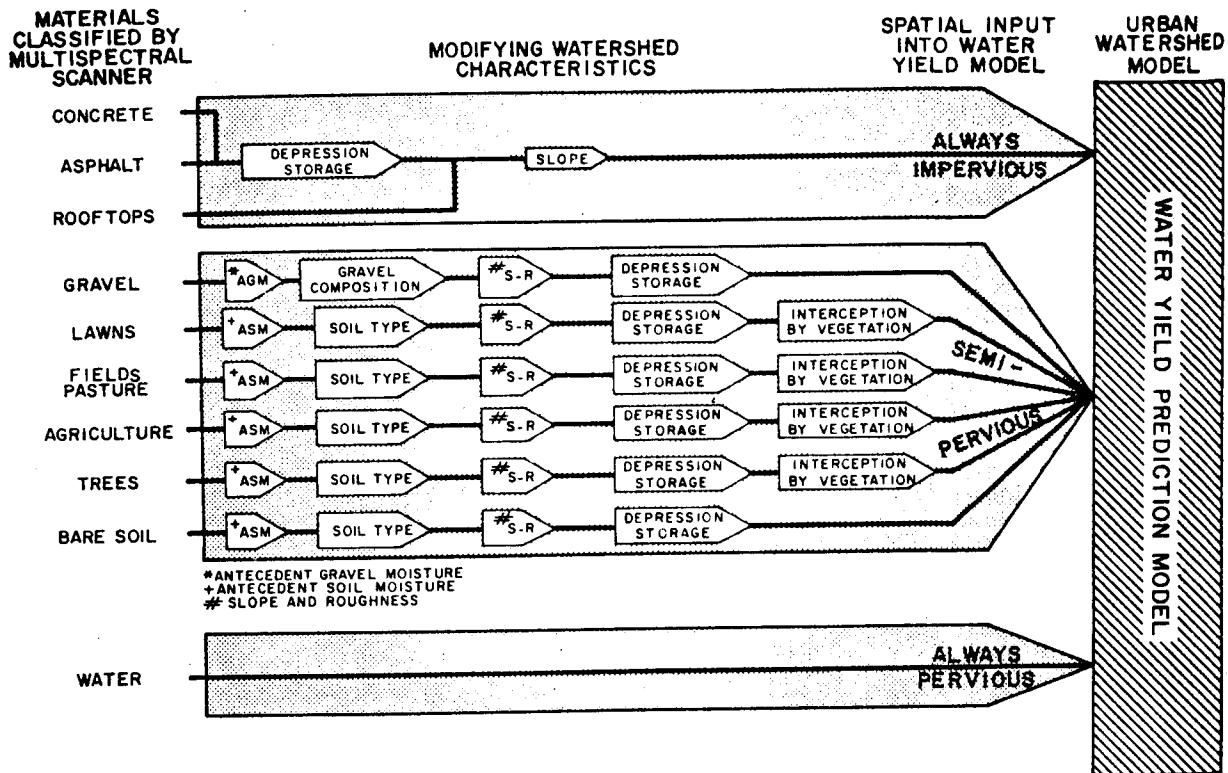
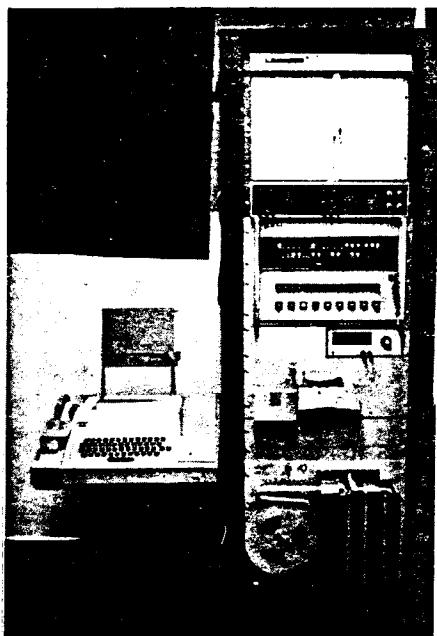
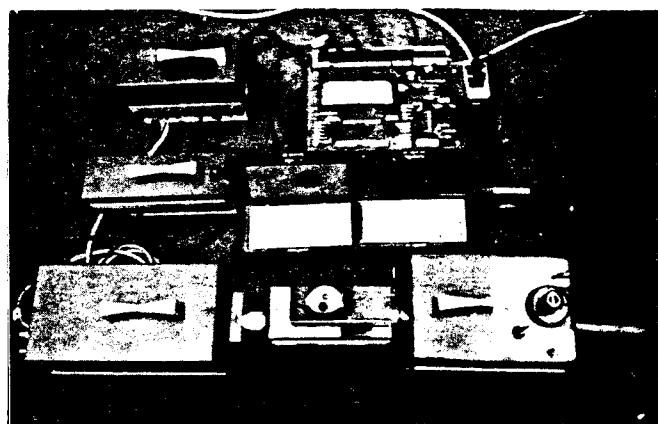


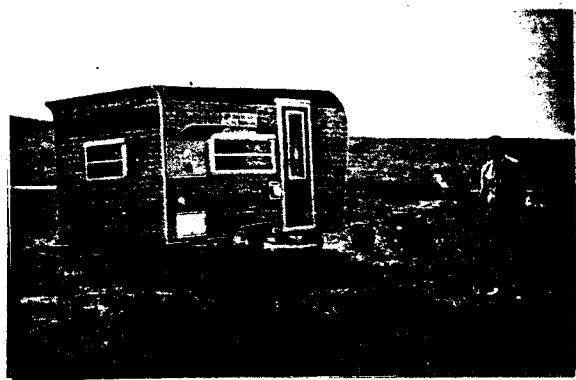
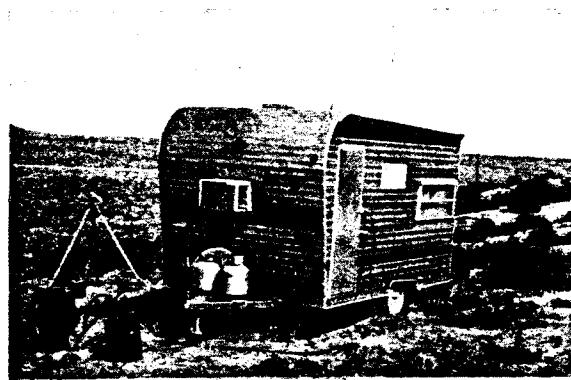
FIGURE 11. "MAPPING" THE CLASSIFICATION OF SURFACE MATERIALS INTO UNITS OF SURFACE HYDROLOGY BY REMOTE MULTISPECTRAL SENSING. Each hydrologic unit must be refined by the hydrologic characteristics of each of the contributing remote sensing units, such as antecedent soil moisture, soil type (e.g., porosity, permeability, etc.), depression storage, slope and roughness, and interception by vegetation, before being input into the watershed model.



(a) computer digital data acquisition system



(b) spectroradiometer modules



(c) field trailer configuration

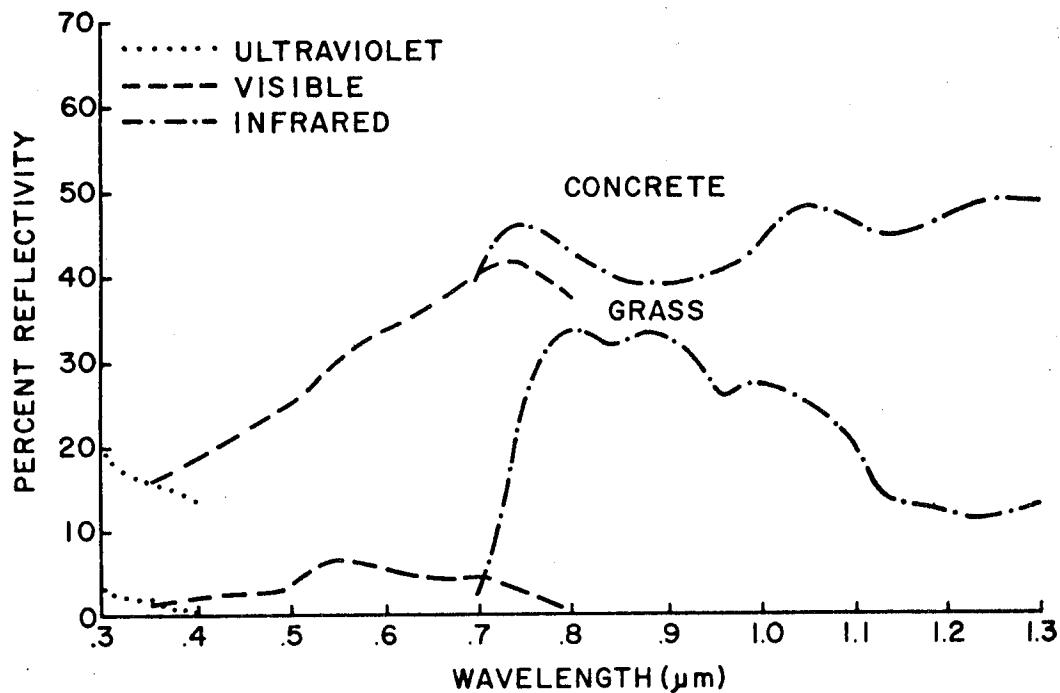
FIGURE 12. FIELD SPECTROMETER SYSTEM. This system was used in the field measurement of all spectroreflectance curves. (a) Computerized digital data acquisition system shown in the rack used for indoor laboratory operations during the winter months. (b) Composite view of the EG&G model 580-585 spectroradiometer showing all available hardware used in the laboratory. (c) Field trailer housing the spectroradiometer, computer system, and ancillary equipment as they are being used for 'in situ' collection of spectroradiance and spectroreflectance measurements. Note generator used for field power. Note also the small tripod mounted, first surfaced mirror used for folding the horizontal view of the spectroradiometer pointed out the side of the trailer down normal to the ground surface. Larger 75 by 100 cm mirrors are also used to measure quarter square meter ground patches. (Courtesy Pearson and Miller, 1971)

FIGURE 12a. DESCRIPTION EXPANDED. The Hewlett-Packard minicomputer data system consists of:

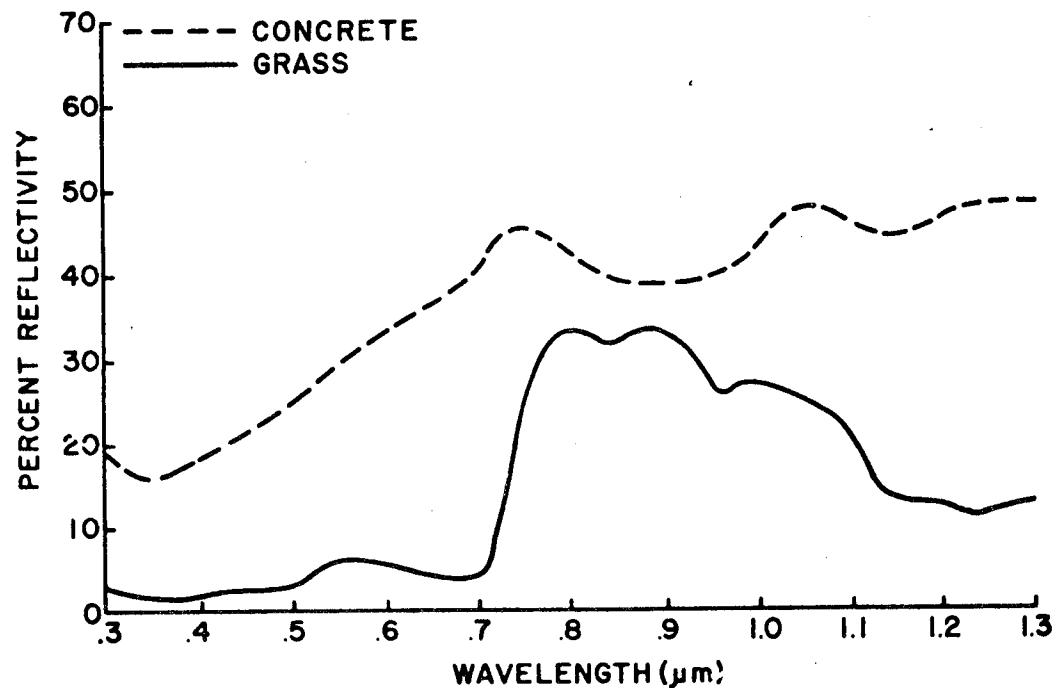
1. an analog x-y plotter, interfaced to the computer through a digital to analog converter card, and used to plot the spectral curves as they are reduced on line by the computer (top of rack);
2. a model 2114A digital computer (middle of rack);
3. a digital multimeter for system maintenance and testing (below computer);
4. a high speed (300 eight-bit characters per second) punched paper tape reader used primarily for program input to the computer (lower middle of rack);
5. a low level analog to digital converter for conversion of input analog signals from the spectroradiometer and other sensors (just below the paper tape reader);
6. a high speed (120 eight-bit characters per second) paper tape punch for data output (bottom of rack);
7. a multiplexer for selecting under program control the analog input channel to be digitized (below paper tape punch); and
8. a model ASR-33 teletype for keyboard input and printed output from the computer (left).

FIGURE 12b. DESCRIPTION EXPANDED. The spectroradiometer system is composed of the following modular subsystems:

1. a reflective telescope for viewing the sample (lower right);
2. a monochromator housing which accepts one of three gratings used to select the wavelength being sampled (lower center and middle);
3. a high sensitivity, near infrared detector head (lower left) and a separate power supply and cooling controller (upper left);
4. a high sensitivity, ultraviolet-visible detector head (middle left);
5. an indicator unit through which the radiant intensity signal is amplified (upper middle); and
6. a one-meter fiber optics probe which replaces the telescope (upper left).



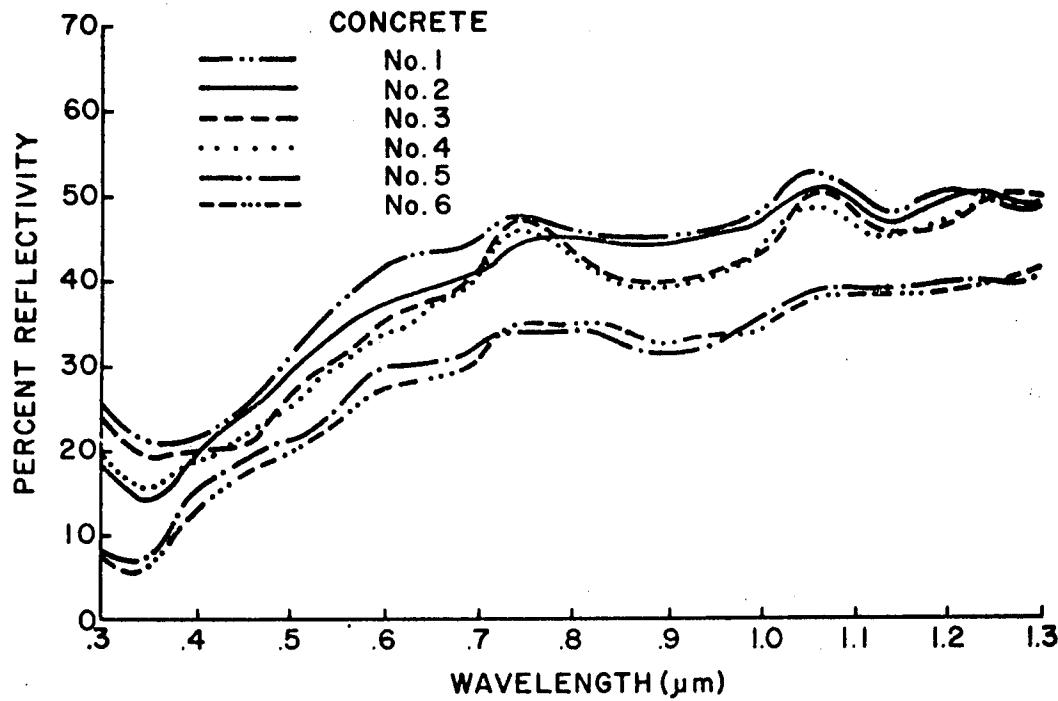
(a) "raw" spectroreflectance curves



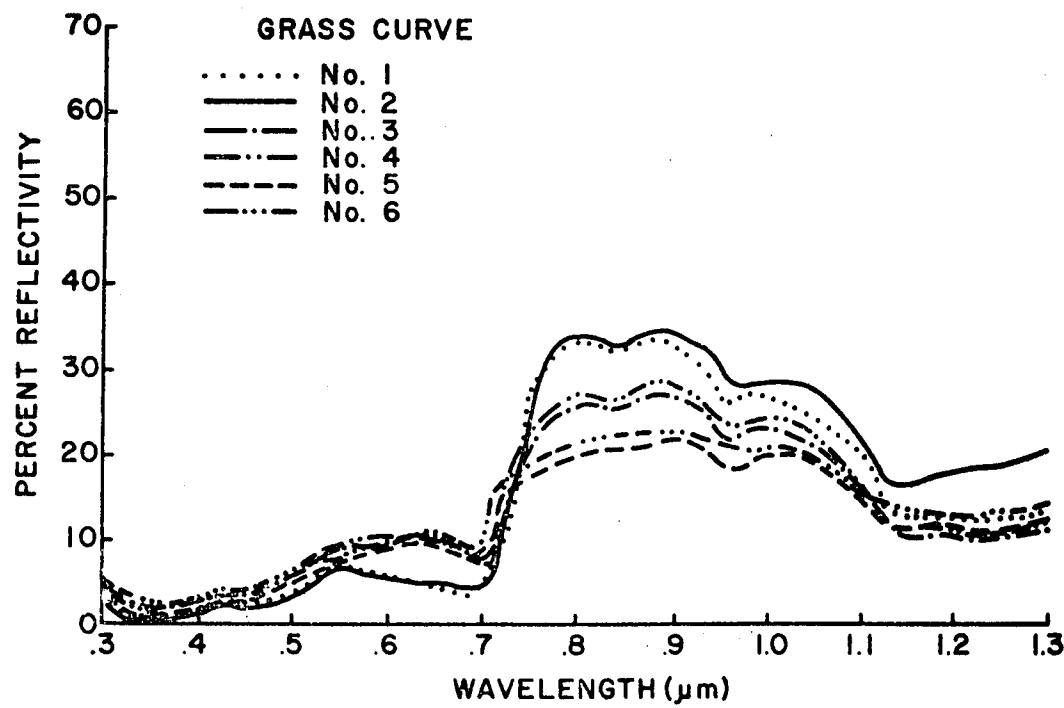
(b) "JOINED" spectroreflectance curves

FIGURE 13. SAMPLE SPECTROREFLECTANCE CURVES OF GRASS AND CONCRETE.

(a) The spectroreflectance is measured normal to the plane of the material in three segments - ultraviolet, visible, and photo infrared by various detector-grating combinations. (b) The three segments of the raw data curves are formed into a contiguous curve and replotted using a FORTRAN program JOIN (Appendices E and F).



(a) 1&2 = fresh concrete, 3&4 = intermediate, 5&6 = dirty concrete



(b) 1&2 = lush green lawn, 3&4 = intermediate, 5&6 = dried lawn

FIGURE 14. REPLICATED SPECTROREFLECTANCE CURVES FOR GRASS AND CONCRETE. Six curves are shown for each material representing two measurements on each of three samples. The three samples represent the natural variability in each material and the two replicate runs measured at different positions on each sample represent its variability.

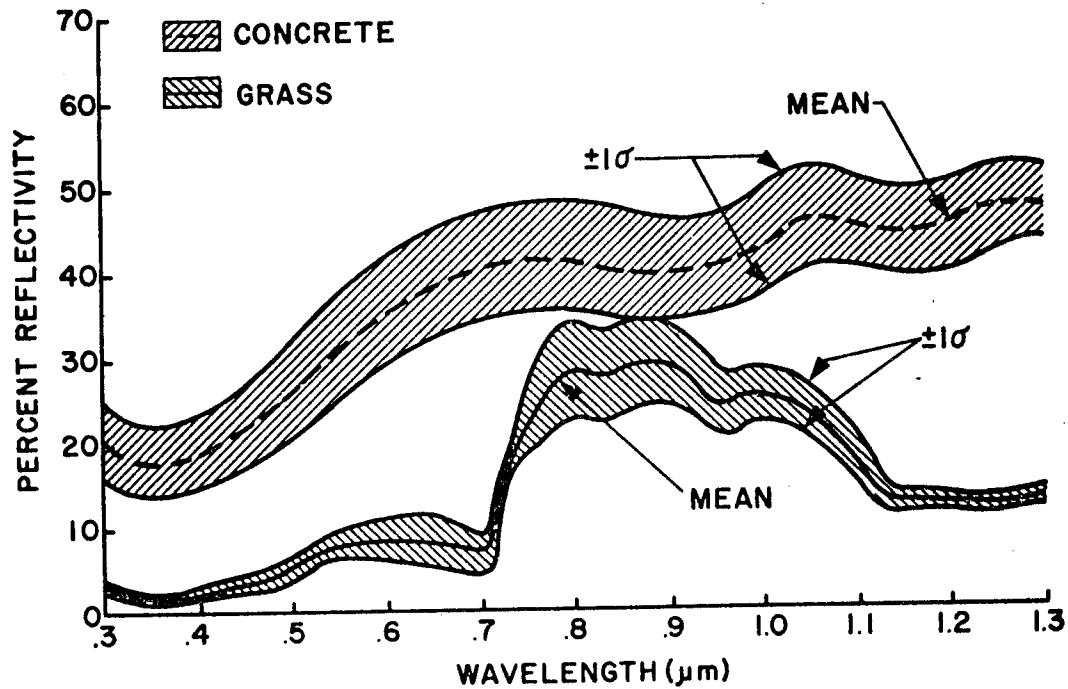


FIGURE 15. MEAN SPECTROREFLECTANCE AND STANDARD DEVIATION FOR GRASS AND CONCRETE. The six curves for each material shown in Figures 14a and b are combined and plotted in the field trailer by the FORTRAN program AVER (Appendices E and F).

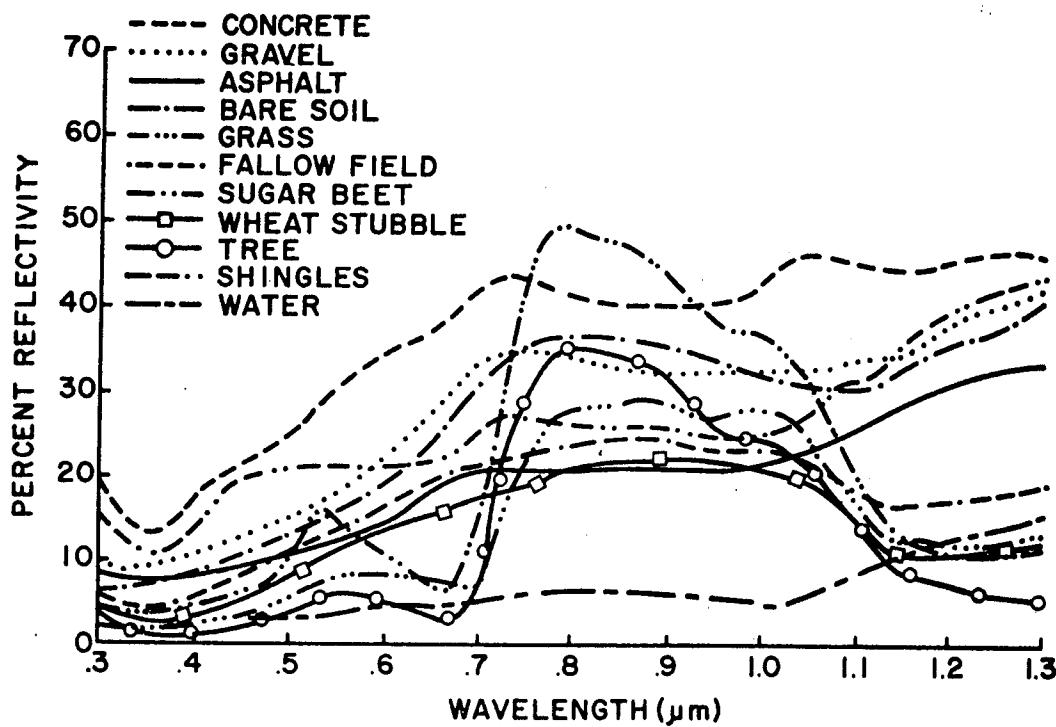
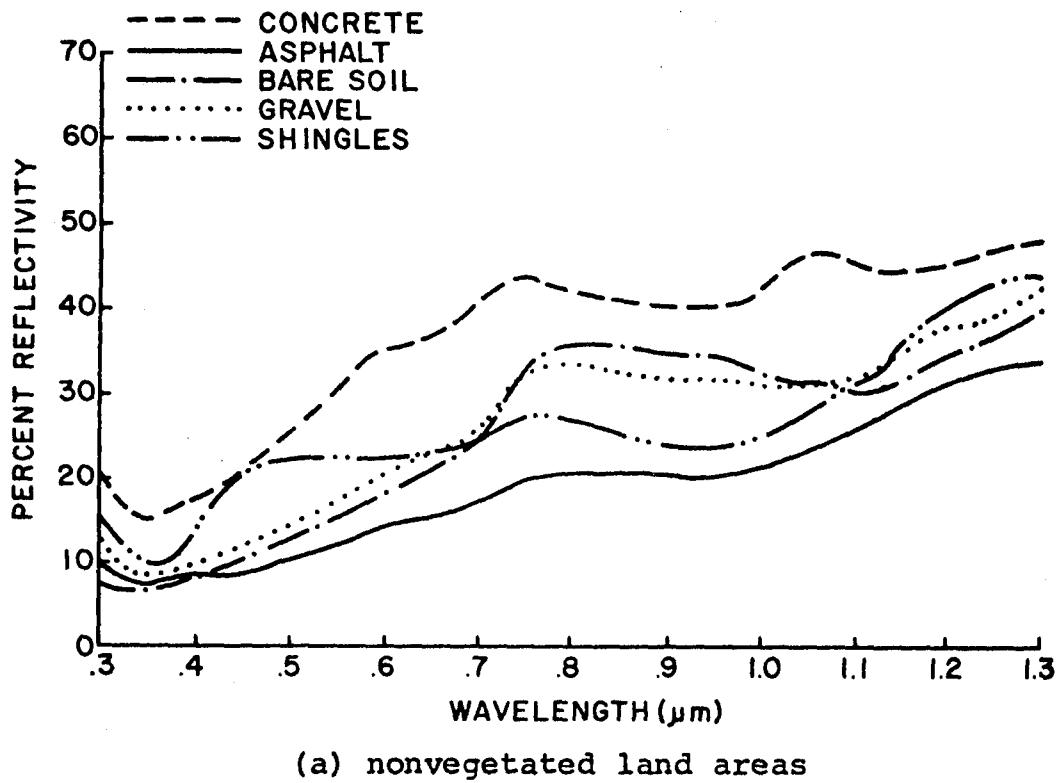
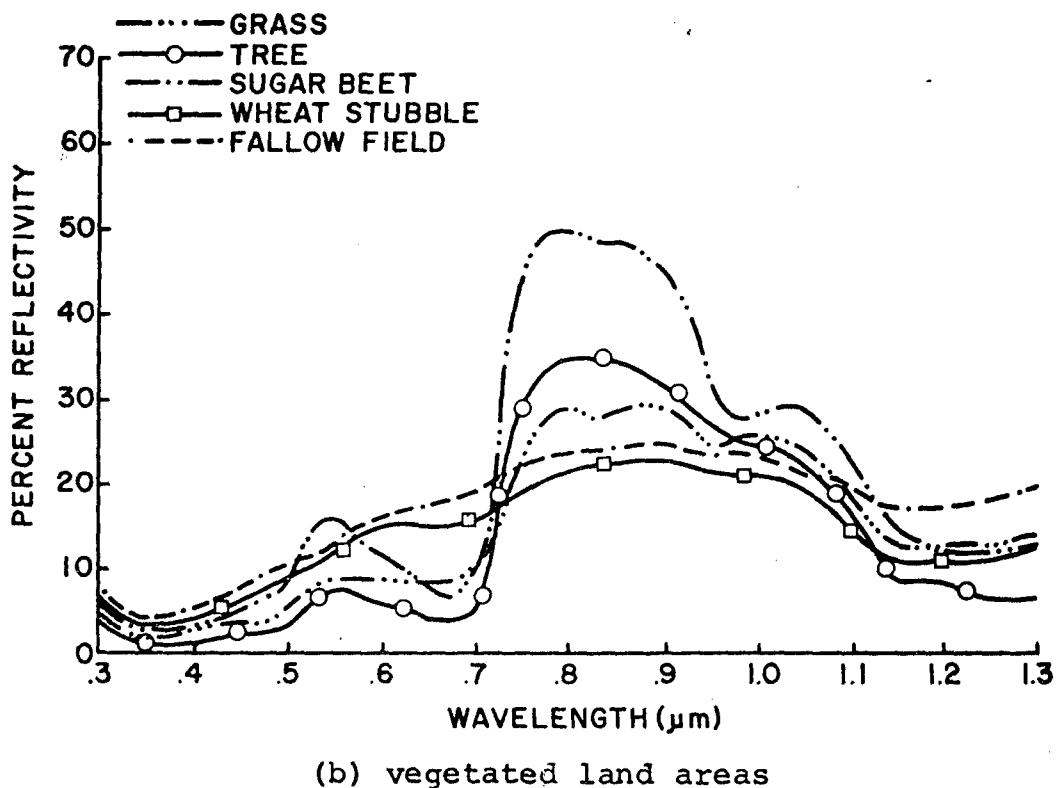


FIGURE 16. MEAN SPECTROREFLECTANCE CURVES FOR ELEVEN SURFACE MATERIAL CATEGORIES IN AN URBANIZING WATERSHED. These mean curves were formed from six complete spectroreflectance curves for each of the materials in the same fashion as illustrated in Figures 13 to 15. The surface material "agriculture" is here represented by green sugar beets and wheat stubble, which constitute the primary agricultural land use around Denver at this time of year. Each of the eleven units constituted an area of greater than .5% in a typical Denver watershed in midsummer.

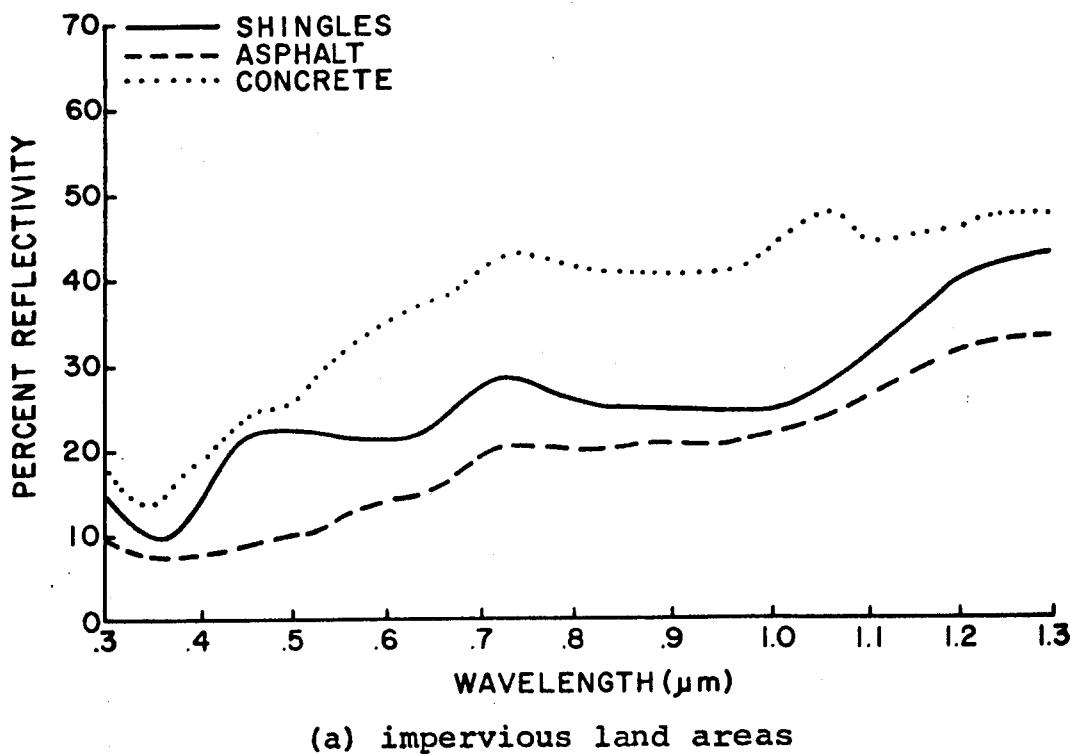


(a) nonvegetated land areas

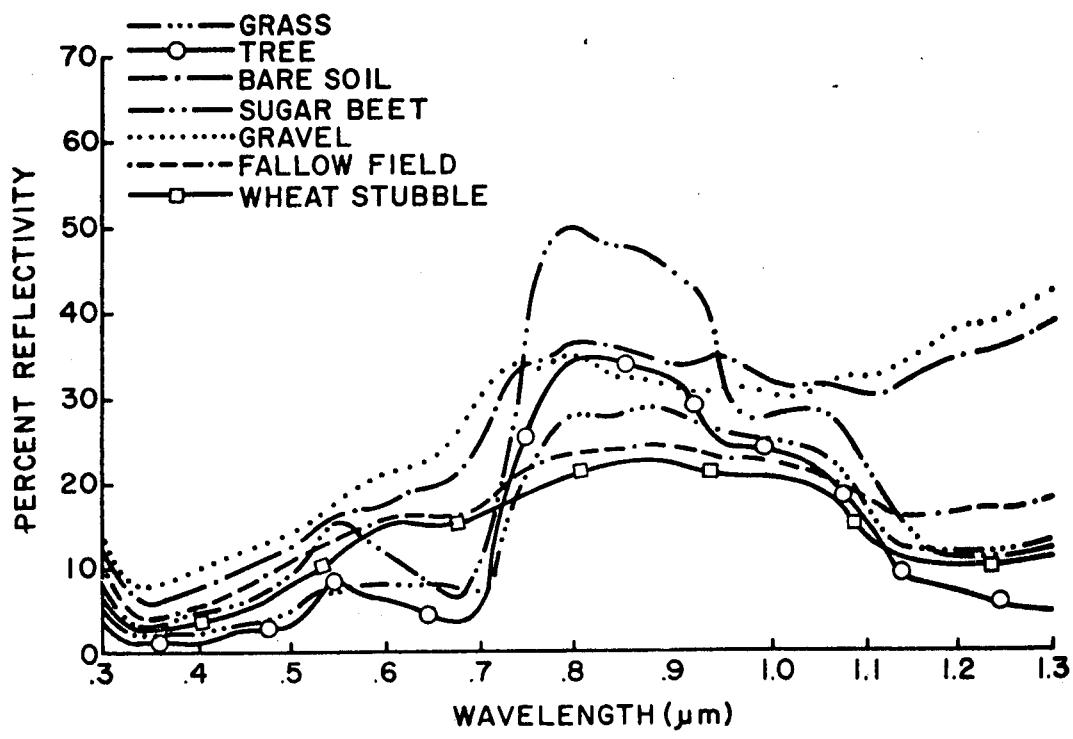


(b) vegetated land areas

FIGURE 17. COMPARISON OF MEAN SPECTROREFLECTANCE CURVES FOR NON-VEGETATED AND VEGETATED URBAN UNITS. This division of the curves is similar to that shown by the University of Michigan in Figure 1. Note that a division of the urban watershed into these two classes could easily be made at 1.2 μm .



(a) impervious land areas



(b) pervious land areas

FIGURE 18. COMPARISON OF MEAN SPECTROREFLECTANCE CURVES FOR IMPERVIOUS AND PERVERIOUS URBAN UNITS. This division of the curves illustrates the basic hydrologic classification of an urban watershed. Note that bare soil and gravel which could be properly classified as nonvegetation in Figure 17 at 1.2 μm would be confused with impervious materials in this example.

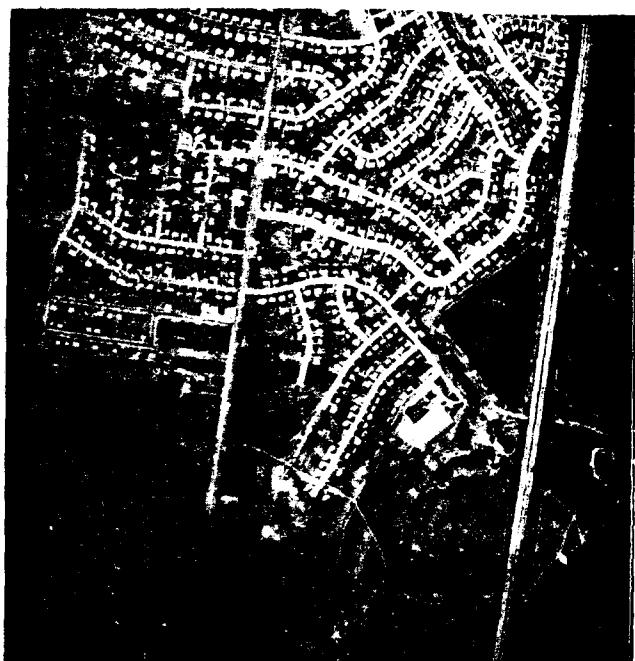
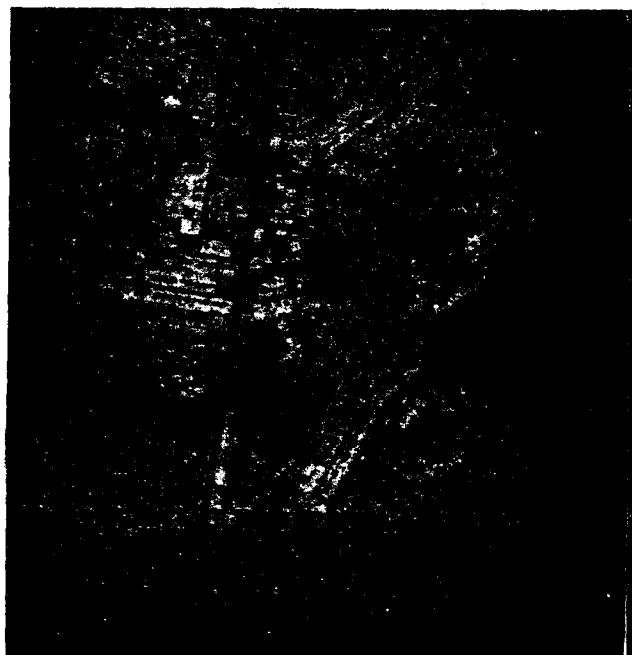
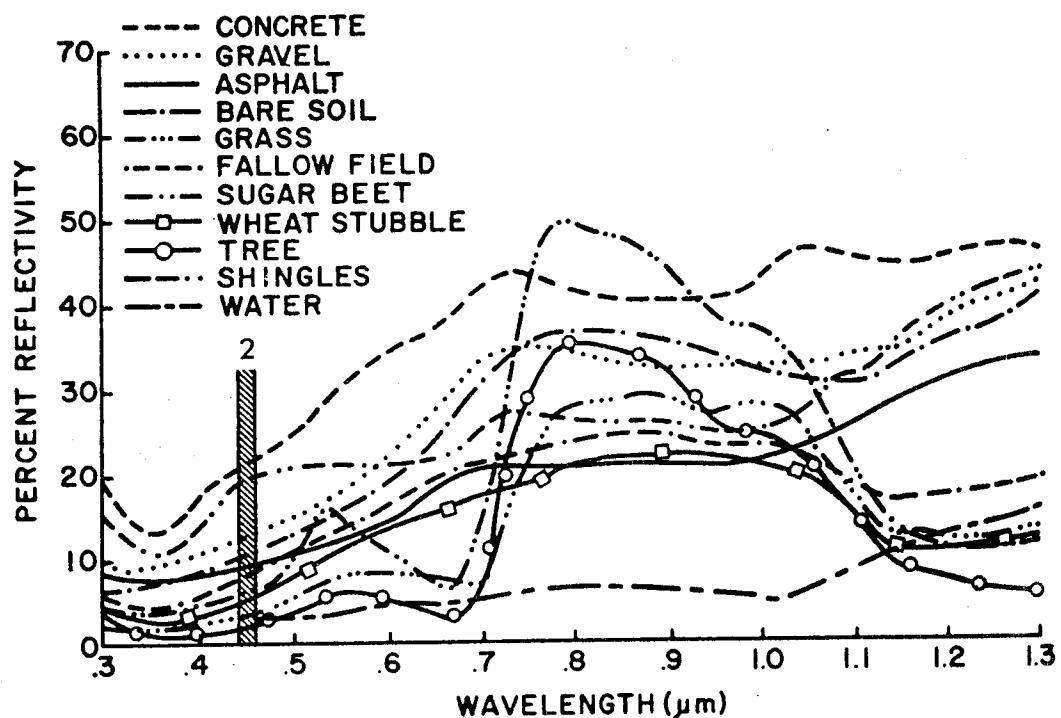
(a) blue band (.4-.5 μm)(b) green band (.5-.6 μm)(c) red band (.6-.7 μm)(d) photo infrared band (.7-.9 μm)

FIGURE 19. MULTIBAND AERIAL PHOTOGRAPHS OF THE NORTHGLENN-7201 WATER-SHED. Flown by Civil Engineering Department, Colorado State University on 28 April 1971 with an I'S multiband camera. Scale approximately 1/30,000. Figure 20 contains a selective color combination of these photographs.

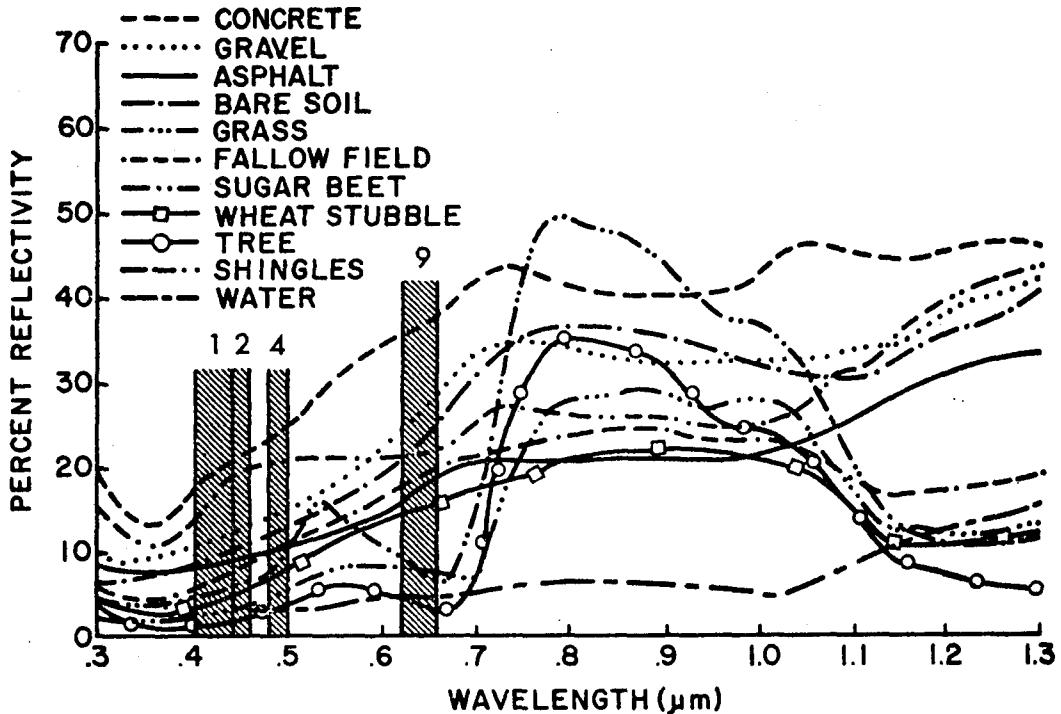


FIGURE 20. COLOR COMBINED BLACK AND WHITE MULTIBAND PHOTOGRAPHS (Fig. 19). Flown in the spring on 28 April 1971 at a scale of approximately 1/14,000. Impervious materials appear pink with the exception of some fallow fields, while pervious areas are blue. A check of this classification can be made with the frontpiece which contains this same area. The individual photographs used occur in Figure 19. In superimposing in color the red image (Fig. 19c) was coded red while the photo infrared (Fig. 19d) was coded blue.



Band Combination	Maximum Euclidean Distance	Band Combination	Minimum Euclidean Distance	Band Combination	Average Euclidean Distance
2	14.812	2	.245	2	3.511
3	14.324	10	.124	1	3.202
9	14.038	11	.107	3	3.081
4	12.982	7	.081	4	2.948
1	12.915	1	.052	9	2.627
8	10.475	2	.039	5	2.602
5	9.477	9	.036	10	2.548
7	8.345	12	.032	8	2.393
10	7.231	3	.030	7	2.381
6	6.876	6	.016	6	2.314
11	6.159	5	.006	12	1.793
12	4.778	8	.002	11	1.482

FIGURE 21. OPTIMIZED SINGLE SPECTRAL BAND FOR URBAN MAPPING. The .44-.46 μm spectral band (no. 2) is highest in all three qualifying statistics denoting the separation of the eleven materials shown with their mean curves. The spectral interval of each of the twelve bands tested can be found in Table 4.



Band Combination	Maximum Euclidean Distance	Band Combination	Minimum Euclidean Distance	Band Combination	Average Euclidean Distance
2,3,4,9	28.110	1,6,7,12	.957	1,2,3,4	6.430
1,2,3,9	28.079	1,5,11,12	.957	1,2,3,9	6.390
1,2,3,4	27.566	1,7,8,12	.948	1,2,3,10	6.367
1,2,4,9	27.419	1,6,8,12	.946	1,2,3,5	6.324
1,3,4,9	27.158	1,4,6,12	.945	1,2,4,9	6.331
2,3,8,9	27.044	1,5,6,12	.937	1,2,4,10	6.304
2,3,5,9	26.673	1,4,8,12	.936	1,2,4,5	6.257
2,3,4,8	26.511	1,4,7,12	.932	1,2,3,8	6.256
1,2,3,8	26.478	1,5,8,12	.928	1,2,3,6	6.240
2,4,8,9	26.358	1,5,7,12	.924	1,2,3,7	6.231
.
.
6,7,11,12	11.191	1,2,3,4	.300	7,8,11,12	4.412
7,10,11,12	11.159	7,8,9,11	.291	6,8,11,12	4.378
6,10,11,12	10.901	7,9,11,12	.280	6,7,11,12	4.351

FIGURE 22. OPTIMIZED FOUR SPECTRAL BANDS FOR URBAN MAPPING. The .40-.44 μm , .44-.46 μm , .48-.50 μm , and .62-.68 μm spectral bands (nos. 1, 2, 4, and 9) are consistently high in the three qualifying statistics denoting the separation of the eleven materials shown with their mean curves. This solution neglects curve crossovers and the redundancy of adjacent bands. The spectral interval of each of the twelve bands tested can be found in Table 4.

APPENDIX A: ABRIDGED BIBLIOGRAPHY ON THE IMPACT
OF REMOTE SENSING ON URBAN WATERSHED ANALYSIS

The articles in the bibliography have been selected from 7000 in the RESENA (REmote SEnsing of NATURE) library, Department of Watershed Sciences, Colorado State University. This list of references relates selected articles and reports dealing with urban hydrology and watershed modeling to those dealing with the capabilities of remote sensing of urban areas. The bibliography is divided into six sections.

- I. GENERAL HYDROLOGY covering a wide variety of topics in hydrology of possible use in urban watershed studies.
- II. URBAN HYDROLOGY dealing specifically with hydrology studies related to urban areas.
- III. GENERAL WATERSHED MODELING including varying types of watershed models over a variety of types of watersheds.
- IV. URBAN WATERSHED MODELING specifically dealing with modeling of urban watersheds.
- V. REMOTE SENSING: GENERAL SOURCES dealing with potentialities and problems of remote sensors and imagery analysis.
- VI. REMOTE SENSING: URBAN ENVIRONMENT specifically describes the use of remote sensors for evaluating the surface characteristics of urban areas.

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APPENDIX B: 13 STUDY WATERSHEDS, DENVER, COLORADO

The 13 watersheds analyzed in this study are located in and about the suburbs of Denver, Colorado (Fig. B-1). These watersheds were chosen for study from those being modeled by the USGS, Water Resources Division because of their varying degrees of urbanization, from undeveloped to completely developed. For a more detailed look at the watersheds, a USGS topographic map at 1/24,000 and an airphoto at 1/27,500 (May, 1970) are provided (Figs. B-2 to B-9) showing the detailed distribution of topography and surface features of the watersheds and for the areas immediately surrounding them. Watershed boundaries are marked as heavy black lines on both the maps and aerial photos. Inspection of these maps and photographs reveals the range of urbanization of the 13 study watersheds in the variation of impervious cover in the form of rooftops, streets, and parking lots.

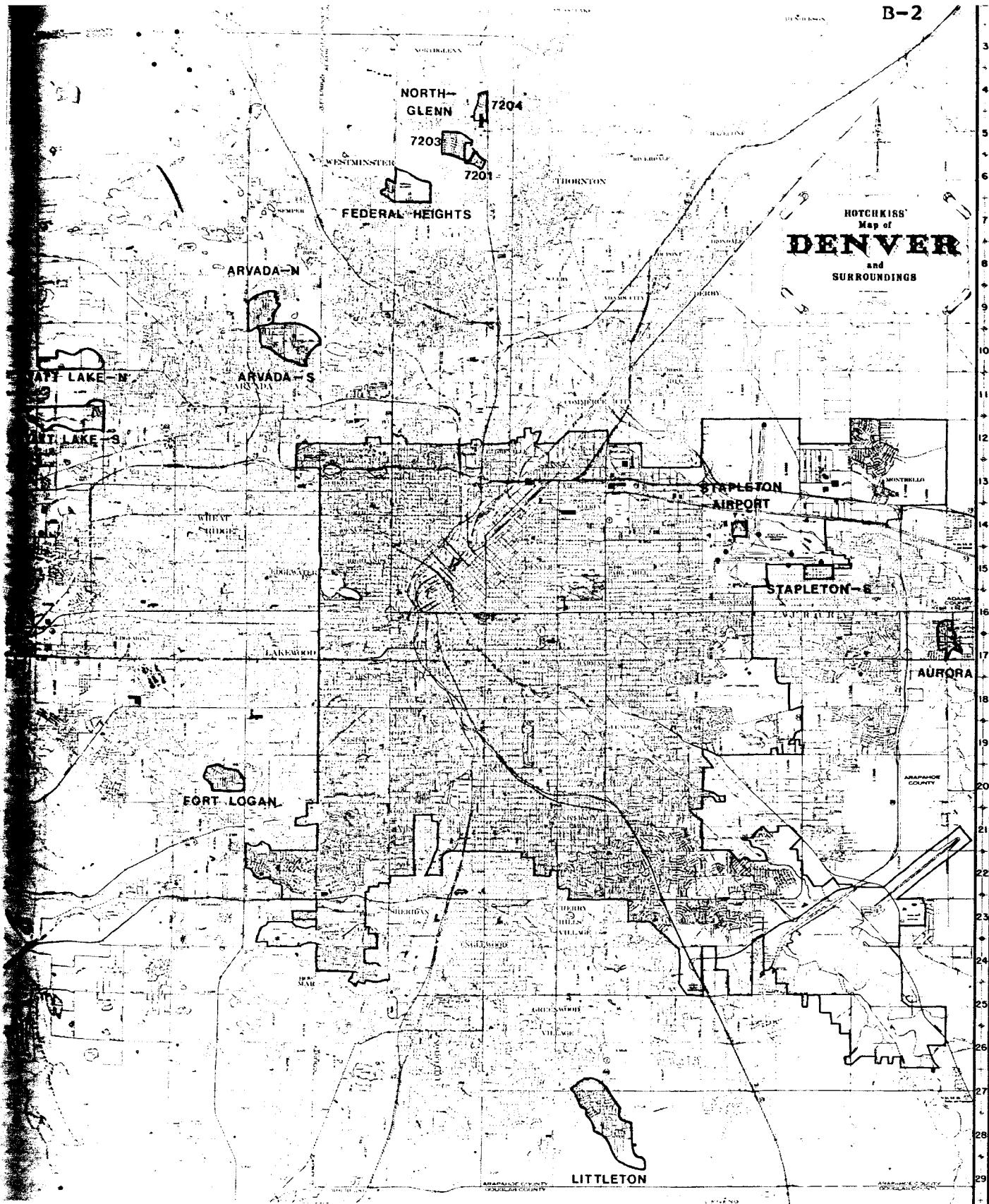
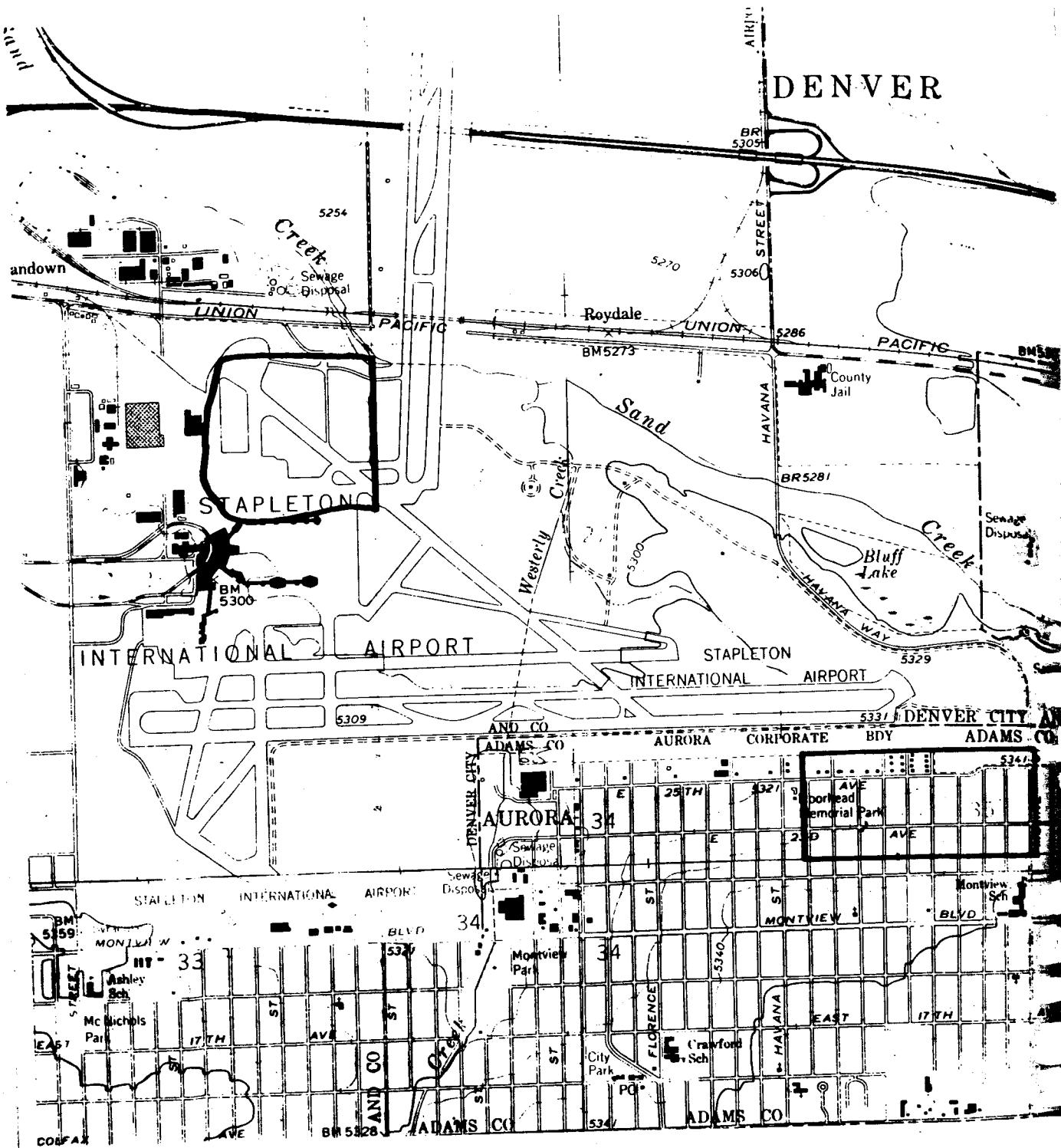


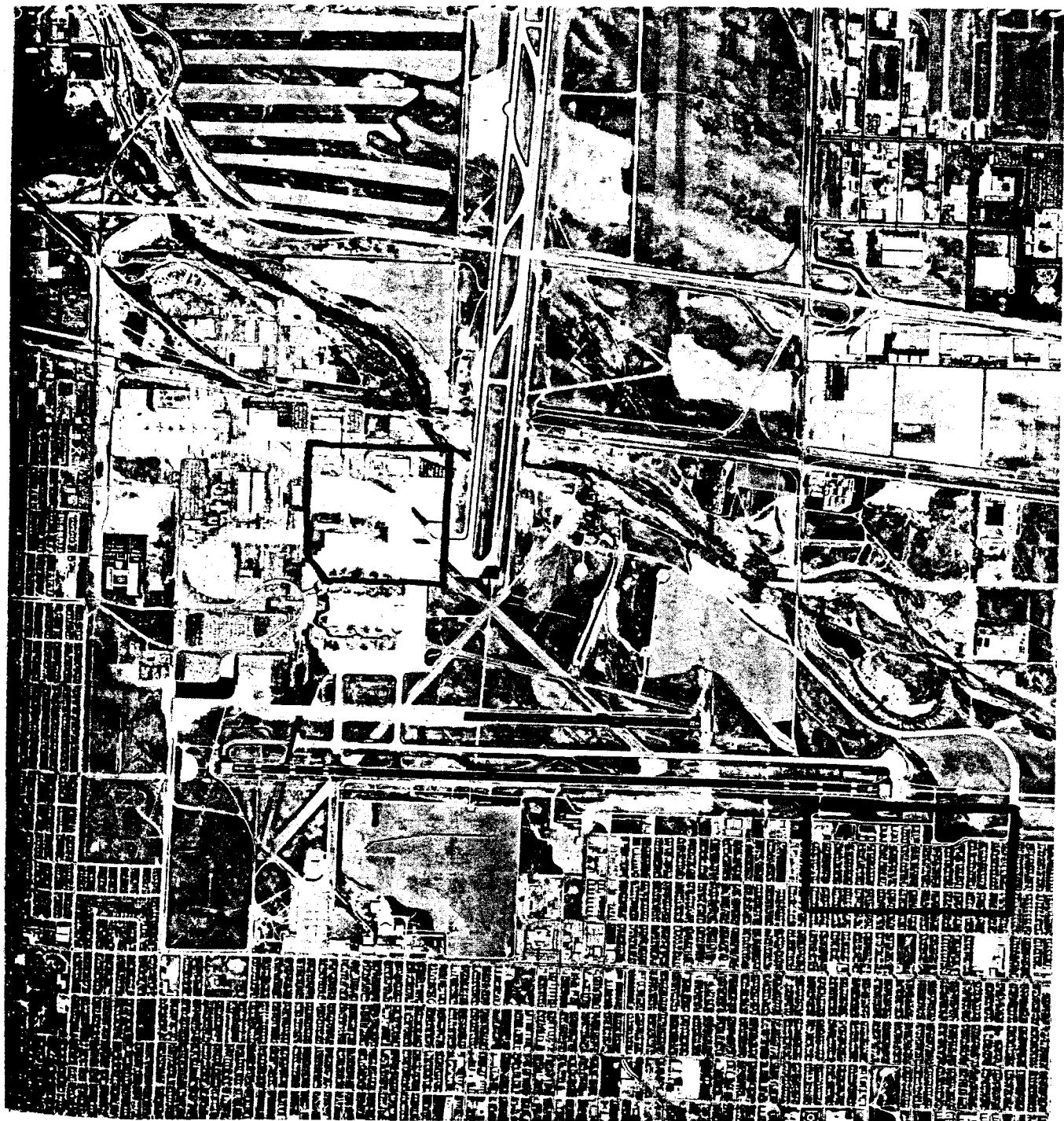
FIGURE B-1. MASTER INDEX MAP TO 13 DENVER AREA URBAN WATERSHEDS.

This map shows the location of 13 watersheds used in this study. These watersheds were selected from 30 under study by the USGS - Water Resources Division for the effects of urbanization on water yield.

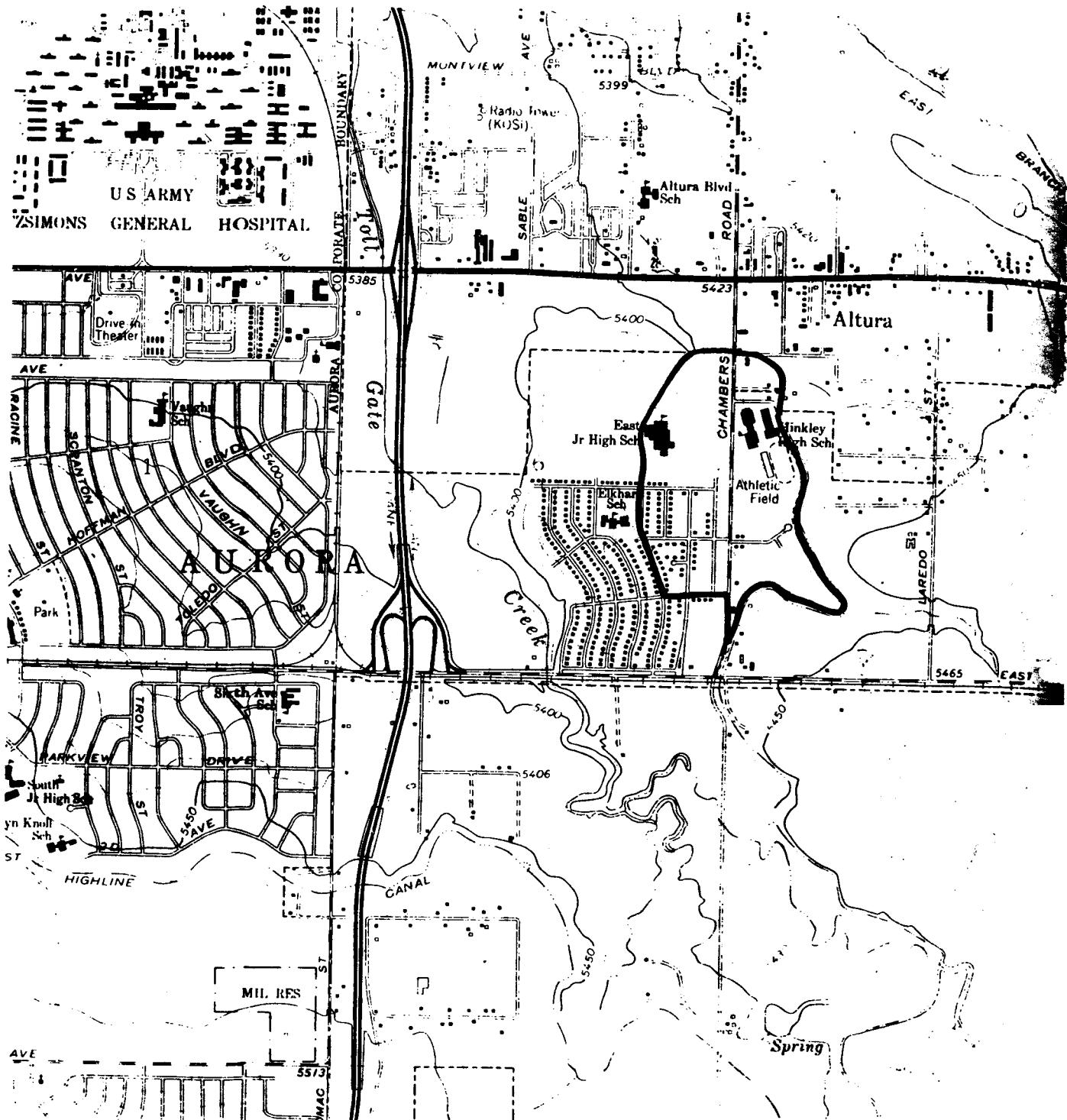


(a) topographic map - 1/24,000

FIGURE B-2. STAPLETON WATERSHEDS. The upper basin is the Stapleton Airport basin and contains 70 acres. The lower right basin is Stapleton-S and contains 130 acres.

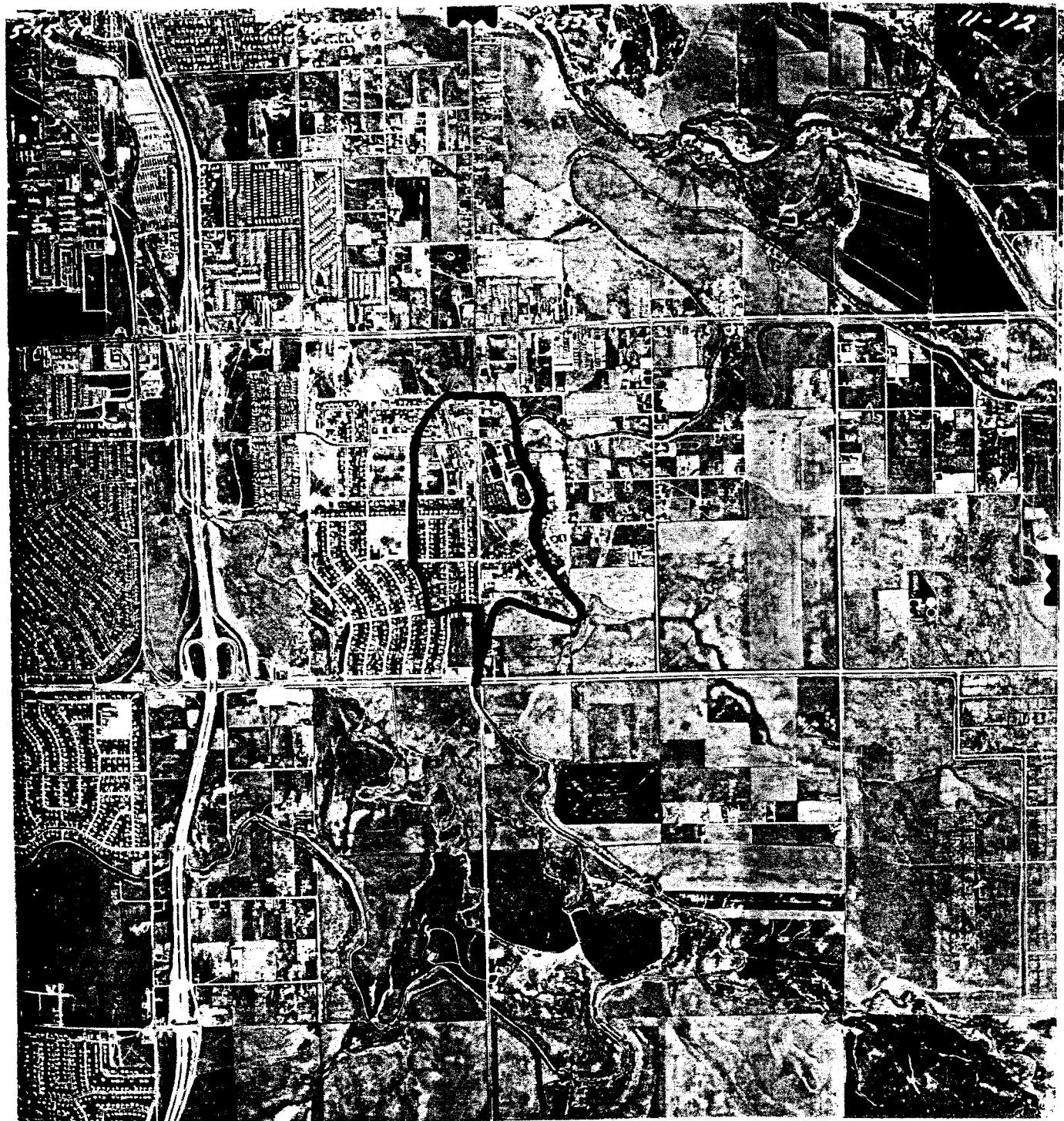


(b) airphoto - 1/27,500

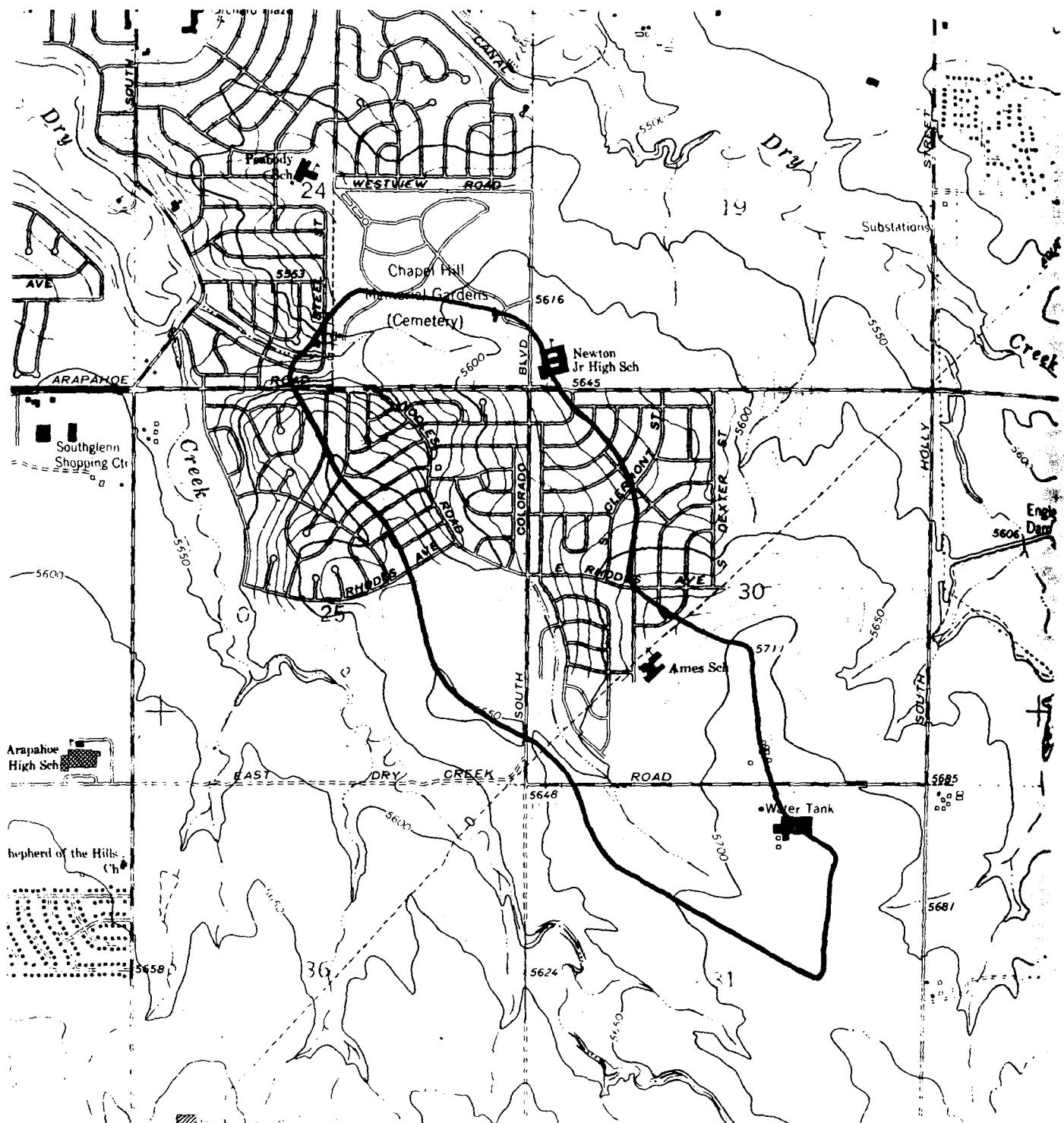


(a) topographic map - 1/24,000

FIGURE B-3. AURORA WATERSHED. The basin contains 180 acres.

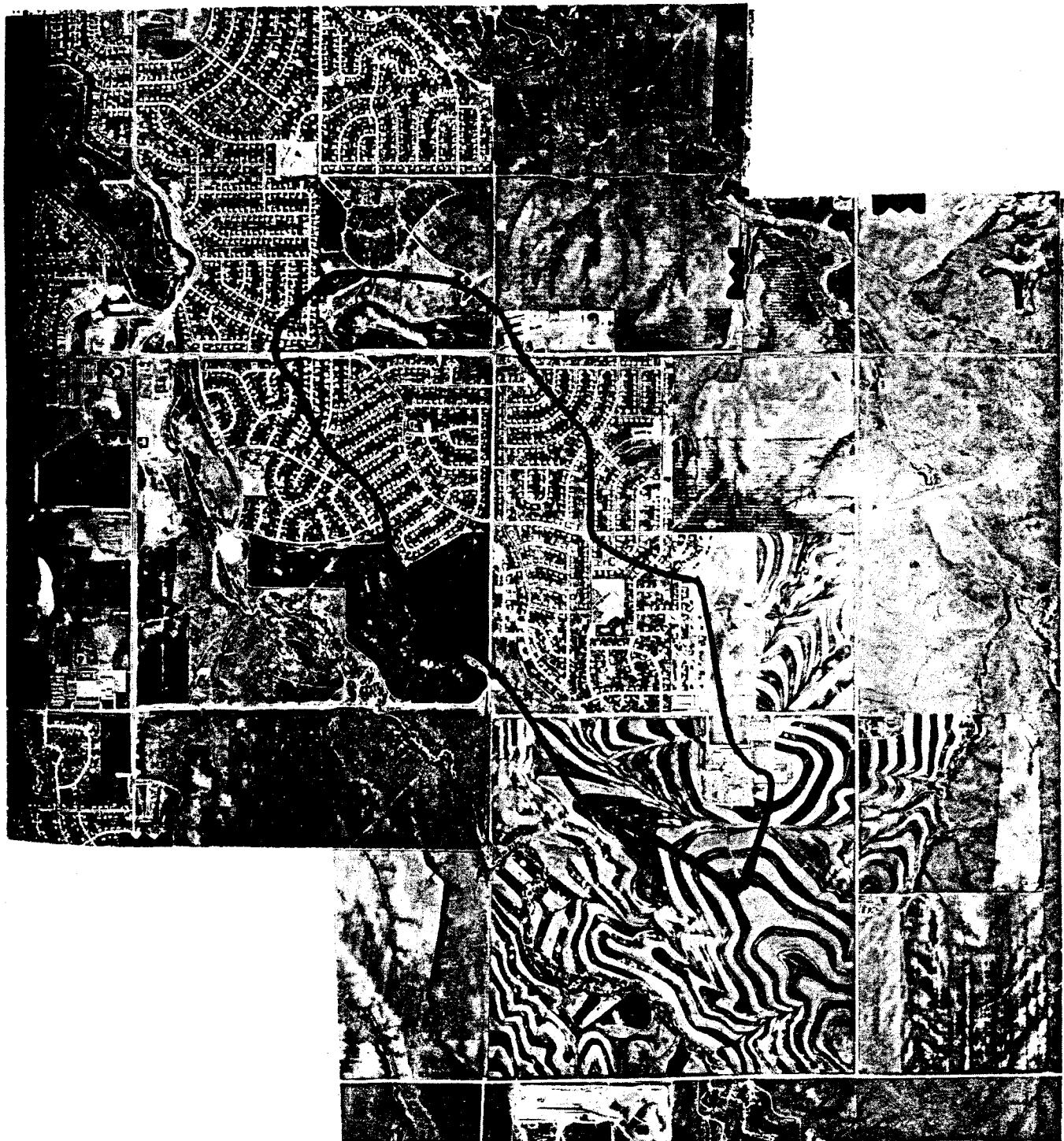


(b) airphoto - 1/27,500

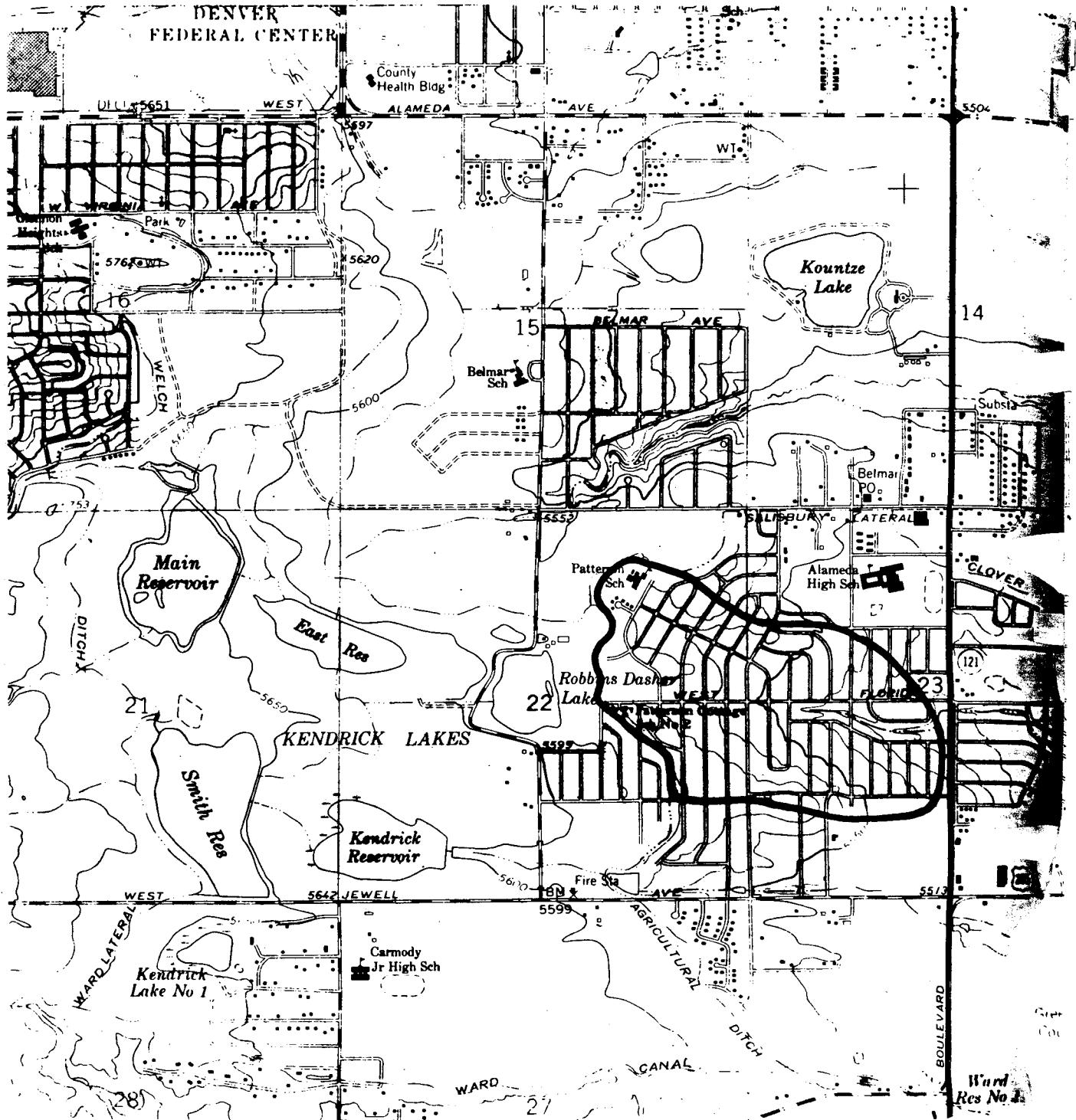


(a) topographic map - 1/24,000

FIGURE B-4. LITTLETON WATERSHED. The basin contains 600 acres.



(b) airphoto - 1/27,500

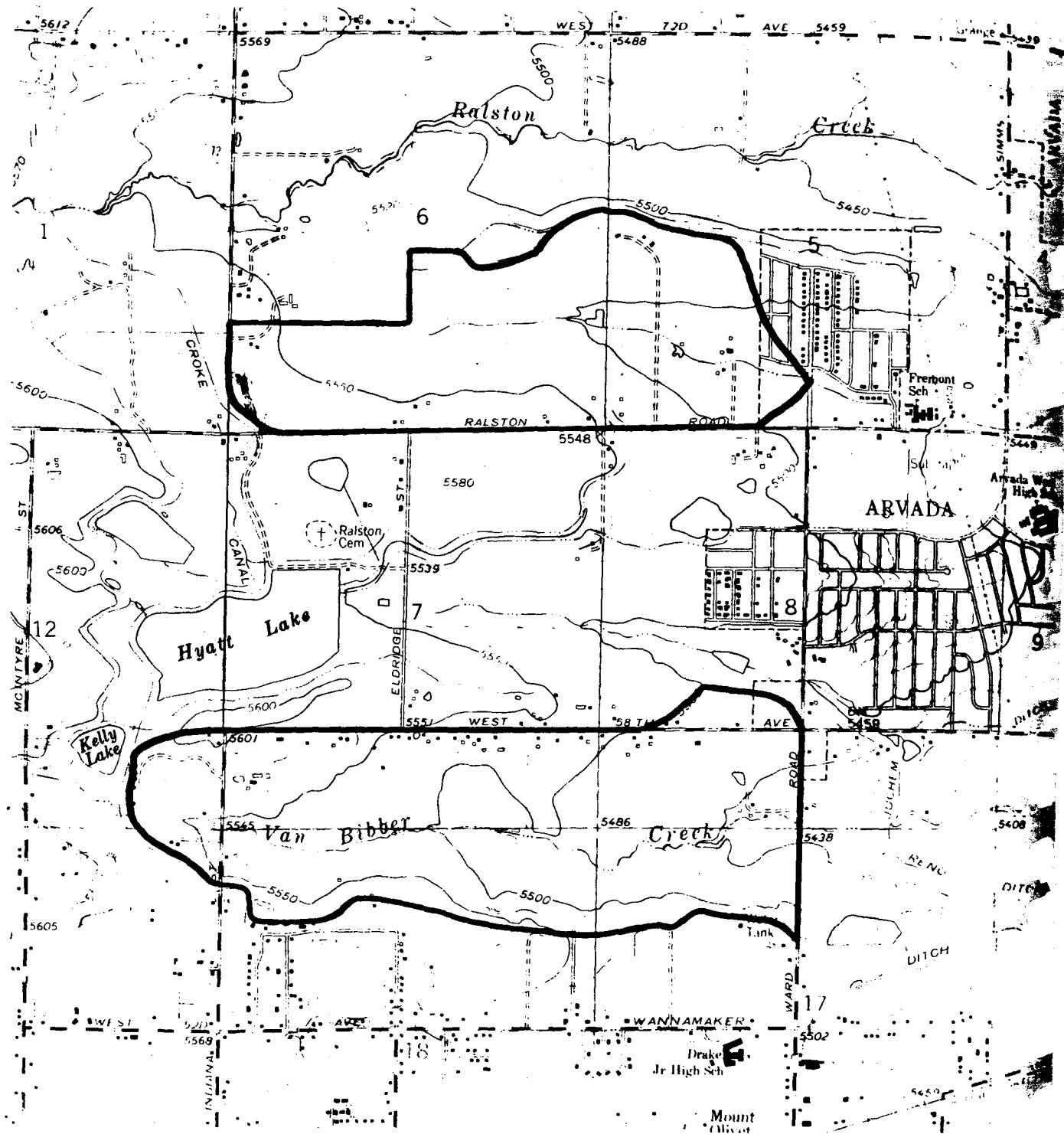


(a) topographic map - 1/24,000

FIGURE B-5. FORT LOGAN WATERSHED. The basin contains 275 acres.

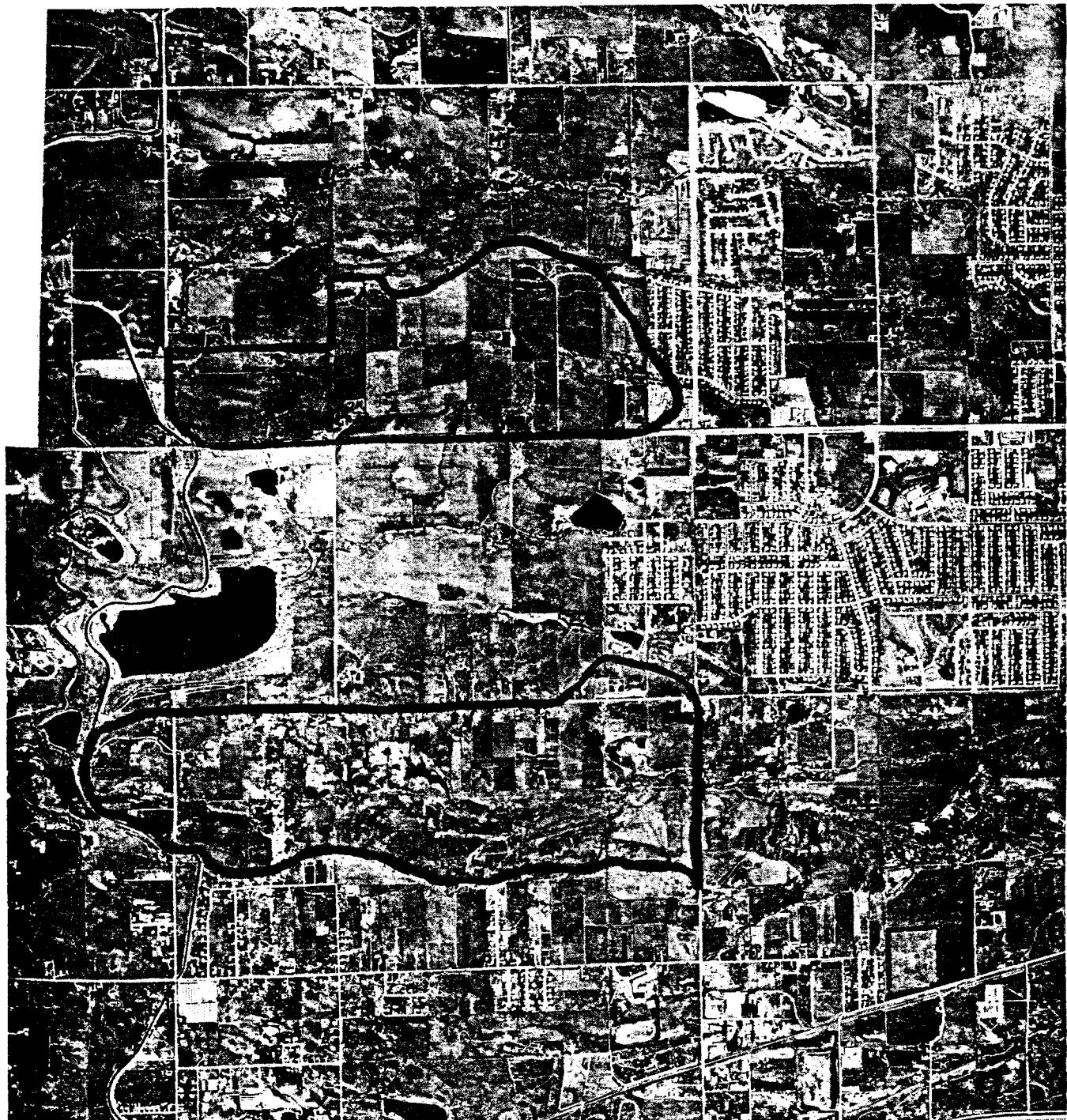


(b) airphoto - 1/27,500

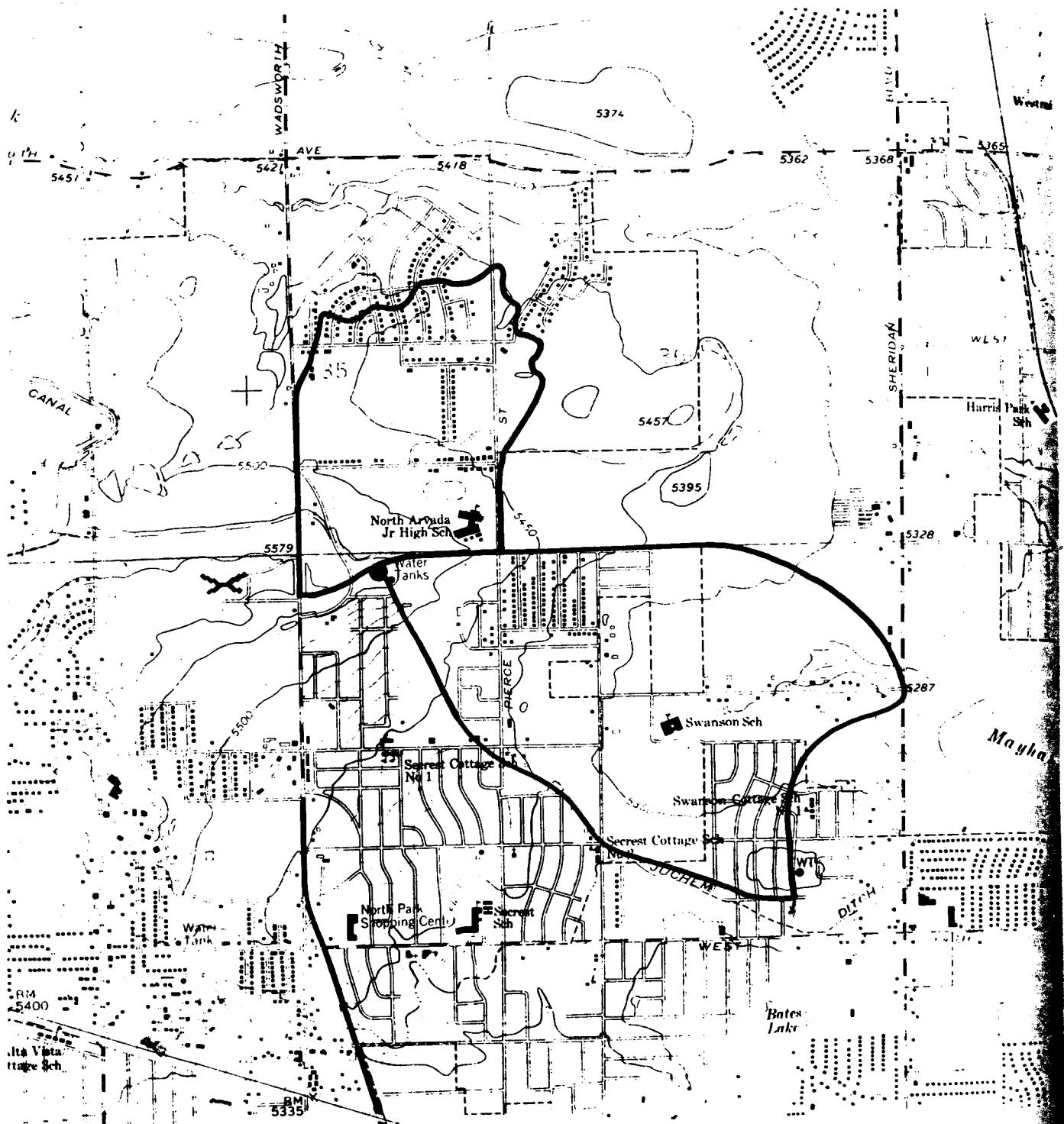


(a) topographic map - 1/24,000

FIGURE B-6. HYATT LAKE WATERSHEDS. The upper basin is Hyatt Lake-N and contains 380 acres, while the lower basin is Hyatt Lake-S and contains 600 acres.

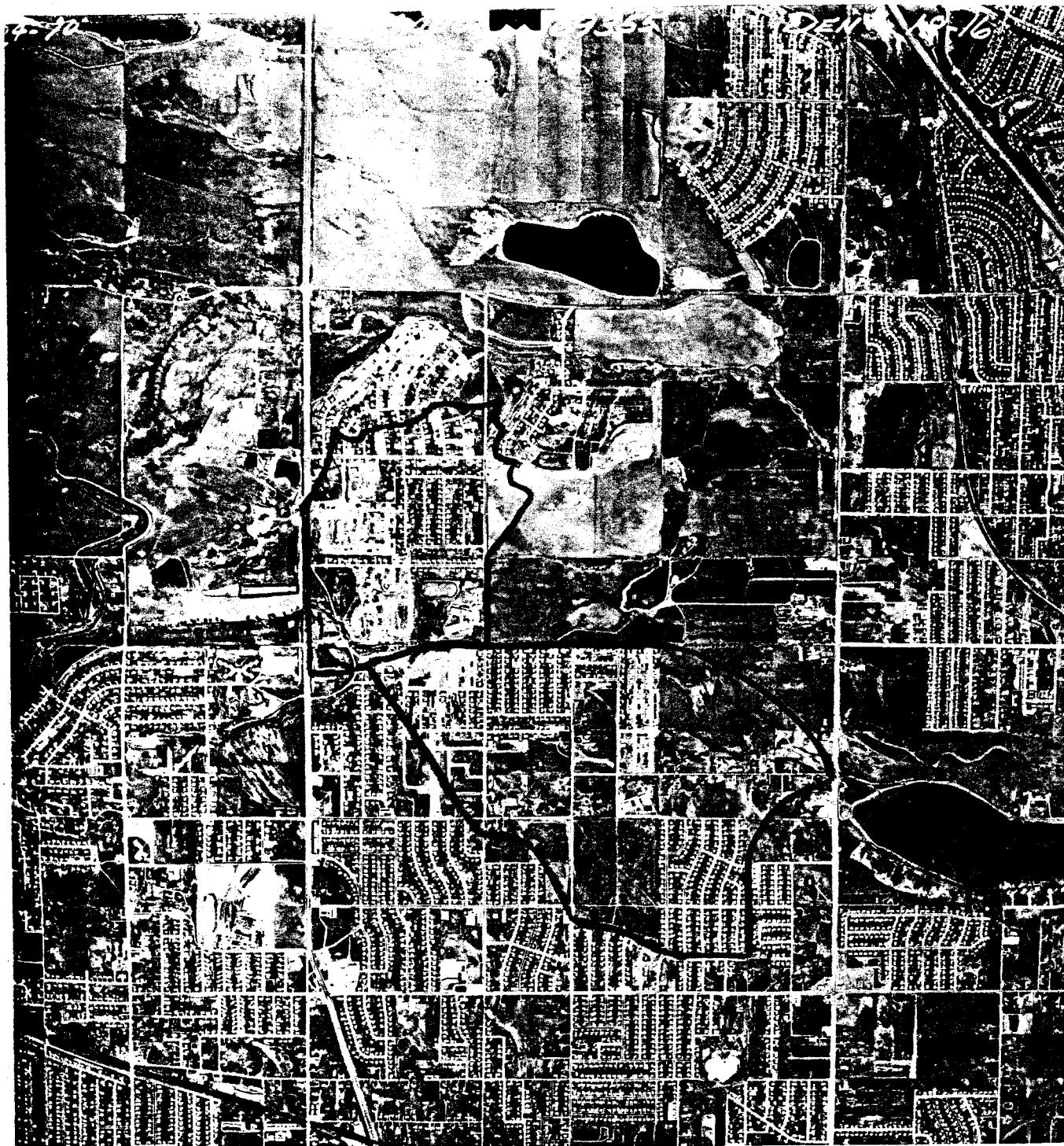


(b) airphoto - 1/27,500

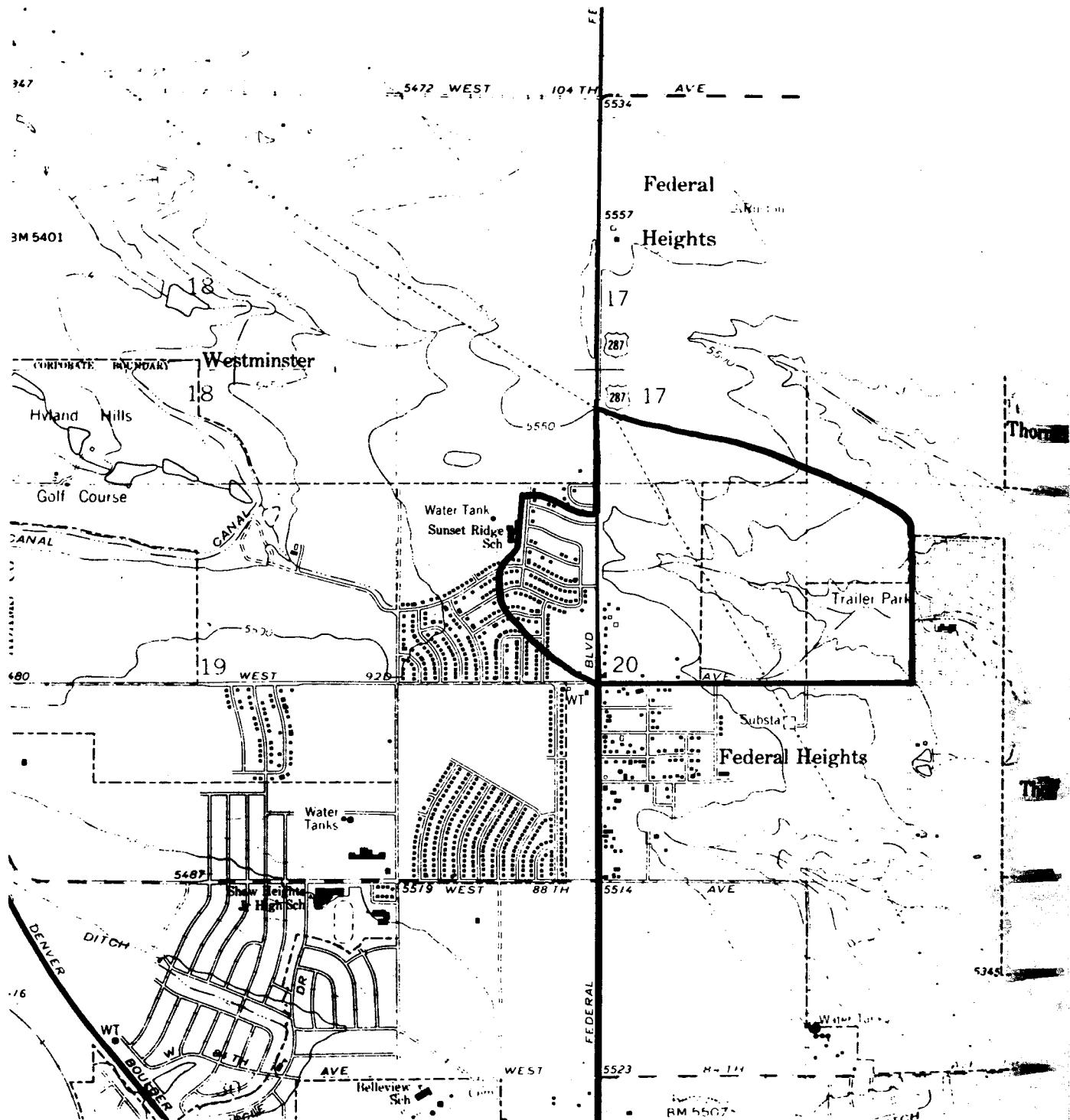


(a) topographic map - 1/24,000

FIGURE B-7. ARVADA WATERSHEDS. The upper basin is Arvada-N and contains 200 acres, while the lower basin is Arvada-S and contains 450 acres.

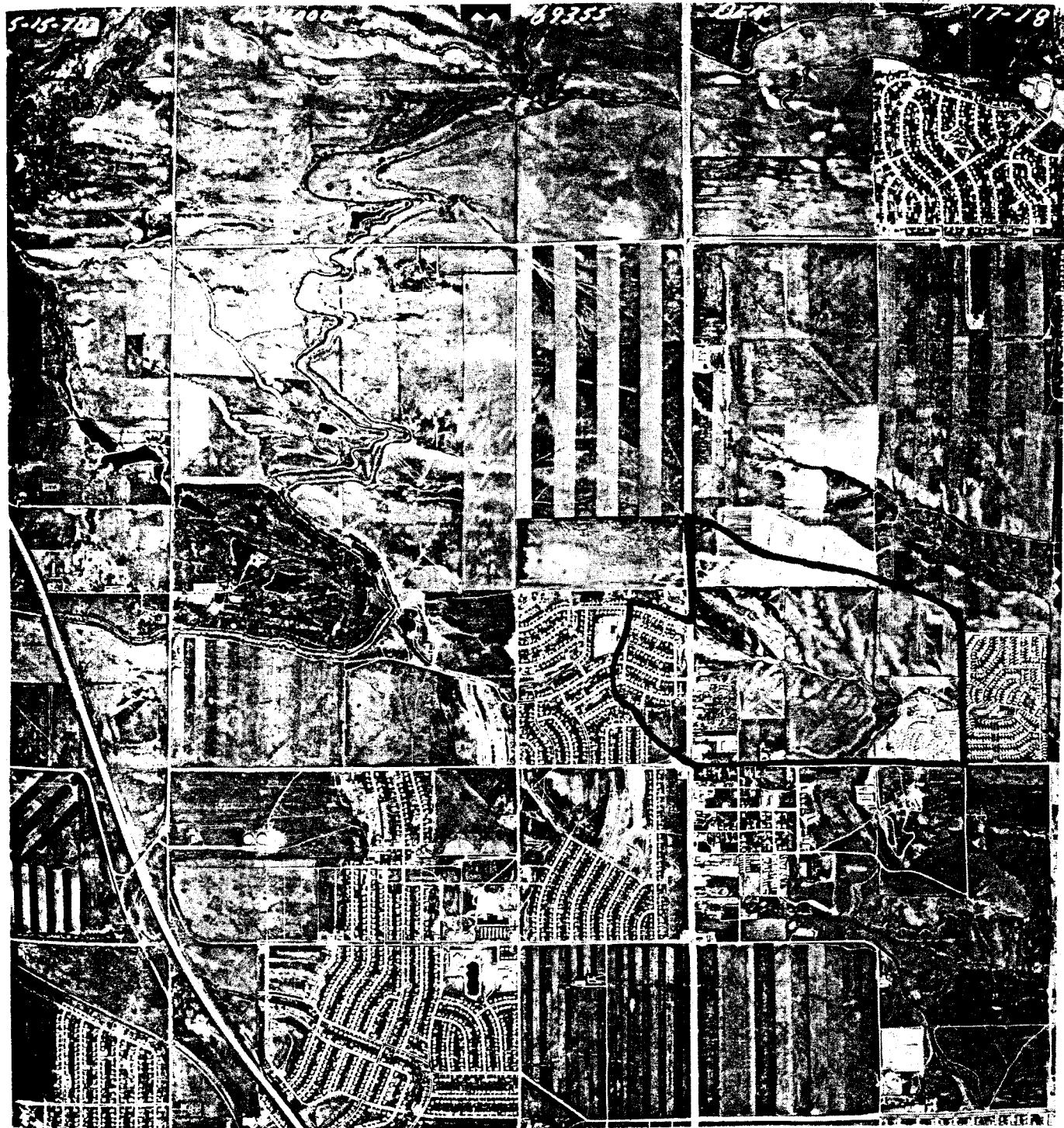


(b) airphoto - 1/27,500

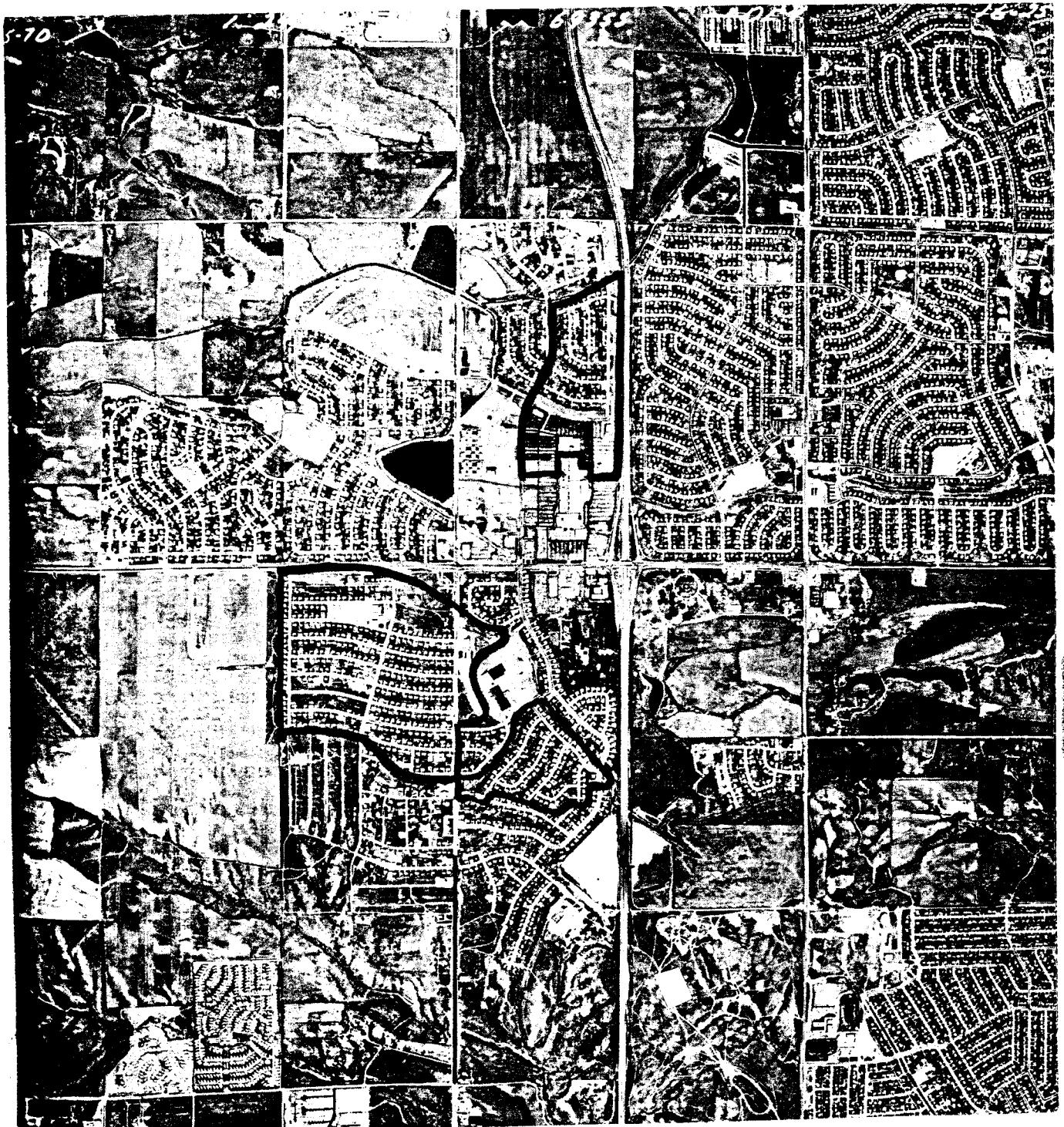


(a) topographic map - 1/24,000

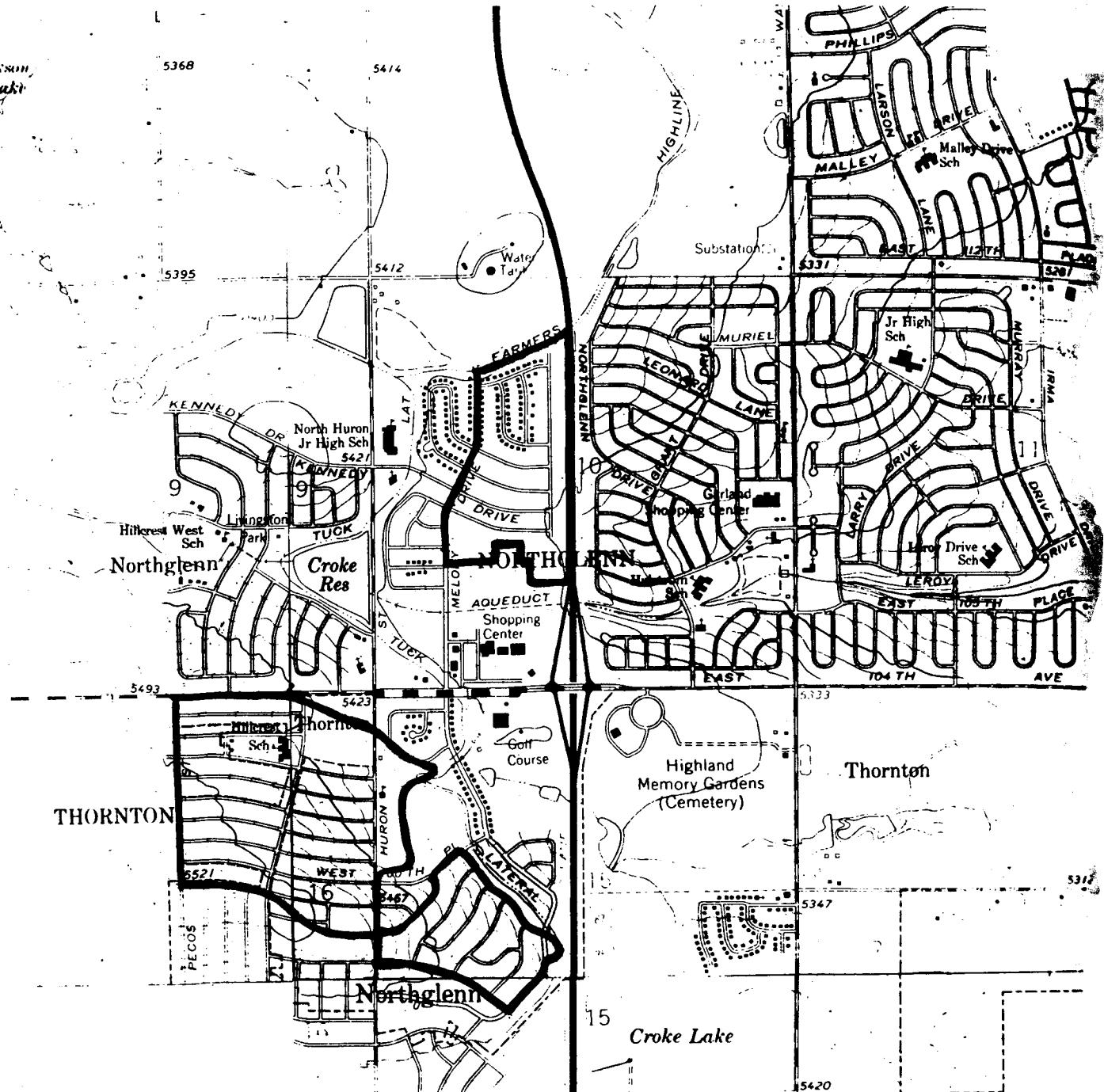
FIGURE B-8. FEDERAL HEIGHTS WATERSHED. The basin contains 300 acre



(b) airphoto - 1/27,500



(b) airphoto - 1/27,500



(a) topographic map - 1/24,000

FIGURE B-9. NORTHGLENN WATERSHEDS. Upper basin is Northglenn #7204 and contains 70 acres. Middle left basin #7203 contains 180 acres. Lower basin #7201 contains 40 acres.

APPENDIX C: DESCRIPTION OF THE
EQUIVALENT-SQUARE INTERPRETIVE TECHNIQUE

The total area of each watershed is initially determined by fitting a square of equal area to the irregular boundary of the basin being analyzed such that parts of the watershed lying outside the square are equal to areas within the square not contained in the watershed (Fig. C-1). One side of the square is scaled into ten equal parts which are marked off on a note card as a scale and each resulting interval is the side of a square which comprises one percent of the watershed area. The note card is then used essentially as a scale to measure the areas of each of the watershed units within the watershed, referenced to a one percent estimation area. For example, the number of rooftops necessary to fill a one percent square (N) is determined, the total number of houses in the watershed counted (H), and the percent area of rooftops calculated as H/N . Larger roofs are treated separately and added to the total figure. Street areas are determined by measuring total street length on one percent units and multiplying by the street width, also in one percent units. Grass, fields, and cultivated areas are measured by counting the number of one percent squares that occupy the area.

The final tally of all areas for a watershed does not generally exactly equal one hundred percent and all measured areas are adjusted in proportion to their size to compensate for the difference. Measurements normally need to be slightly adjusted one way or the other by increments of one to five percent, depending on the area initially measured. After initial development and practice, the equivalent-square technique reproduces percent area measurements on the same basin to within one to two percent. Possible sources of measurement error are:

1. Incorrect determination of the initial equivalent square.
2. Difficulty in delineating object boundaries on poorer quality photos.
3. Incorrect determination of the number of rooftops contained in the one percent square.
4. Difficulty in measuring areas much smaller than the one percent square, such as driveways, small grass plots, small areas of bare soil, etc.

Considering the time involved to measure the areal percentage of surface units in each watershed (45 minutes to one hour) and the overall purpose of the resulting data, this method is sufficiently accurate. Changes in impervious cover with time, due to urban development, can be detected from this data to within five percent.

A tabulation form showing the areal extent of each watershed unit in terms of pervious or impervious cover is used during the interpretation of each basin (Fig. C-2). A second tabulation form is constructed from these airphoto interpretations which indicates short term and seasonal changes of the hydrological character of each of the watershed units (Fig. C-3). All impervious materials show little or no change with changing conditions, but the pervious materials will behave differently under different rainfall, snowfall, and seasonal conditions. The approximate ratio between pervious and impervious surface materials can be logically estimated for each season condition, e.g., the soil area is one hundred percent impervious in frozen winter conditions. These estimated ratios (Fig. C-3) for each surface material and season can be applied to the percentage of the surface material in a given watershed to arrive at a seasonal estimation of the variation in impervious and pervious surface area in that watershed.

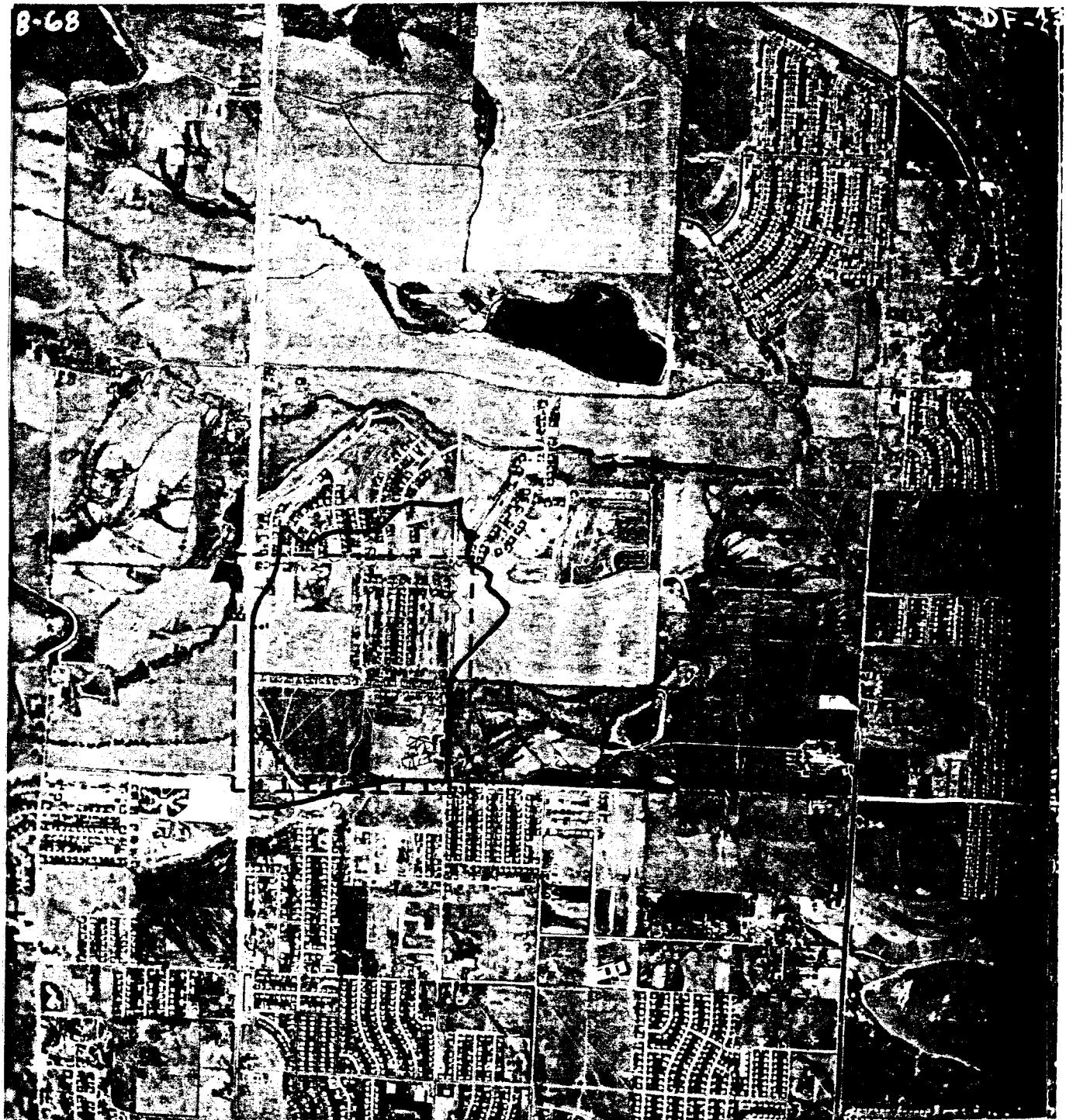


FIGURE C-1. FITTING AN EQUIVALENT-SQUARE TO THE ARVADA-N WATERSHED.

The area inside the dashed square is approximately equal to the area inside the solid irregular watershed boundary. The tick marks on the edge of the square represent the sizes of measurement cells whose areas are one percent of the watershed boundary.

	P = PERVIOUS	I = IMPERVIOUS	UNDEVELOPED RURAL	SEMI DEVELOPED SUBURBAN	COMPLETELY DEVELOPED SUBURBAN (<5 YEARS OLD)	COMPLETELY DEVELOPED SUBURBAN (>5 YEARS OLD)	BUSINESS	LIGHT INDUSTRY (OFFICES, LIGHT MANUFACTURING)	HEAVY INDUSTRY (STEEL MILLS, REFINERIES, HEAVY MANUFAC)
CONCRETE									
ASPHALT									
ROOFTOPS									
GRAVEL	1								
LAWNS									
FIELDS/PASTURE	8								
AGRICULTURE	90								
TREES	1								
EXPOSED SOIL									
WATER									
TOTAL AREA P	100								
TOTAL AREA I		0							

FIGURE C-2. SAMPLE EQUIVALENT-SQUARE TABULATION. Pervious (P) and impervious (I) areas as a percent of the total watershed area for the Arvada-N watershed using a 1949 airphoto. See Figure C-1 for an airphoto of this watershed.

	P = PERVIOUS	I = IMPERVIOUS	na = not applicable	WINTER OR GROUND FROZEN	SPRING GROUND FROZEN AND PARTLY THAWED	SPRING GROUND ALMOST SATURATED WITH WATER	SUMMER AFTER ONE HR RAINFALL	SUMMER ONE WEEK AFTER RAINFALL	AUTUMN 2-3 WEEKS WITHOUT RAIN	WINTER GROUND BARE AND COMPLETELY FROZEN	WINTER GROUND COVERED WITH SNOW
	P	I	P	P	I	P	I	P	I	P	I
CONCRETE	0	1.0	0	1.0	0	1.0	0	1.0	0	1.0	0
ASPHALT	0	1.0	0	1.0	0	1.0	0	1.0	0	1.0	0
ROOFTOPS	0	1.0	0	1.0	0	1.0	0	1.0	0	1.0	0
GRAVEL	.10	.90	.15	.85	.20	.80	.25	.75	.25	.75	.10
LAWNS	.25	.75	.17	.83	.30	.70	.25	.75	.35	.65	.10
FIELDS/PASTURE	.20	.80	.15	.85	.25	.75	.60	.40	.30	.70	.10
AGRICULTURE	.25	.75	.17	.83	.35	.65	.30	.70	.40	.60	.10
TREES	.30	.70	.20	.80	.35	.65	.30	.70	.40	.60	.10
EXPOSED SOIL	.20	.80	.15	.85	.30	.70	.65	.35	.40	.60	.10
WATER	1.0	0	1.0	0	1.0	0	1.0	0	1.0	0	1.0
TOTAL AREA P	na	na	na	na	na	na	na	na	na	na	na
TOTAL AREA I	na	na	na	na	na	na	na	na	na	na	na

FIGURE C-3. FACTORS USED FOR PRORATING MEASURED VALUES TO ACCOUNT FOR SEASONAL VARIATIONS. These factors applied to the surface area estimates in Figure C-2 reapportion the surfaces into impervious and pervious areas according to season. These are only logical estimates and the user may substitute his own factors.

APPENDIX D: SURFACE MATERIAL CLASSIFICATION OF
THIRTEEN WATERSHEDS, DENVER, COLORADO

The watershed surface material classifications which follow are in horizontal, adjacent, twin tables. The left table represents percent areas of the surface materials found in the watershed and the right table the projected seasonal variation in the perviousness and imperviousness of the materials.

The percent area of each of the surface materials in the watershed is determined by the equivalent-square technique (Appendix C). The resulting data is tabulated according to perviousness or imperviousness under the appropriate land use category in the left half of each twin table. These surface material classifications characterize the watershed as it would appear to a remote sensing device and during subsequent image processing.

The surface material classification is further refined to account for seasonal effects which may cause the relative perviousness of many surface materials to vary considerably. Estimates of degrees of perviousness of the pervious materials were calculated based upon the proportions shown in Figure C-3 of Appendix C. The percent area of pervious materials is multiplied by the proportions for the appropriate seasonal conditions and occurs in the right half of each of the twin tables. Totals at the bottom of the table show the total relative perviousness versus imperviousness of the watershed under the different seasonal conditions. In this analysis the impervious surface materials were treated as impervious under all conditions. For the pervious materials the relative degree of perviousness or imperviousness takes into account such factors as lawn sprinkling, irrigation, soil compaction in pasture, imperviousness of frozen surfaces, etc. This portion of the analysis represents possible interpretations of the surface material classifications that may be of interest to the hydrologist in a water yield prediction model and further illustrates how remote multispectral classification of surfaces might be refined for use in an urban watershed model.

Watershed analysis data for Arvada - N, 1949

P = PVIOUS I = IMPVIOUS		CONCRETE																		
		ASPHALT		ROOFTOPS		GRAVEL		LAWNS		FIELDS/PASTURE		AGRICULTURE		TREES		EXPOSED SOIL		WATER		
UNDEVELOPED	RURAL	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	TOTAL AREA	P
SEMI-DEVELOPED	SUBURBAN	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	TOTAL AREA	I
COMPLETED	SUBURBAN (15 years)	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	TOTAL AREA	P
COMPLETED	SUBURBAN (15 years)	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	TOTAL AREA	I
DEVELOPED	SUBURBAN (15 years)	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	TOTAL AREA	P
DEVELOPED	SUBURBAN (15 years)	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	TOTAL AREA	I
BUSINESS	LIGHT INDUSTRY	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	TOTAL AREA	P
MANUFACTURING	HEAVY INDUSTRY	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	TOTAL AREA	I
REFINING MILLS	HEAVY INDUSTRY	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	TOTAL AREA	P
WATER	WATER	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	TOTAL AREA	I
WATER	WATER	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	TOTAL AREA	P
EXPOSED SOIL	EXPOSED SOIL	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	TOTAL AREA	I
TREES	TREES	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	TOTAL AREA	P
AGRICULTURE	AGRICULTURE	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	TOTAL AREA	I
FIELDS/PASTURE	FIELDS/PASTURE	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	TOTAL AREA	P
LAWNS	LAWNS	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	TOTAL AREA	I
GRAVEL	GRAVEL	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	TOTAL AREA	P
ROOFTOPS	ROOFTOPS	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	TOTAL AREA	I
ASPHALT	ASPHALT	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	P	TOTAL AREA	P

Watershed analysis data for Arvada - N. 1954

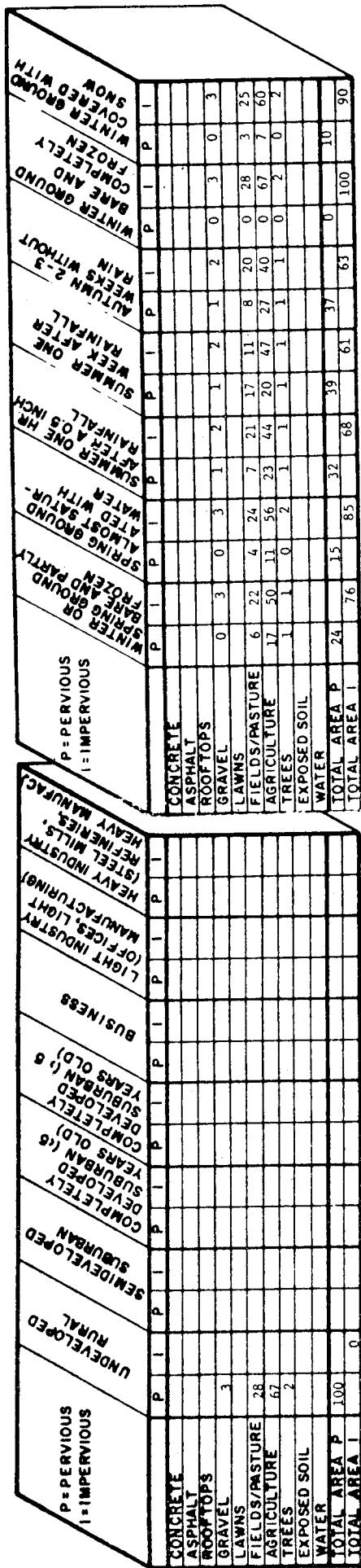
Watershed analysis data for Arvada - N, 1959

Watershed analysis data for Arvada - N, 1963

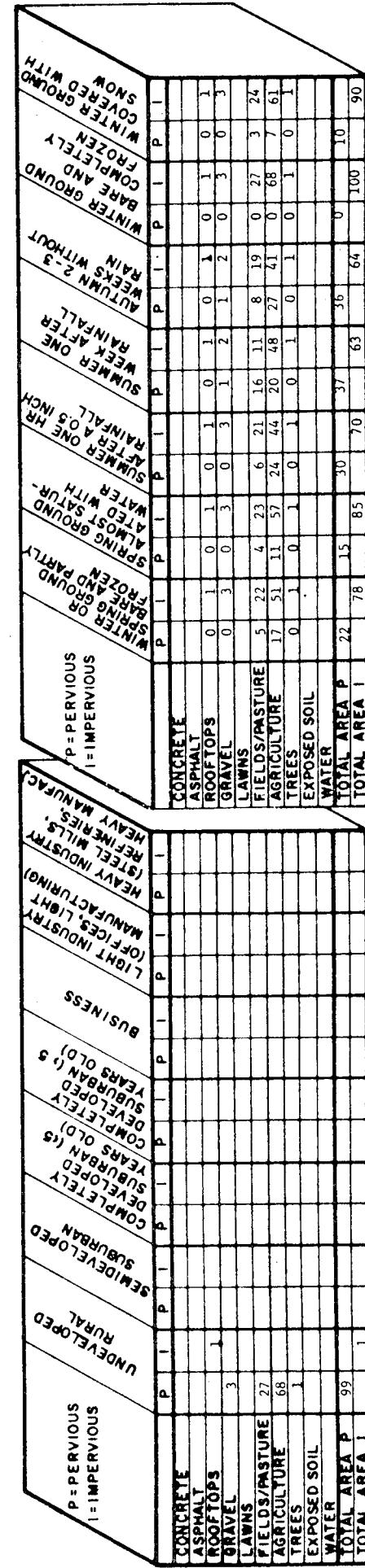
Watershed analysis data for Arvada - N, 1968

P = Pervious I = Imperious		Soil Development (Years Old)									
Undeveloped Rural		Semi-Urban		Developed Urban (1-5 Years Old)		Developed Urban (6-10 Years Old)		Developed Urban (11-15 Years Old)		Developed Urban (16+ Years Old)	
CONCRETE	P	0	1	0	1	0	1	0	1	0	1
ASPHALT	P	0	10	0	10	0	10	0	10	0	10
ROOFTOPS	P	0	14	0	14	0	14	0	14	0	14
GRAVEL	P	5	16	4	17	10	11	10	12	9	0
LAWNS	P	7	22	5	24	6	23	19	10	10	19
FIELDS/PASTURE	P	0	1	0	1	0	1	0	1	0	1
AGRICULTURE	P	0	1	0	1	0	1	0	1	0	1
TREES	P	6	18	4	20	7	17	16	8	9	15
EXPOSED SOIL	P	0	1	0	1	0	1	0	1	0	1
WATER	P	0	1	0	1	0	1	0	1	0	1
TOTAL AREA I	P	18	11	11	23	17	23	17	23	17	23
TOTAL AREA P	P	82	87	77	53	47	32	0	0	0	93

Watershed analysis data for Arvada - N, 1970



Watershed analysis data for Arvada - S, 1949



Watershed analysis data for Arvada - S, 1954

Watershed analysis data for Arvada - S, 1959

		P = PERVIOUS I = IMPERVIOUS		
		UNDEVELOPED RURAL		
		SEMI-DEVELOPED SUBURBAN		
		COMPLETED SUBURBAN (18 YEARS OLD)		
		P	I	P
CONCRETE		2		
ASPHALT		15		
ROOFTOPS		20		
GRAVEL		1		
LAWNS		25		
FIELDS/PASTURE		32		
AGRICULTURE				
TREES		1		
EXPOSED SOIL		4		
WATER				
TOTAL AREA P		62		
TOTAL AREA I		38		

Watershed analysis data for Arvada - S, 1970

		P = PERVIOUS I = IMPERVIOUS		
		UNDVELOPED RURAL		
		SEMI-DEVELOPED SUBURBAN		
		COMPLETED SUBURBAN (18 YEARS OLD)		
		P	I	P
CONCRETE				
ASPHALT		1		
ROOFTOPS				
GRAVEL				
LAWNS				
FIELDS/PASTURE		8		
AGRICULTURE				
TREES				
EXPOSED SOIL				
WATER				
TOTAL AREA P		25		
TOTAL AREA I		75		

		P = PERVIOUS I = IMPERVIOUS		
		HEAVY INDUSTRY REFINERIES, MILLS, MANUFACTURERS		
		LIGHT INDUSTRY FARM/AGRICULTURE		
		BUSINESS		
		P	I	P
CONCRETE				
ASPHALT				
ROOFTOPS				
GRAVEL				
LAWNS				
FIELDS/PASTURE				
AGRICULTURE				
TREES				
EXPOSED SOIL				
WATER				
TOTAL AREA P		1		
TOTAL AREA I		1		

		P = PERVIOUS I = IMPERVIOUS		
		SPRING AND SUMMER WATER		
		AUTUMN ONE WEEK AFTER		
		SUMMER ONE WEEK AFTER		
		P	I	P
CONCRETE		2		
ASPHALT		0		
ROOFTOPS		0		
GRAVEL		0		
LAWNS		0		
FIELDS/PASTURE		0		
AGRICULTURE		0		
TREES		0		
EXPOSED SOIL		0		
WATER		0		
TOTAL AREA P		18		
TOTAL AREA I		82		

		P = PERVIOUS I = IMPERVIOUS		
		AUTUMN TWO WEEKS AFTER		
		WINTER ONE WEEK AFTER		
		P	I	P
CONCRETE		2		
ASPHALT		0		
ROOFTOPS		0		
GRAVEL		0		
LAWNS		0		
FIELDS/PASTURE		0		
AGRICULTURE		0		
TREES		0		
EXPOSED SOIL		0		
WATER		0		
TOTAL AREA P		1		
TOTAL AREA I		1		

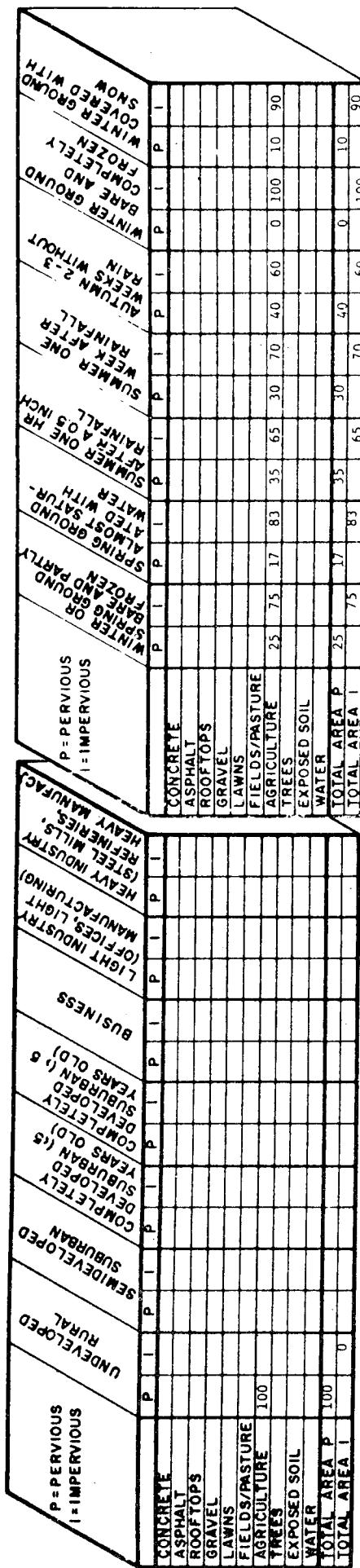
Watershed analysis data for Federal Heights, 1954

Watershed analysis data for Federal Heights. 1959

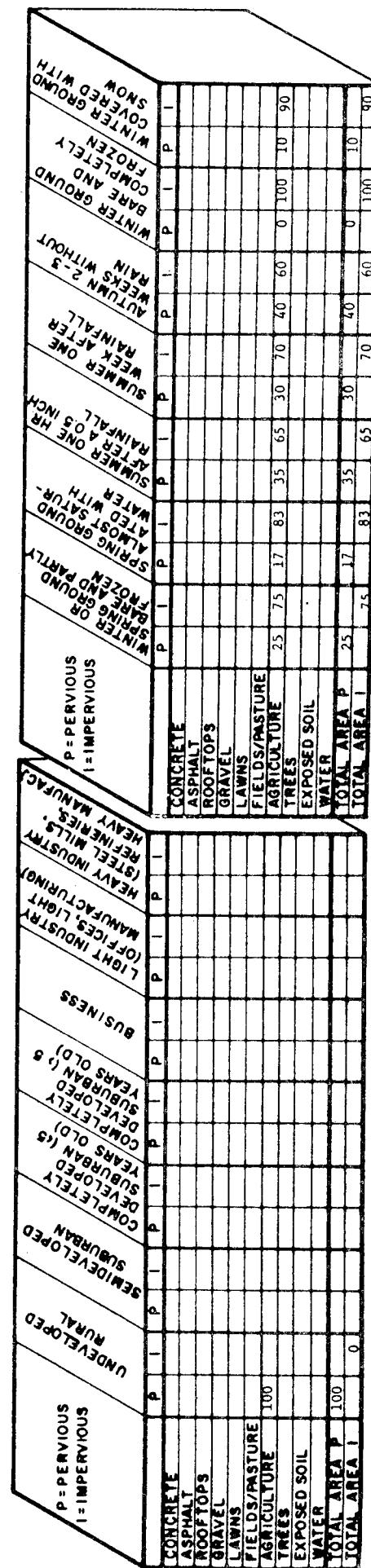
Watershed analysis data for Federal Heights. 1963

Watershed analysis data for Federal Heights, 1968

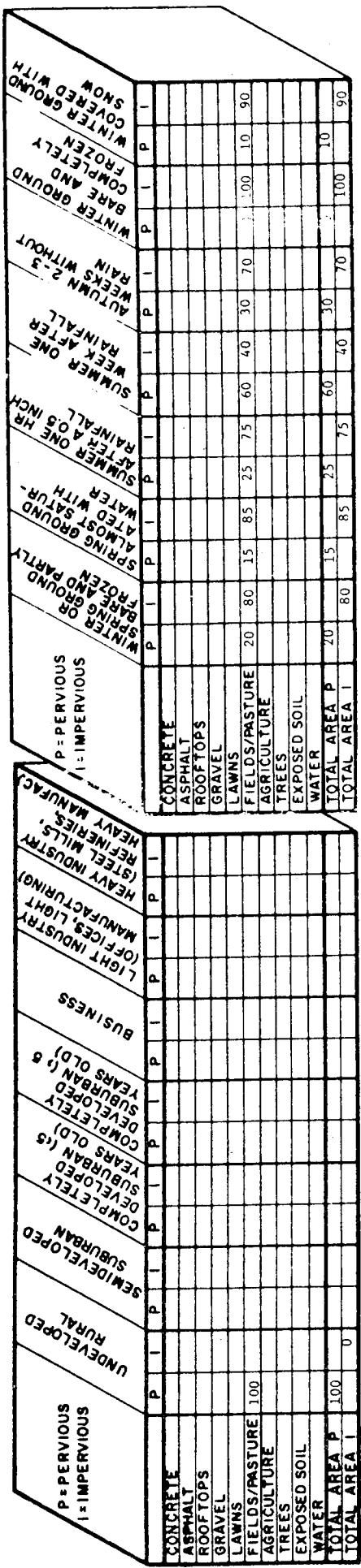
Watershed analysis data for Federal Heights, 1970



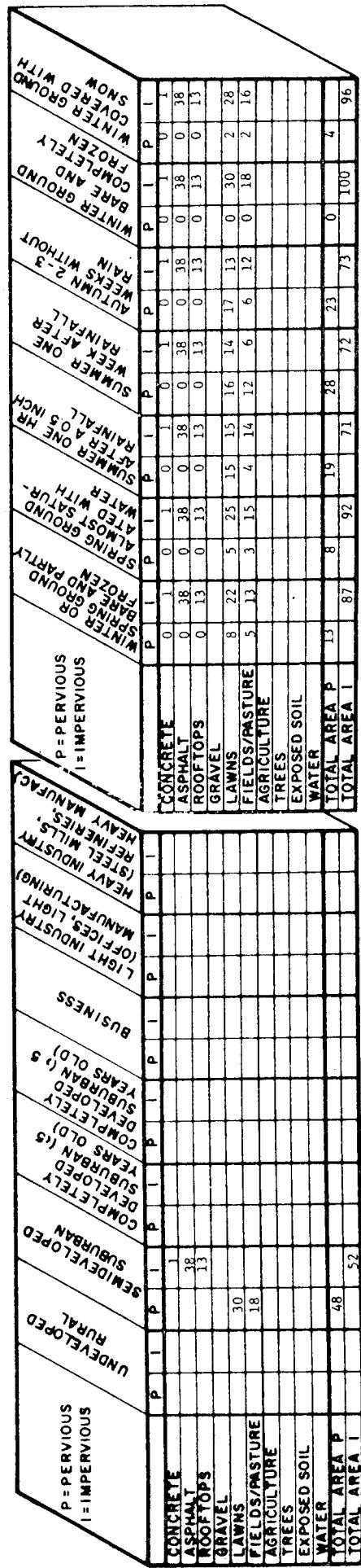
Watershed analysis data for Northglenn 7204, 1954



Watershed analysis data for Northglenn 7204, 1959



Watershed analysis data for Northglenn 7204, 1963



Watershed analysis data for Northglenn 7204, 1968

		P = PERVIOUS		I = IMPERVIOUS		CONCRETE		ASPHALT		ROOFTOPS		GRAVEL		LAWNS		FIELDS/PASTURE		AGRICULTURE		TREES		EXPOSED SOIL		WATER		TOTAL AREA P		TOTAL AREA I	
		WINTER GROUND COV.		WINTER GROUND COV.																									
		SUMMER ONE-HOUR RAINFALL																											
		AUTUMN 2-3 WEEKS																											
		WINTER GROUND COV.																											
		TOTAL AREA P		TOTAL AREA I		TOTAL AREA P		TOTAL AREA I		TOTAL AREA P		TOTAL AREA I		TOTAL AREA P		TOTAL AREA I		TOTAL AREA P		TOTAL AREA I		TOTAL AREA P		TOTAL AREA I		TOTAL AREA P			
		96		91		100		61		100		71		39		71		29		66		34		83		25		100	

Watershed analysis data for Northglenn 7204, 1970

		P = PERVIOUS		I = IMPERVIOUS		CONCRETE		ASPHALT		ROOFTOPS		GRAVEL		LAWNS		FIELDS/PASTURE		AGRICULTURE		TREES		EXPOSED SOIL		WATER		TOTAL AREA P		TOTAL AREA I	
		WINTER GROUND COV.																											
		SUMMER ONE-HOUR RAINFALL																											
		AUTUMN 2-3 WEEKS																											
		WINTER GROUND COV.																											
		TOTAL AREA P		TOTAL AREA I		TOTAL AREA P		TOTAL AREA I		TOTAL AREA P		TOTAL AREA I		TOTAL AREA P		TOTAL AREA I		TOTAL AREA P		TOTAL AREA I		TOTAL AREA P		TOTAL AREA I		TOTAL AREA P			
		55		9		45		45		1		1		1		1		1		1		1		1		1			

Watershed analysis data for Northglenn 7203, 1954

		P : PERVIOUS		I : IMPERVIOUS			
		P	I	P	I	P	I
CONCRETE							
ASPHALT							
ROOFTOPS	0	2	0	2	0	2	0
GRAVEL	0	3	0	3	1	2	1
LAWNS							
FIELDS/PASTURE	17	68	13	72	21	64	51
AGRICULTURE							
TREES	0	1	0	1	0	1	0
EXPOSED SOIL	2	7	1	8	3	6	3
WATER							
TOTAL AREA P	19	17	25	17	58	30	0
TOTAL AREA I	81	66	75	42	70	100	90

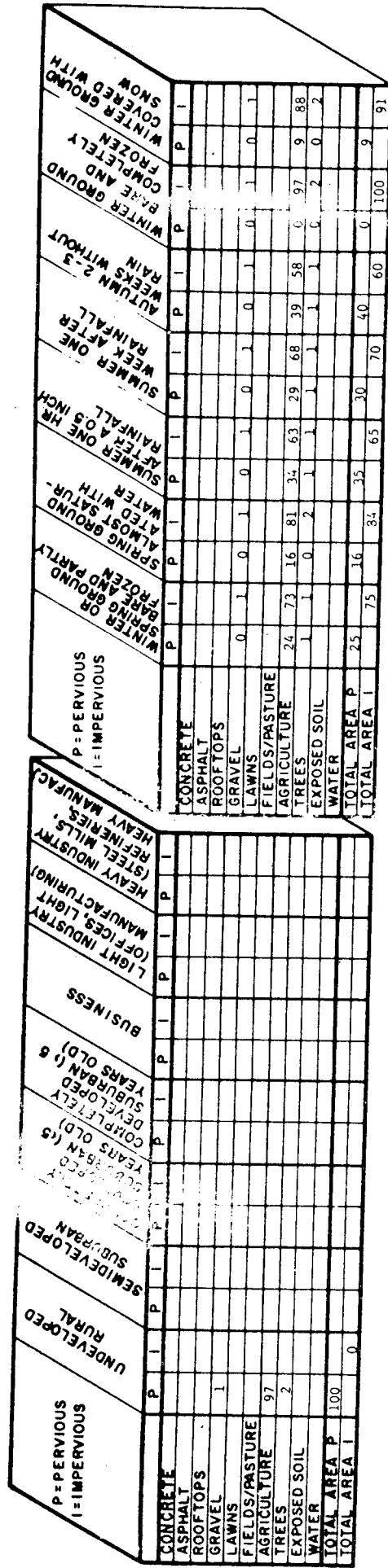
Watershed analysis data for Northglen 7203, 1959

		P : PERVIOUS		I : IMPERVIOUS			
		P	I	P	I	P	I
CONCRETE							
ASPHALT	0	1	0	1	0	1	0
ROOFTOPS	0	17	0	17	0	17	0
GRAVEL	0	14	0	14	0	14	0
LAWNS	0	0	0	0	0	0	0
FIELDS/PASTURE	3	10	2	11	4	9	3
AGRICULTURE	8	31	6	33	10	29	23
TREES	0	0	0	0	0	0	0
EXPOSED SOIL	3	13	2	14	5	11	6
WATER	0	0	0	0	0	0	0
TOTAL AREA P	14	10	19	19	36	23	7
TOTAL AREA I	86	90	81	81	64	77	93

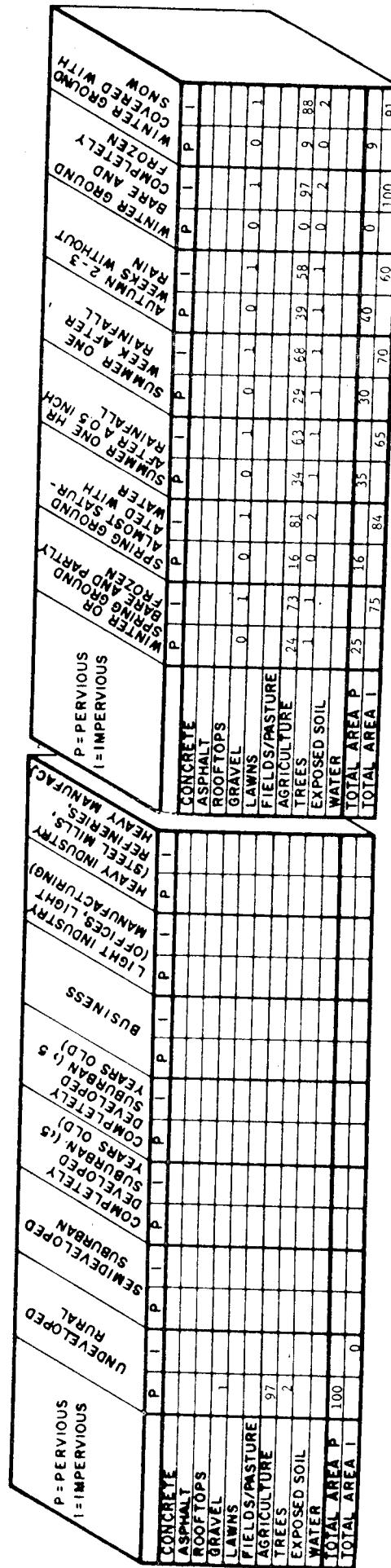
Watershed analysis data for Northglen 7203, 1963

Watershed analysis data for Northglenn 7203, 1968

Watershed analysis data for Northglenn 7203, 1970



Watershed analysis data for Northglenn 7201, 1954



Watershed analysis data for Northglen 7201, 1959

Watershed analysis data for Northglenn 7201, 1963

Watershed analysis data for Northglenn 7201, 1968

Watershed analysis data for Northglenn 7201, 1970

P = PERVIOUS I = IMPERVIOUS		UNDER RURAL SEMI-DEVELOPED		SUBURBAN COMPLETED (15 YEARS OLD)		CITY INDUSTRIAL DEVELOPMENT COMPLETED (15 YEARS OLD)		INDUSTRIAL HEAVY INDUSTRY (ICE, CFC, LIGHT REFINERIES)		MANUFACTURING HEAVY INDUSTRY (STEEL MILLS, REFINERIES)		SPRING GROUNDS WINTER GROUNDS SUMMER GROUNDS AUTUMN ONE WEEKS AFTER AUTUMN 2-3 WEEKS WITHOUT WINTER GROUNDS BARE AND COMPLETED WITH SNOW	
CONCRETE	P	1	P	1	P	1	P	1	P	1	P	1	
ASPHALT	I	22	I	22	I	22	I	22	I	22	I	22	
ROOFTOPS	I	26	I	26	I	26	I	26	I	26	I	26	
GRAVEL	I	50	I	50	I	50	I	50	I	50	I	50	
LAWNS	I	50	I	50	I	50	I	50	I	50	I	50	
FIELDS/PASTURE	I	50	I	50	I	50	I	50	I	50	I	50	
AGRICULTURE	I	50	I	50	I	50	I	50	I	50	I	50	
TREES	I	50	I	50	I	50	I	50	I	50	I	50	
EXPOSED SOIL	I	50	I	50	I	50	I	50	I	50	I	50	
WATER	I	50	I	50	I	50	I	50	I	50	I	50	
TOTAL AREA	P	12	P	8	P	25	P	26	P	27	P	27	
TOTAL AREA	I	88	I	92	I	75	I	74	I	73	I	73	

Watershed analysis data for Stapleton Airport, 1935

Watershed analysis data for Stapleton Airport, 1949

Watershed analysis data for Stapleton Airport, 1954

		P = PERVIOUS		I = IMPERVIOUS			
		P	I	P	I	P	I
UNDEVELOPED	RURAL						
SUPERBUILT	SEMI-URBAN						
COMPLETED	DEVELOPED (15 years)						
COMPLETED	DESUBURBAN (15 years old)						
COMPLETED	DESUBURBAN (old)						
BUSINESS	OFFICES, LIGHT						
LIGHT INDUSTRY	MANUFACTURING						
HEAVY INDUSTRIES	STEEL MILLS,						
HEAVY INDUSTRIES	REFINERIES, MANUFACTURERS						
HEAVY INDUSTRIES	HEAVY INDUSTRY						
BUSINESS	OFFICES, LIGHT						
LIGHT INDUSTRY	MANUFACTURING						
HEAVY INDUSTRIES	STEEL MILLS,						
HEAVY INDUSTRIES	REFINERIES, MANUFACTURERS						
HEAVY INDUSTRIES	HEAVY INDUSTRY						
TOTAL AREA P	78						
TOTAL AREA I	22						

Watershed analysis data for Stapleton Airport, 1956

		P = PERVIOUS		I = IMPERVIOUS			
		P	I	P	I	P	I
UNDERRAILED	COMPLETED						
SUPERBUILT	DESUBURBAN (15 years old)						
COMPLETED	DESUBURBAN (old)						
BUSINESS	OFFICES, LIGHT						
LIGHT INDUSTRY	MANUFACTURING						
HEAVY INDUSTRIES	STEEL MILLS,						
HEAVY INDUSTRIES	REFINERIES, MANUFACTURERS						
HEAVY INDUSTRIES	HEAVY INDUSTRY						
TOTAL AREA P	15						
TOTAL AREA I	85						

		P = PERVIOUS		I = IMPERVIOUS			
		P	I	P	I	P	I
WATER	EXPOSED SOIL						
TREES	AGRICULTURE						
GRAVEL	FIELD/PASTURE						
ROOFTOPS	AGRICULTURE						
ASPHALT	FIELD/PASTURE						
CONCRETE	FIELD/PASTURE						
TOTAL AREA P	16						
TOTAL AREA I	84						

		P = PERVIOUS		I = IMPERVIOUS			
		P	I	P	I	P	I
WATER	EXPOSED SOIL						
TREES	AGRICULTURE						
GRAVEL	FIELD/PASTURE						
ROOFTOPS	AGRICULTURE						
ASPHALT	FIELD/PASTURE						
CONCRETE	FIELD/PASTURE						
TOTAL AREA P	16						
TOTAL AREA I	80						

		P = PERVIOUS		I = IMPERVIOUS			
		P	I	P	I	P	I
WATER	EXPOSED SOIL						
TREES	AGRICULTURE						
GRAVEL	FIELD/PASTURE						
ROOFTOPS	AGRICULTURE						
ASPHALT	FIELD/PASTURE						
CONCRETE	FIELD/PASTURE						
TOTAL AREA P	16						
TOTAL AREA I	89						

		P = PERVIOUS		I = IMPERVIOUS			
		P	I	P	I	P	I
WATER	EXPOSED SOIL						
TREES	AGRICULTURE						
GRAVEL	FIELD/PASTURE						
ROOFTOPS	AGRICULTURE						
ASPHALT	FIELD/PASTURE						
CONCRETE	FIELD/PASTURE						
TOTAL AREA P	16						
TOTAL AREA I	85						

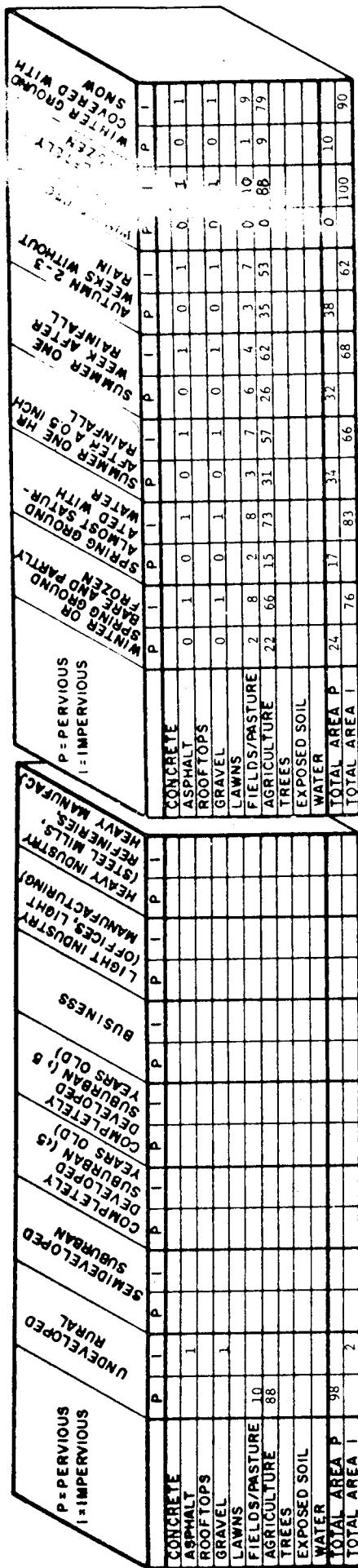
		P = PERVIOUS		I = IMPERVIOUS			
		P	I	P	I	P	I
WATER	EXPOSED SOIL						
TREES	AGRICULTURE						
GRAVEL	FIELD/PASTURE						
ROOFTOPS	AGRICULTURE						
ASPHALT	FIELD/PASTURE						
CONCRETE	FIELD/PASTURE						
TOTAL AREA P	16						
TOTAL AREA I	80						

		P = PERVIOUS		I = IMPERVIOUS			
		P	I	P	I	P	I
WATER	EXPOSED SOIL						
TREES	AGRICULTURE						
GRAVEL	FIELD/PASTURE						
ROOFTOPS	AGRICULTURE						
ASPHALT	FIELD/PASTURE						
CONCRETE	FIELD/PASTURE						
TOTAL AREA P	16						
TOTAL AREA I	75						

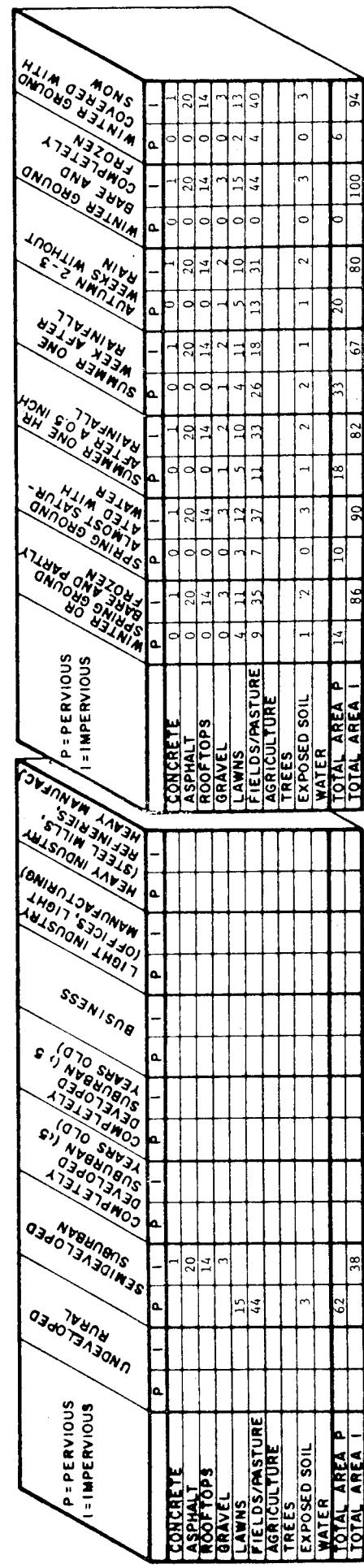
Watershed analysis data for Stapleton Airport, 1959

Watershed analysis data for Stapleton Airport, 1963

Watershed analysis data for Stapleton Airport, 1970



Watershed analysis data for Stapleton - S, 1950



Watershed analysis data for Stapleton - S, 1954

P = PERVIOUS I = IMPERVIOUS		WATERSHED ANALYSIS DATA FOR STAPLETON - S, 1963																											
UNDEVELOPED RURAL																													
SEMI-DEVELOPED SUBURBAN																													
P	I	P	I	P	I	P	I	P	I	P	I	P	I	P	I														
CONCRETE		CONCRETE		CONCRETE		CONCRETE		CONCRETE		CONCRETE		CONCRETE		CONCRETE		CONCRETE													
ASPHALT		ASPHALT		ASPHALT		ASPHALT		ASPHALT		ASPHALT		ASPHALT		ASPHALT		ASPHALT													
ROOFTOPS		ROOFTOPS		ROOFTOPS		ROOFTOPS		ROOFTOPS		ROOFTOPS		ROOFTOPS		ROOFTOPS		ROOFTOPS													
GRAVEL		GRAVEL		GRAVEL		GRAVEL		GRAVEL		GRAVEL		GRAVEL		GRAVEL		GRAVEL													
LAWNS		LAWNS		LAWNS		LAWNS		LAWNS		LAWNS		LAWNS		LAWNS		LAWNS													
FIELDS/PASTURE		FIELDS/PASTURE		FIELDS/PASTURE		FIELDS/PASTURE		FIELDS/PASTURE		FIELDS/PASTURE		FIELDS/PASTURE		FIELDS/PASTURE		FIELDS/PASTURE													
AGRICULTURE		AGRICULTURE		AGRICULTURE		AGRICULTURE		AGRICULTURE		AGRICULTURE		AGRICULTURE		AGRICULTURE		AGRICULTURE													
TREES		TREES		TREES		TREES		TREES		TREES		TREES		TREES		TREES													
EXPOSED SOIL		EXPOSED SOIL		EXPOSED SOIL		EXPOSED SOIL		EXPOSED SOIL		EXPOSED SOIL		EXPOSED SOIL		EXPOSED SOIL		EXPOSED SOIL													
WATER		WATER		WATER		WATER		WATER		WATER		WATER		WATER		WATER													
TOTAL AREA P	64	TOTAL AREA I	36	TOTAL AREA P	14	TOTAL AREA I	10	TOTAL AREA P	18	TOTAL AREA I	13	TOTAL AREA P	22	TOTAL AREA I	77	TOTAL AREA P													
TOTAL AREA I																													

Watershed analysis data for Stapleton - S, 1959

P = PERVIOUS I = IMPERVIOUS		WATERSHED ANALYSIS DATA FOR STAPLETON - S, 1963																											
UNDEVELOPED RURAL																													
SEMI-DEVELOPED SUBURBAN																													
P	I	P	I	P	I	P	I	P	I	P	I	P	I	P	I														
CONCRETE		CONCRETE		CONCRETE		CONCRETE		CONCRETE		CONCRETE		CONCRETE		CONCRETE		CONCRETE													
ASPHALT		ASPHALT		ASPHALT		ASPHALT		ASPHALT		ASPHALT		ASPHALT		ASPHALT		ASPHALT													
ROOFTOPS		ROOFTOPS		ROOFTOPS		ROOFTOPS		ROOFTOPS		ROOFTOPS		ROOFTOPS		ROOFTOPS		ROOFTOPS													
GRAVEL		GRAVEL		GRAVEL		GRAVEL		GRAVEL		GRAVEL		GRAVEL		GRAVEL		GRAVEL													
LAWNS		LAWNS		LAWNS		LAWNS		LAWNS		LAWNS		LAWNS		LAWNS		LAWNS													
FIELDS/PASTURE		FIELDS/PASTURE		FIELDS/PASTURE		FIELDS/PASTURE		FIELDS/PASTURE		FIELDS/PASTURE		FIELDS/PASTURE		FIELDS/PASTURE		FIELDS/PASTURE													
AGRICULTURE		AGRICULTURE		AGRICULTURE		AGRICULTURE		AGRICULTURE		AGRICULTURE		AGRICULTURE		AGRICULTURE		AGRICULTURE													
TREES		TREES		TREES		TREES		TREES		TREES		TREES		TREES		TREES													
EXPOSED SOIL		EXPOSED SOIL		EXPOSED SOIL		EXPOSED SOIL		EXPOSED SOIL		EXPOSED SOIL		EXPOSED SOIL		EXPOSED SOIL		EXPOSED SOIL													
WATER		WATER		WATER		WATER		WATER		WATER		WATER		WATER		WATER													
TOTAL AREA P	15	TOTAL AREA I	12	TOTAL AREA P	18	TOTAL AREA I	12	TOTAL AREA P	28	TOTAL AREA I	21	TOTAL AREA P	0	TOTAL AREA I	0	TOTAL AREA P													
TOTAL AREA I																													

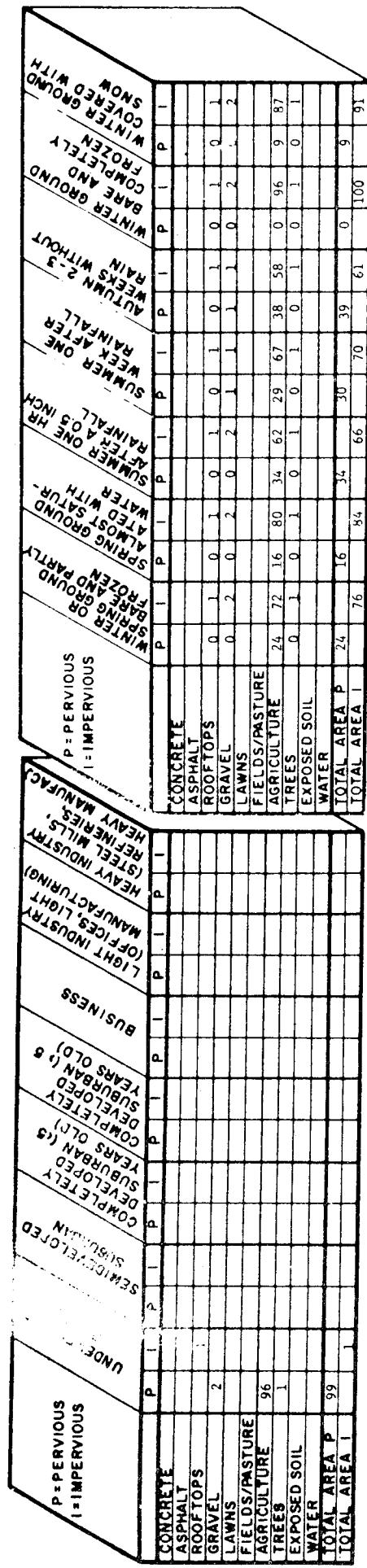
Watershed analysis data for Stapleton - S, 1963

		P: PVIOUS		I: IMPERVIOUS			
		P	I	P	I	P	I
CONCRETE	0	1	0	1	0	1	0
ASPHALT	0	22	0	22	0	22	0
ROOFTOPS	0	16	0	16	0	16	0
GRAVEL	0	0	0	0	0	0	0
LAWNS	11	35	8	38	14	32	11
FIELDS/PASTURE	2	10	2	10	3	9	7
AGRICULTURE	0	0	0	0	0	0	0
TREES	1	0	2	1	1	1	1
EXPOSED SOIL	0	1	0	1	1	1	1
WATER	0	0	0	0	1	1	0
TOTAL AREA P	14	10	18	20	22	22	6
TOTAL AREA I	86	90	82	80	78	70	64

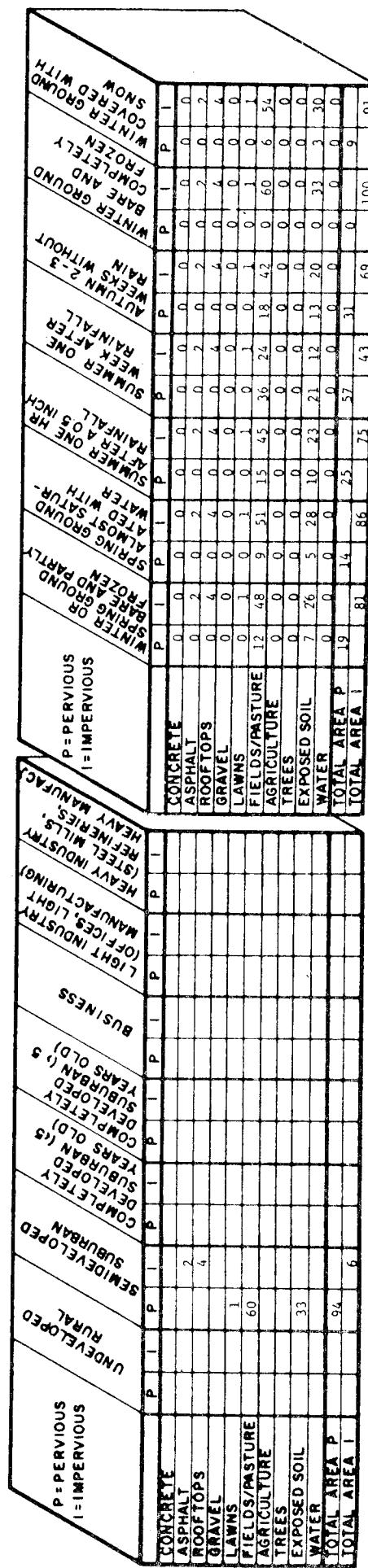
Watershed analysis data for Stapleton - S, 1970

		P: PVIOUS		I: IMPERVIOUS			
		P	I	P	I	P	I
CONCRETE	0	1	0	1	1	1	0
ASPHALT	0	22	0	22	0	22	0
ROOFTOPS	0	16	0	16	0	16	0
GRAVEL	0	0	0	0	0	0	0
LAWNS	11	35	8	38	14	32	11
FIELDS/PASTURE	2	10	2	10	3	9	7
AGRICULTURE	0	0	0	0	0	0	0
TREES	1	0	2	1	1	1	1
EXPOSED SOIL	0	1	0	1	1	1	1
WATER	0	0	0	0	1	1	0
TOTAL AREA P	14	10	18	20	22	22	6
TOTAL AREA I	86	90	82	80	78	70	64

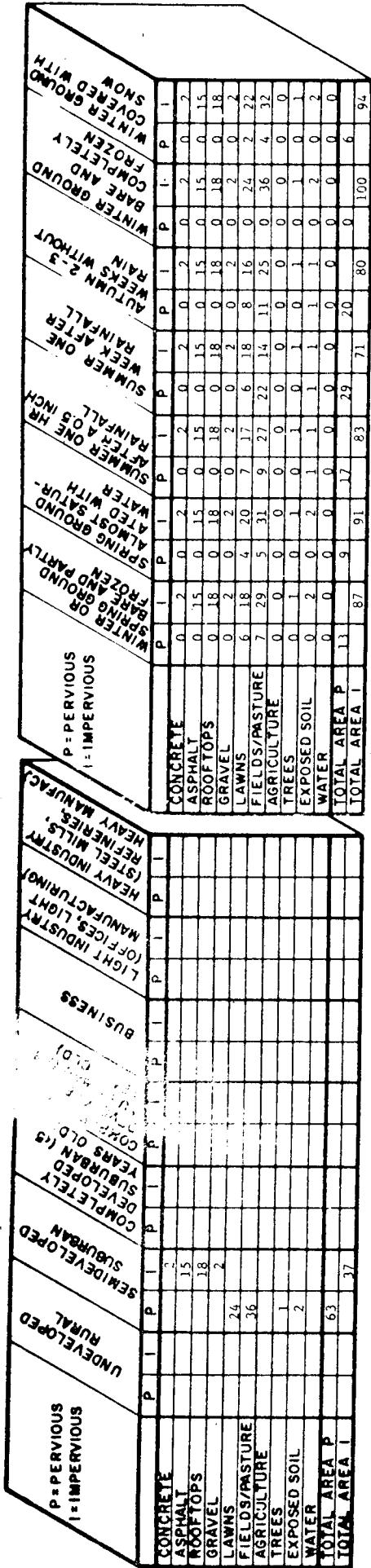
Watershed analysis data for Aurora, 1954



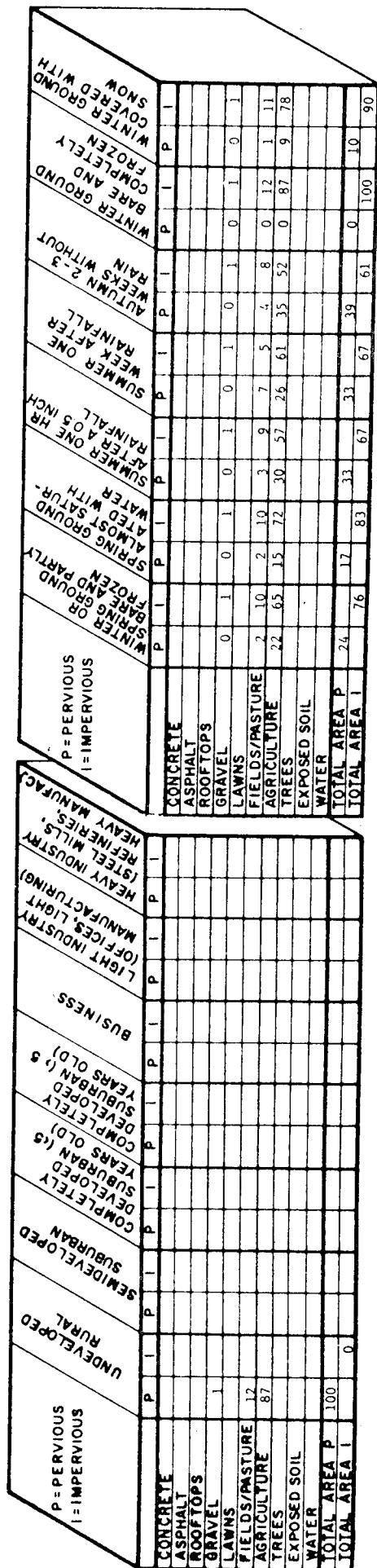
Watershed analysis data for Aurora, 1959



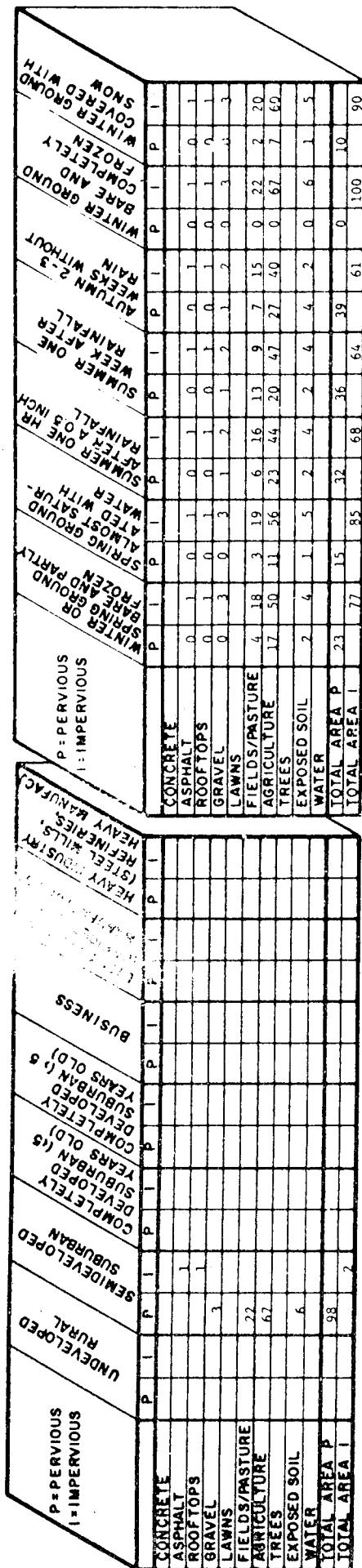
Watershed analysis data for Aurora: 1963



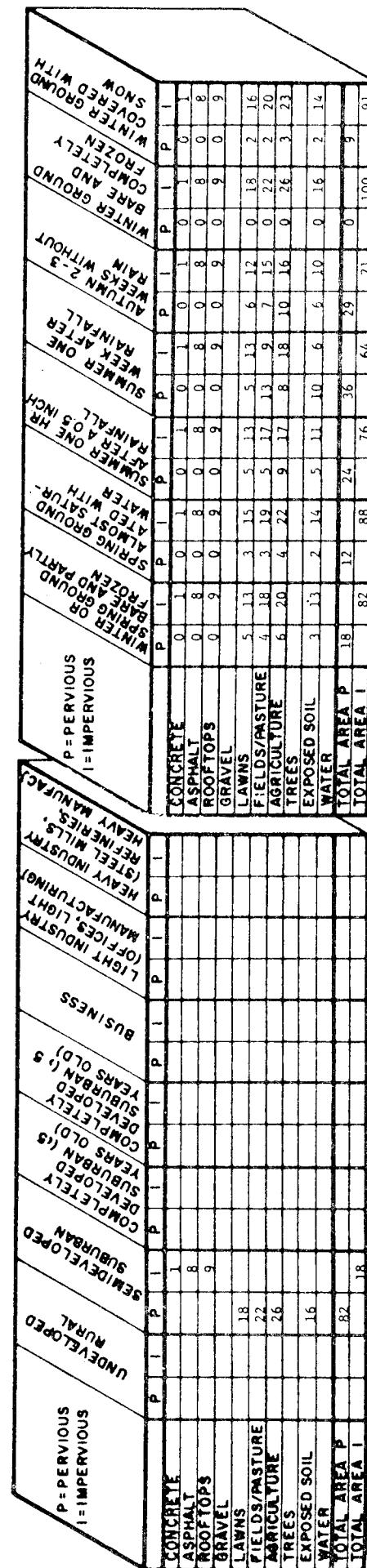
Watershed analysis data for Aurora, 1970



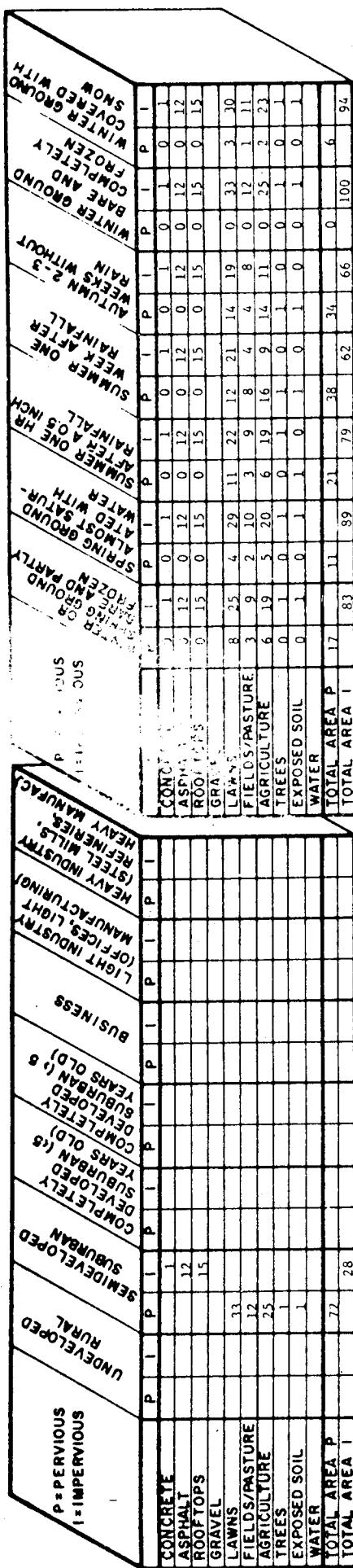
Watershed analysis data for Littleton, 1954



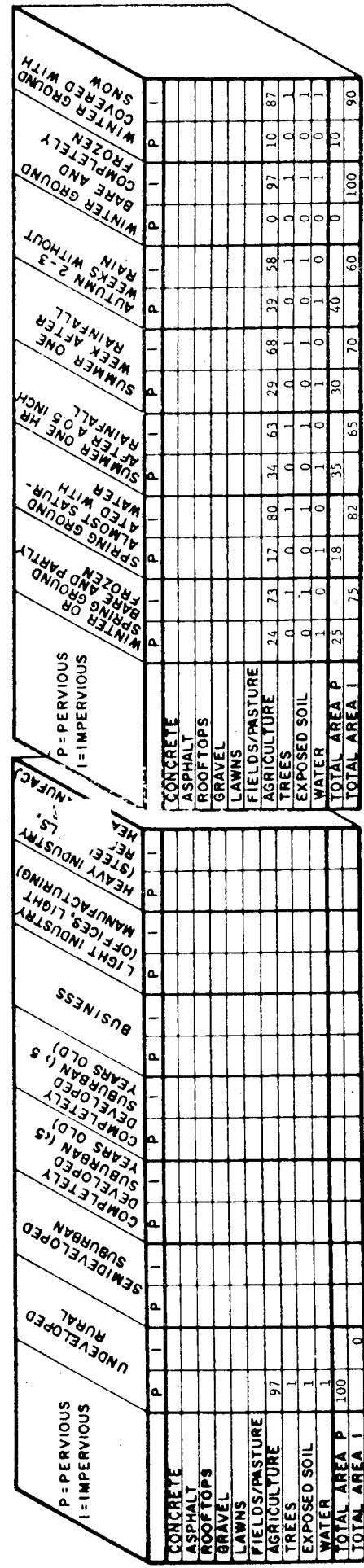
Watershed analysis data for Littleton, 1959



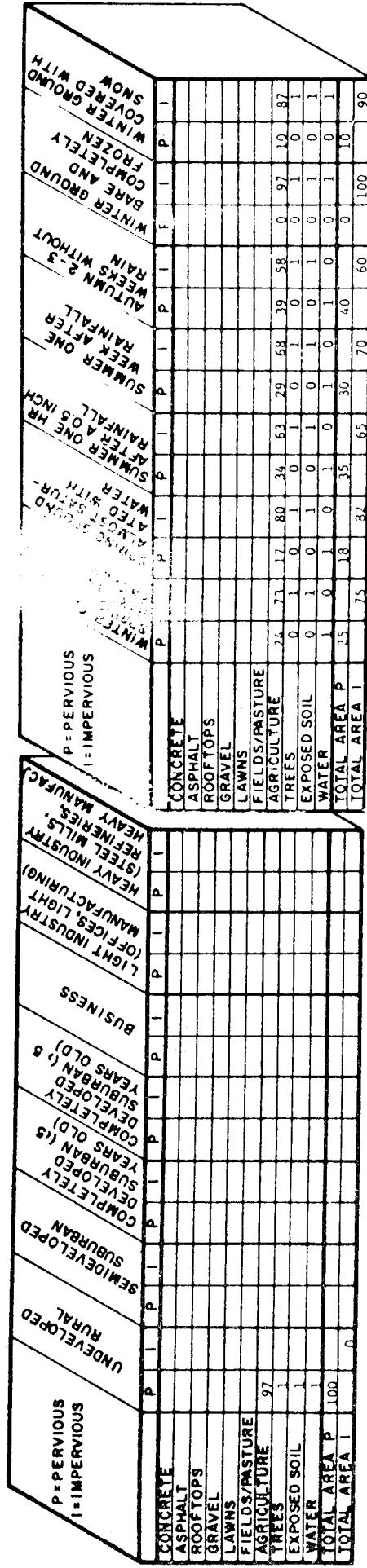
Watershed analysis data for Littleton, 1963



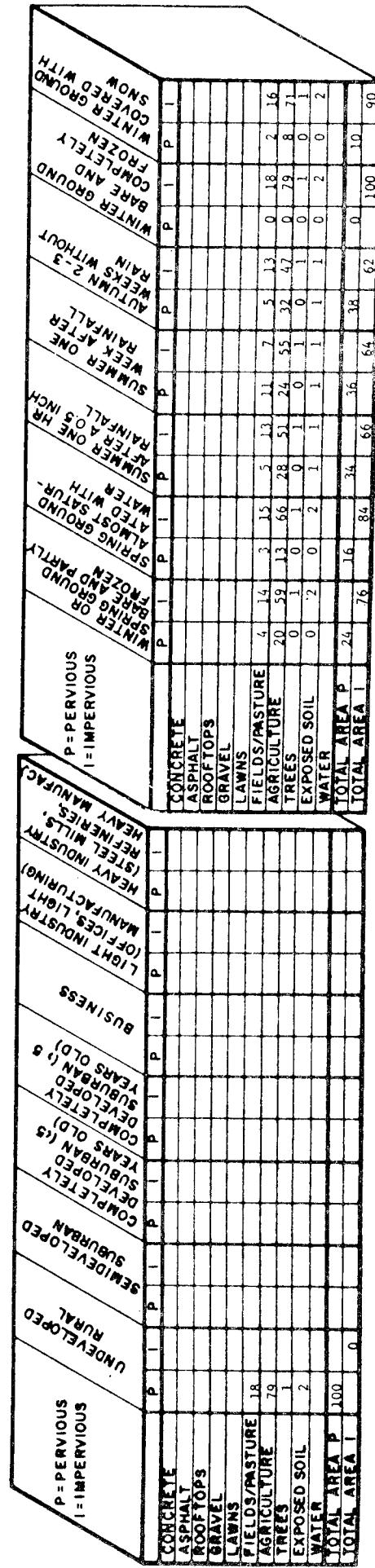
Watershed analysis data for Littleton, 1970



Watershed analysis data for Fort Logan, 1949



Watershed analysis data for Fort Logan, 1954



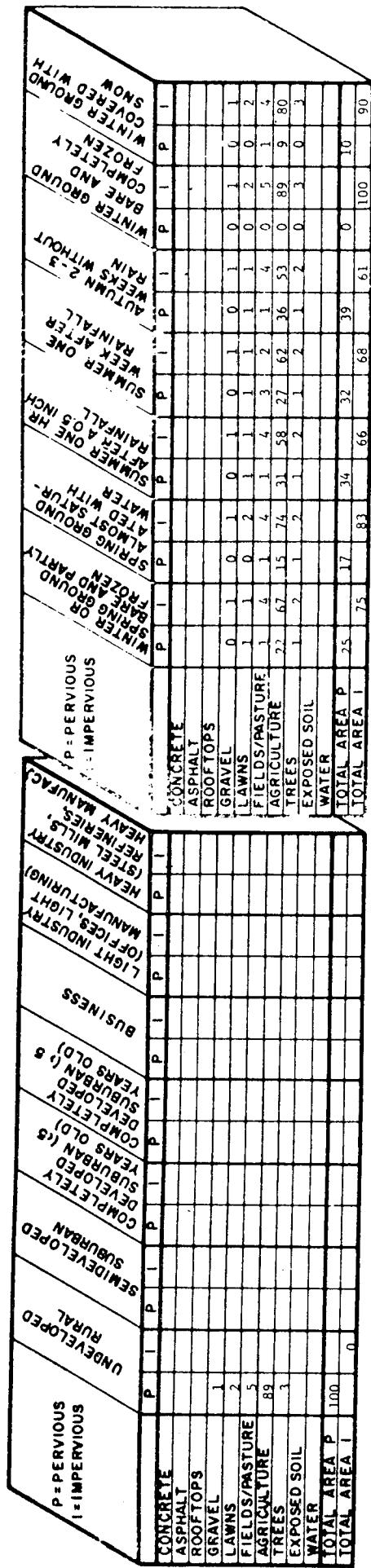
Watershed analysis data for Fort Logan, 1959

		P = PERVIOUS I = IMPERVIOUS		CONCRETE		ASPHALT		ROOFTOPS		GRAVEL		LAWNS		FIELDS/PASTURE		AGRICULTURE		TREES		EXPOSED SOIL		WATER		TOTAL AREA P		TOTAL AREA I		
				P	I	P	I	P	I	P	I	P	I	P	I	P	I	P	I	P	I	P	I	P	I	P	I	
UNDEVELOPED	RURAL			CONCRETE	6	1	0	6	0	6	0	6	0	6	0	6	0	6	0	6	0	6	0	6	0	6	0	6
SEMI-DEVELOPED	YEARLY			ASPHALT	9	0	9	0	9	0	9	0	9	0	9	0	9	0	9	0	9	0	9	0	9	0	9	0
COMPLETED (1-5)	DESUBURBAN (1-5)			ROOFTOPS	2	0	2	0	2	0	2	0	2	0	2	0	2	0	2	0	2	0	2	0	2	0	2	0
COMPLETED (6-10)	DESUBURBAN (6-10)			GRAVEL	8	0	8	0	8	0	8	0	8	0	8	0	8	0	8	0	8	0	8	0	8	0	8	0
COMPLETED (11-15)	DESUBURBAN (11-15)			LAWNS	50	1	50	1	50	1	50	1	50	1	50	1	50	1	50	1	50	1	50	1	50	1	50	1
SEMI-DEVELOPED	MANUFACTURING			FIELDS/PASTURE	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0
SEMI-DEVELOPED	OFFICES, LIGHT			AGRICULTURE	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0
SEMI-DEVELOPED	HEAVY INDUSTRY			TREES	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0
SEMI-DEVELOPED	HEAVY INDUSTRY			EXPOSED SOIL	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0
SEMI-DEVELOPED	HEAVY INDUSTRY			WATER	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0
TOTAL AREA P				TOTAL AREA P	84	1	84	1	84	1	84	1	84	1	84	1	84	1	84	1	84	1	84	1	84	1	84	1
TOTAL AREA I				TOTAL AREA I	16	1	16	1	16	1	16	1	16	1	16	1	16	1	16	1	16	1	16	1	16	1	16	1

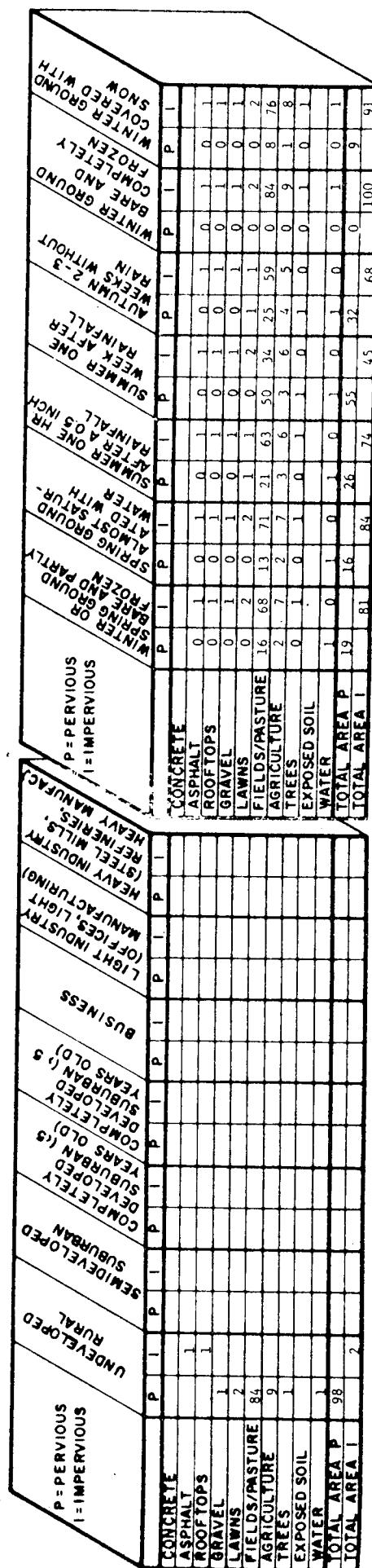
Watershed analysis data for Fort Logan, 1963

		P = PERVIOUS I = IMPERVIOUS		CONCRETE		ASPHALT		ROOFTOPS		GRAVEL		LAWNS		FIELDS/PASTURE		AGRICULTURE		TREES		EXPOSED SOIL		WATER		TOTAL AREA P		TOTAL AREA I		
				P	I	P	I	P	I	P	I	P	I	P	I	P	I	P	I	P	I	P	I	P	I	P	I	
UNDEVELOPED	RURAL			CONCRETE	2	0	2	0	2	0	2	0	2	0	2	0	2	0	2	0	2	0	2	0	2	0	2	0
SIMI-DEVELOPED	YEARLY			ASPHALT	26	0	26	0	26	0	26	0	26	0	26	0	26	0	26	0	26	0	26	0	26	0	26	0
COMPLETED (1-5)	DESUBURBAN (1-5)			ROOFTOPS	21	0	21	0	21	0	21	0	21	0	21	0	21	0	21	0	21	0	21	0	21	0	21	0
COMPLETED (6-10)	DESUBURBAN (6-10)			GRAVEL	50	1	50	1	50	1	50	1	50	1	50	1	50	1	50	1	50	1	50	1	50	1	50	1
COMPLETED (11-15)	DESUBURBAN (11-15)			LAWNS	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0
SEMI-DEVELOPED	MANUFACTURING			FIELDS/PASTURE	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0
SEMI-DEVELOPED	OFFICES, LIGHT			AGRICULTURE	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0
SEMI-DEVELOPED	HEAVY INDUSTRY			TREES	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0
SEMI-DEVELOPED	HEAVY INDUSTRY			EXPOSED SOIL	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0
SEMI-DEVELOPED	HEAVY INDUSTRY			WATER	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0	12	0
TOTAL AREA P				TOTAL AREA P	88	1	88	1	88	1	88	1	88	1	88	1	88	1	88	1	88	1	88	1	88	1	88	1
TOTAL AREA I				TOTAL AREA I	49	1	49	1	49	1	49	1	49	1	49	1	49	1	49	1	49	1	49	1	49	1	49	1

Watershed analysis data for Fort Logan. 1970



Watershed analysis data for Hyatt Lake - N, 1959



Watershed analysis data for Hyatt Lake - N. 1963

P = PERVIOUS I = IMPERVIOUS	
UNDEVELOPED RURAL	0
SEMIDEVELOPED SUBURBAN	0
COMPLETED SUBURBAN YEARS OLD (15)	0
DEVELOPED SUBURBAN YEARS OLD (5)	0
SUBURBAN YEARS OLD (8)	0
COMPLETED SUBURBAN YEARS OLD (15)	0
DEVELOPED SUBURBAN YEARS OLD (5)	0
MANUFACTURING (OFFICES, LIGHT)	0
HEAVY INDUSTRY (OFFICES, LIGHT)	0
HEAVY INDUSTRY (STEEL MILLS, REFINERIES, RECYCLING)	0
HEAVY INDUSTRY (STEEL MILLS, REFINERIES, MANUFACTURING)	0
SPRING GROUNDS ALMOST STANDING WATER	0
SPRING GROUNDS ALMOST STANDING WATER ONE INCH	0
SPRING GROUNDS ALMOST STANDING WATER 2-5 INCH	0
SPRING GROUNDS ALMOST STANDING WATER 5-10 INCH	0
SPRING GROUNDS ALMOST STANDING WATER 10-20 INCH	0
SPRING GROUNDS ALMOST STANDING WATER 20-50 INCH	0
SPRING GROUNDS ALMOST STANDING WATER 50-100 INCH	0
SPRING GROUNDS ALMOST STANDING WATER 100+ INCH	0
SPRING GROUNDS ALMOST STANDING WATER 100+ INCH SUMMER ONE INCH	0
SPRING GROUNDS ALMOST STANDING WATER 100+ INCH SUMMER 2-5 INCH	0
SPRING GROUNDS ALMOST STANDING WATER 100+ INCH SUMMER 5-10 INCH	0
SPRING GROUNDS ALMOST STANDING WATER 100+ INCH SUMMER 10-20 INCH	0
SPRING GROUNDS ALMOST STANDING WATER 100+ INCH SUMMER 20-50 INCH	0
SPRING GROUNDS ALMOST STANDING WATER 100+ INCH SUMMER 50-100 INCH	0
SPRING GROUNDS ALMOST STANDING WATER 100+ INCH SUMMER 100+ INCH	0
CONCRETE	0
ASPHALT	1
ROOFTOPS	1
GRAVEL	1
LAWNS	2
FIELDS/PASTURE	15
AGRICULTURE	15
TREES	79
EXPOSED SOIL	1
WATER	1
TOTAL AREA P	98
TOTAL AREA I	2
TOTAL AREA I	68
TOTAL AREA P	87
77	23
65	82
0	0
18	35
94	100

Watershed analysis data for Hyatt Lake - N, 1970

P = PERVIOUS I = IMPERVIOUS	
UNDEVELOPED RURAL	0
SEMIDEVELOPED SUBURBAN	0
COMPLETED SUBURBAN YEARS OLD (5)	0
DEVELOPED SUBURBAN YEARS OLD (15)	0
MANUFACTURING (OFFICES, LIGHT)	0
HEAVY INDUSTRY (OFFICES, LIGHT)	0
HEAVY INDUSTRY (STEEL MILLS, REFINERIES, MANUFACTURING)	0
SPRING GROUNDS ALMOST STANDING WATER	0
SPRING GROUNDS ALMOST STANDING WATER ONE INCH	0
SPRING GROUNDS ALMOST STANDING WATER 2-5 INCH	0
SPRING GROUNDS ALMOST STANDING WATER 5-10 INCH	0
SPRING GROUNDS ALMOST STANDING WATER 10-20 INCH	0
SPRING GROUNDS ALMOST STANDING WATER 20-50 INCH	0
SPRING GROUNDS ALMOST STANDING WATER 50-100 INCH	0
SPRING GROUNDS ALMOST STANDING WATER 100+ INCH	0
SPRING GROUNDS ALMOST STANDING WATER 100+ INCH SUMMER ONE INCH	0
SPRING GROUNDS ALMOST STANDING WATER 100+ INCH SUMMER 2-5 INCH	0
SPRING GROUNDS ALMOST STANDING WATER 100+ INCH SUMMER 5-10 INCH	0
SPRING GROUNDS ALMOST STANDING WATER 100+ INCH SUMMER 10-20 INCH	0
SPRING GROUNDS ALMOST STANDING WATER 100+ INCH SUMMER 20-50 INCH	0
SPRING GROUNDS ALMOST STANDING WATER 100+ INCH SUMMER 50-100 INCH	0
SPRING GROUNDS ALMOST STANDING WATER 100+ INCH SUMMER 100+ INCH	0
CONCRETE	0
ASPHALT	0
ROOFTOPS	0
GRAVEL	1
LAWNS	2
FIELDS/PASTURE	63
AGRICULTURE	4
TREES	11
EXPOSED SOIL	3
WATER	1
TOTAL AREA P	98
TOTAL AREA I	2
TOTAL AREA I	79
16	84
26	74
53	47
0	68
10	100
90	100

Watershed analysis data for Hyatt Lake - S, 1959

Watershed analysis data for Hyatt Lake - S, 1963

Watershed analysis data for Hyatt Lake - S, 1970

APPENDIX E: LISTINGS OF FORTRAN PROGRAMS
USED IN SPECTRAL BAND OPTIMIZATION

Three computer programs, all written in FORTRAN, were used in this study as a means for handling the data as it comes from the computer-controlled field spectrometer, for averaging data curves together, and for performing the Euclidean distance calculations for the spectral band optimization process. This appendix contains the listings for these programs, JOIN, AVER, OPTIM, and Appendix F contains their detailed flow diagrams. Several additional programs following OPTIM in this sequence are in the process of being perfected and will occur in a supplemental report.

JOIN This program reads the spectroreflectance paper tapes output from the field spectrometer and joins all segments (ultraviolet, visible, and infrared) into one continuous curve, joining the segments together at operator specified wavelengths. The program plots out the joined curve on an on-line, x-y plotter as an operator option and punches an output tape of the continuous curve for input into AVER.

AVER This program reads up to six joined curves output by JOIN and calculates the average spectroreflectance and variance curves. The resulting average curve can be plotted on the x-y plotter as an operator option along with \pm one standard deviation, also optional. This averaged spectroreflectance curve is punched as an output paper tape with the wavelength, mean, and variance values at each sample point for input into OPTIM.

OPTIM This program reads up to 10 statistical spectroreflectance curves output from AVER and accepts up to 12 spectral bands of any spectral bandwidth and location within the range of $.3\mu\text{m}$ to $1.3\mu\text{m}$. It calls for a number representing the optimum subset of the total number of bands entered and calculates the minimum, maximum, and average Euclidean distances for each band combination equal to the number of bands specified as the optimum subset. OPTIM follows the procedure given in the text for producing the Euclidean distances from which the best bands are chosen by human inspection. OPTIM prints out the reflectance averages over each of the total number of bands specified, and likewise the variance averages in the form of two matrices, and prints out a third matrix of squared reflectivity differences which result from an interim step in the Euclidean distance calculations. As final output each band combination is listed, followed by the minimum, maximum, and average Euclidean distances, as calculated for each respective combination. Following the program listing of OPTIM is a sample output list containing the three matrices as described above for 10 materials with 12 total bands and the beginning of a long list of four-band combinations out of 12 bands (495 in all) followed by the Euclidean distance calculations. OPTIM is being modified to punch out these data for entry into two additional programs which will assist the user in selecting the one best optimal spectral band combination. These modifications and new programs will be documented in a subsequent report.

```

PROGRAM JOIN
COMMON NAME(34), IWAVE(750), RI(750), L(6)
      5 WRITE(6,500)
      500 FORMAT('CURVE NAME')
         READ(1,501) NAME
      501 FORMAT(34A2)
         WRITE(6,502)
      502 FORMAT('NUMBER OF CURVE SECTIONS')
         READ(1,*), NSEC
      503 WRITE(6,503)
      503 FORMAT('BEGINNING AND ENDING WAVELENGTHS FOR EACH SEGMENT')
         DO 10 I=1,NSEC
      10 READ(1,*), L(I), H(I)
      504 WRITE(6,504)
      504 FORMAT("LOAD CURVES, TURN ON PUNCH, --- PRESS RUN")
         PAUSE
      505 WRITE(4,505) NAME
      505 FORMAT(1H',34A2,2H ",1")
         NP=0
         DO 50 J=1,NSEC
            WRITE(4,506) L(J)
      506 FORMAT(15)
         NJ=J+1
         READ(5,*), NCUR
         WRITE(4,506) NCUR
         READ(5,512) ID, TH, IM
      512 FORMAT(1,I2,I2,I2,I2,I2)
         WRITE(4,507) ID, TH, IM
      507 FORMAT(1I3,"I2","I2")
         READ(5,506) LIM
         DO 50 K=1,LIM
            READ(5,*), IW,DIM1,DIM2,R
            IF(ISSW(5))11,12
      11   WRITE(6,600) IW,R,LIM
      600  FORMAT(5X,I5,5X,F6.4,5X,I3)
      12   IF(IW-L(J))50,16,15
      15   IF(IW-L(NJ))20,20,40
      16   IF((J-1)50,20,50
      20   NP=NP+1
            IWAVE(NP)=IW
            REF(NP)=R
      40   IF(K-LIM)50,60
      60   IF((J-NSEC)70,50
      70   IK=J-1
            WRITE(6,510) IK
      510  FORMAT("LOAD CURVE SEGMENT",I2)
            PAUSE
      50  CONTINUE
            WRITE(4,508) NP
      508 FORMAT(I3)
            DO 100 I=1,NP
      100  WRITE(4,509) IWAVE(I),REF(I)
      509 FORMAT(15,"F6.4)
            WRITE(6,511)
      511 FORMAT("FOR PLOT TURN ON SW 1 -- SET UP PLOTTER")
            PAUSE
            IF(ISSW(1))80,90
      80  DO 200 I=1,NP
               WAVE=IWAVE(I)
               WMAX=16000
               WMIN=1800
               WPLT=RMAX*(WAVE-WMIN)/(RMAX-WMIN)
               RMAX=1.
            CALL PLOT(WPLT,WMAX,REF(I),RMAX)
      200 CONTINUE
            WRITE(6,511)
      513 FORMAT("FOR ADDITIONAL PLOT, SET UP PLOTTER, SW 10 ON")
            PAUSE
            IF(ISSW(10))80,90
      90  PAUSE
            GO TO 5
         END
        END$
```

PROGRAM AVER

```

PROGRAM AVER
COMMON REF(4,300),NAME(20)
WRITE(6,701)
701 FORMAT("SW 1 ON FOR MEAN PLOT; SW 2 ON FOR STD DEV PLOT")
WRITE(6,500)
500 FORMAT("TOTAL NUMBER OF MATERIALS")
READ(1,*),IC
WRITE(6,501)
501 FORMAT("NUMBER OF CURVES PER MATERIAL")
READ(1,*),N
WRITE(6,510)
510 FORMAT("NUMBER OF RAW CURVE SEGMENTS")
READ(1,*),NSEG
WRITE(6,502)
502 FORMAT("BEGINNING AND ENDING WAVELENGTHS; SAMPLE INTERVAL,
1---","---ALL IN ANGSTROMS")
READ(1,*),MINW,MAXW,INT
INAX=1+(MAXW-MINW)/INT
CN=N
N=N-1
CN=M
DO 90 I=1,IC
WRITE(6,800)II
800 FORMAT("NAME OF MATERIAL",I3)
READ(1,801)NAME
801 FORMAT("20A2")
DO 100 I=1,N
L=0
WRITE(1,503)I,NAME
503 FORMAT(IX,"LOAD TAPE FOR CURVE",I2," OF ", "20A2",
1"--TURN ON PUNCH--PRESS RUN")
PAUSE
C---READ HEADER INFORMATION-----
Read(5,*),NO
DO 700 JJ=1, NSEG
READ(5,*),N1
READ(5,*),N2
700 READ(5,*),N3,N4,N5
READ(5,*),N6
C---READ TAPE UP TO MIN WAVELENGTH WANTED-----
10 READ(5,*),IW,R
IF((IW-MINW)>10,15
15 IW=1K
GO TO 25
20 READ(5,*),W,R
25 W=W/100000.
R=R*.100.
AVE=0.
VAR=0.
IF((SSW(5))>50,60
50 WRITE(6,600)W,R
600 FORMAT(5X,"W=",F6.4,"R=",F6.2)
60 L=L+1
IF((L-N)>30,40,30
30 REF(I,L)=R

```

PROGRAM OPTIM

E-4

```

PROGRAM OPTIM
DIMENSION AV(10,12),AVAR(10,12),G(12,2),K(10)
COMMON U(45,12)
WRITE (6,900)
900 FORMAT("NUMBER OF DATA CURVES")
READ (1,*), IC
WRITE (6,901)
901 FORMAT("TOTAL NUMBER OF WAVELENGTH BANDS")
READ (1,*), IB
WRITE (6,902)
902 FORMAT("WAVELENGTH SAMPLING INTERVAL (MICRONS)")
READ (1,*), SINT
WRITE (6,903)
903 FORMAT("NUMBER OF OPTIMUM SAMPLING BANDS DESIRED")
READ (1,*), IOPT
WRITE (1,904)
904 FORMAT("MIN AND MAX WAVELENGTH IN EACH BAND")
DO 150 I=1,IB
150 READ (1,*), (G(I,J),J=1,2)
      WRITE (1,701) ((G(I,J),J=1,2),I=1,IB)
701 FORMAT(2F6.4)
DO 10 IX=1,IC
WRITE (1,899) IX
899 FORMAT("INSERT DATA CURVE "I2" IN PHOTOREADER, PRESS RUN")
PAUSE
READ (5,*), NNDUM
DO 10 IY=1,IB
T=0.
VT=0.
S=0.
20 READ (5,*), W,R,VAR
IF (ISSW(1)) 5,6
5  WRITE (1,702) W,R,VAR
702 FORMAT("W="F8.3,6X,"R="F8.3,5X,"V="F8.3)
6  IF (W- (G(IY,1)-SINT/2.)) 20,20,25
   6  IF (W- (G(IY,2)-SINT/2.)) 27,27,30
27 T=T+R
VT=VT+VAR
S=S+1.
IF (ISSW(1)) 7,8
7  WRITE (1,703) T,S
703 FORMAT("T="F8.3,5X,"S="F8.3)
8  GO TO 20
30 AV (IX,IY)=T/S
AVAR (IX,IY)=VT/S
IF (ISSW(2)) 31,10
31 WRITE (1,704) IX,IY,G(IY,1),G(IY,2)
704 FORMAT("IX="I2,"IY="I2,5X,F8.3,F8.3)
10 CONTINUE
WRITE (6,905)
905 FORMAT("BAND AVERAGES----ROWS=SAMPLE CURVES, COLUMNS=BANDS")
DO 251 I=1,IC
251 WRITE (6,906) (AV(I,J),J=1,IB)
906 FORMAT(I2(F5.2,IX))
WRITE (6,915)

```

PROGRAM OPTIM

```

55 IQ=Q1
56 IF (IQ-TQ2)57,57,520
57 IF (IQ-IT)500,500,58
58 K(2)=IQ
      IF (IOPT-7)60,60,62
60 IR1=-8
     IR2=-8
62 DO 500 IR=IR1,IR2
     IF (IR-IQ)500,500,64
64 K(3)=IR
     IF (IS-IR)66,66,68
66 IS1=-7
     IS2=-7
68 DO 500 IS=IS1,IS2
     IF (IS-IR)500,500,70
70 K(4)=IS
     IF (IOPT-5)72,72,74
72 IT1=-6
     IT2=-6
74 DO 500 IT=IT1,IT2
     IF (IT-IS)500,500,76
76 K(5)=IT
     IF (IOPT-4)78,78,80
78 IU1=-5
     IU2=-5
80 DO 500 IU=IU1,IU2
     IF (IU-IT)500,500,82
82 K(6)=IU
     IF (IOPT-3)84,84,86
84 IV1=-4
     IV2=-4
86 DO 500 IV=IV1,IV2
     IF (IV-IU)500,500,88
88 K(7)=IV
     IF (IOPT-2)90,90,92
90 IW1=-3
     IW2=-3
92 DO 500 IW=IW1,IW2
     IF (IW-IV)500,500,94
94 K(8)=IW
     IF (IOPT-1)96,96,98
96 IX1=-2
     IX2=-2
98 DO 500 IX=IX1,IX2
     IF (IX-IW)500,500,100
100 K(9)=IX
     DO 500 IY=IY1,IY2
     IF (IY-IX)500,500,108
108 K(10)=IY

      WRITE (6,908)
908 FORMAT ("BANDS====")
      II=II-IOPT
      DO 200 IH=II,10
382 WRITE (4,385) K(IH)
385 FORMAT(12)
200 CONTINUE
      DO 400 IZ=1,IE
F1=0.
      DO 300 M=II,10
IJK(M)
      F1=F1+J(IZ,M)
300 CONTINUE
      F=SQRT (F1)
      IF (F-B)112,112,110
110 B=F
      112 IF (F-SM)114,116,116
114 SM=F
      116 T=T+F
400 CONTINUE
      E=IE
      A=T/E
      WRITE (6,910) B,SM,A
910 FORMAT ('MAX='F6.3'---MIN='F6.3'---AVE='F6.3//')
      500 CONTINUE
510 IQ=IQ+1
      GO TO 56
520 CONTINUE
530 IP=IP+1
      GO TO 52
540 CONTINUE
      STOP
      END
END$


      BEGIN MIN-MAX SORTING ROUTINE
      SM=1000.
      B=0.
      T=0.

```

OUTPUT FROM PROGRAM OPTIM

F-6

NUMBER OF DATA CURVES

	BAND AVERAGES---ROWS=SAMPLE CURVES, COLUMNS=BANDS
1.0	4.63 6.02 6.26 7.62 11.54 14.96 13.35 10.87 7.87 10.26 41.66 40.71
TOTAL NUMBER OF WAVELENGTH BANDS	4.42 5.77 6.89 8.07 8.91 10.57 12.58 14.74 13.92 13.81 19.26 21.39
1.2	8.05 8.84 9.73 9.63 10.57 11.56 12.91 13.79 14.59 16.23 19.84 20.28
WAVELENGTH SAMPLING INTERVAL (MICRONS)	2.18 2.95 2.93 3.34 5.17 7.57 6.51 5.87 4.56 7.18 29.31 30.08
.005	18.65 22.17 21.65 21.15 21.08 21.38 21.30 21.03 22.43 23.75 26.70 24.03
NUMBER OF OPTIMUM SAMPLING BANDS DESIRED	6.98 8.75 9.66 10.57 11.54 12.97 14.42 15.44 15.35 19.75 22.19 23.66
4	10.70 12.80 13.04 13.78 15.00 16.91 19.13 21.00 19.90 21.33 32.26 31.73
MIN AND MAX WAVELENGTH IN EACH BAND	2.88 3.37 3.90 4.61 5.94 7.31 7.80 8.08 7.95 8.36 23.14 26.71
.40,.44	19.24 21.54 23.86 24.46 27.12 29.55 32.78 34.94 36.90 38.08 42.33 40.33
.44,.46	8.87 10.66 11.33 12.17 12.84 15.02 16.52 18.29 19.45 20.39 34.79 34.57
.46,.48	
.48,.50	
.50,.52	
.52,.55	
.55,.58	
.58,.62	
.62,.66	
.66,.72	
.72,.80	
.80,1.00	
4000 .4400	
.4400 .4600	
.4600 .4800	
.4800 .5000	
.5000 .5200	
.5200 .5500	
.5500 .5800	
.5800 .6200	
.6200 .6600	
.6600 .7200	
.7200 .8000	
.80001.0000	

VAR AVE

.57	.52	.83	1.36	3.10	3.38	3.93	3.35	2.76	.79	50.67	79.49
.04	.04	.04	.06	.25	.57	.36	1.83	1.15	.45	.42	1.98
8.88	11.62	9.99	15.64	19.11	24.82	33.43	37.88	43.53	46.24	54.80	59.97
.11	.23	.28	.43	.71	.96	1.39	1.17	.67	3.23	16.92	28.38
249.2	370.4	361.3	343.4	329.6	326.2	318.5	317.8	375.6	325.7	325.1	262.1
.17	.08	.16	.19	.19	.28	.41	.50	.51	.46	1.29	1.60
6.78	5.41	6.45	5.17	5.10	8.51	11.21	14.93	19.31	11.11	25.32	12.35
.47	.68	1.23	1.56	1.12	1.30	3.14	6.00	8.28	5.68	18.36	20.12
9.05	10.09	24.39	21.67	24.48	30.55	27.94	37.33	47.61	33.30	27.64	29.16
9.57	12.96	15.56	15.70	19.01	26.66	42.63	72.18	61.40	105.3	159.4	130.8

PAUSE
INSERT DATA CURVE 1 IN PHOTOREADER, PRESS RUN sugar beetsPAUSE
INSERT DATA CURVE 2 IN PHOTOREADER, PRESS RUN wheatPAUSE
INSERT DATA CURVE 3 IN PHOTOREADER, PRESS RUN asphaltPAUSE
INSERT DATA CURVE 4 IN PHOTOREADER, PRESS RUN forestPAUSE
INSERT DATA CURVE 5 IN PHOTOREADER, PRESS RUN shinglesPAUSE
INSERT DATA CURVE 6 IN PHOTOREADER, PRESS RUN fallow fieldsPAUSE
INSERT DATA CURVE 7 IN PHOTOREADER, PRESS RUN gravelPAUSE
INSERT DATA CURVE 8 IN PHOTOREADER, PRESS RUN grassPAUSE
INSERT DATA CURVE 9 IN PHOTOREADER, PRESS RUN concretePAUSE
INSERT DATA CURVE 10 IN PHOTOREADER, PRESS RUN bare soils

(Items in script for information only - not part of I/O)

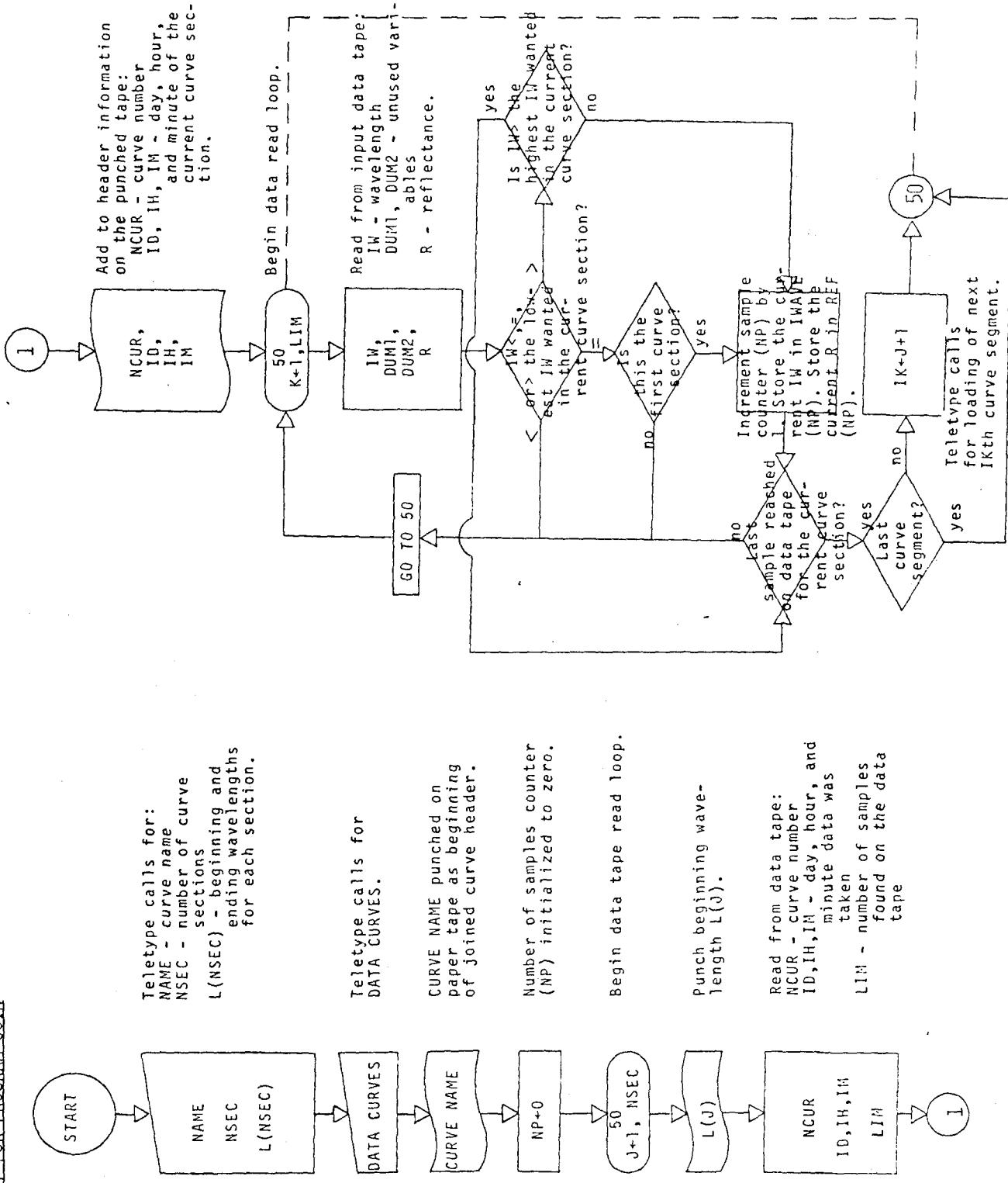
MATRIX OF SQUARED CURVE COMBINATIONS COLUMNS=BANDS,
ROWS=SAMPLE CURVE COMBINATIONS

BANDS=====											
.14	.21	.92	.29	4.15	9.77	.28	5.78	18.72	20.27	19.65	9.17
2.48	1.31	2.23	.47	.09	.82	.01	.41	1.95	1.51	.9.03	5.98
17.68	25.22	19.98	20.46	21.38	25.19	17.64	11.07	6.37	4.74	4.51	2.09
1.57	1.41	1.31	1.06	.55	1.25	.39	.64	1.12	1.11	1.19	1.63
15.02	24.74	23.28	11.30	.00	2.15	.52	10.84	34.33	32.18	14.59	7.17
10.05	15.47	12.65	11.62	2.92	.64	4.41	11.23	13.11	20.58	2.33	1.75
5.84	11.67	5.37	6.19	14.91	25.03	8.72	1.66	.00	1.12	9.94	3.93
44.36	45.40	24.56	24.62	17.60	12.54	23.67	28.47	33.48	45.40	.01	.00
3.55	3.19	3.14	2.42	.15	.00	.43	1.46	4.18	1.93	.45	.36
2.95	1.61	1.61	.31	.28	.08	.01	.05	.02	.25	.01	.04
68.05	59.78	97.73	90.86	29.31	11.82	42.02	52.48	95.96	23.90	11.66	4.98
1.62	1.45	1.21	1.00	.90	.72	.48	.25	.38	.61	.34	.05
63.23	146.5	73.87	51.13	31.45	13.69	8.80	.42	2.50	1.96	10.05	2.88
11.57	18.08	11.67	12.46	13.89	8.88	7.43	4.68	3.50	9.79	13.14	14.71
9.27	15.99	13.99	14.75	12.93	11.42	13.01	11.33	7.55	9.67	1.61	2.57
48.27	49.08	23.56	24.71	26.82	23.15	28.83	20.83	21.68	34.92	37.94	22.83
4.11	3.67	2.53	2.13	1.60	1.46	.73	.34	.98	.82	3.02	2.62
7.67	5.86	9.02	4.92	2.95	1.24	2.36	3.21	4.55	3.31	2.50	2.18
.87	.93	.76	.74	.63	.55	.40	.30	.29	.30	.25	.09
.25	.00	.00	.11	.10	.16	.13	.14	.03	.09	.20	.37
.90	1.84	1.34	1.66	1.62	1.72	1.73	1.97	.90	.91	3.85	3.61
5.71	4.87	6.06	2.92	2.12	1.39	1.43	1.48	1.70	2.39	.30	1.03
13.96	14.86	11.61	11.79	12.57	11.68	12.86	11.89	10.93	12.00	12.27	8.99
.07	.27	.20	.41	.27	.27	.74	.37	.32	.32	2.16	.47
2.18	1.39	1.94	1.84	1.53	1.17	1.37	1.44	.45	.23	2.09	2.14
166.8	219.4	205.2	168.5	89.81	47.28	69.64	109.7	197.1	31.09	5.57	.25
21.11	34.39	30.44	38.80	33.32	18.46	25.32	28.46	23.53	27.94	.41	.13
1.71	.39	1.26	1.62	.65	.06	.74	1.37	2.57	.32	2.16	.47
63.53	67.02	35.52	40.34	38.27	30.67	47.06	43.88	43.33	52.29	7.60	3.63
9.25	9.02	8.92	9.65	5.97	4.02	4.56	4.21	7.14	3.22	.34	.25
1.09	.97	.79	.65	.55	.43	.30	.20	.17	.50	.12	.00
.49	.47	.40	.31	.22	.12	.03	.00	.03	.03	.18	.43
1.99	1.91	1.74	1.58	1.39	1.21	1.13	1.04	1.09	1.43	.07	.05
.00	.00	.03	.06	.21	.37	.76	1.09	.99	1.14	1.39	1.82
.74	.69	.56	.45	.39	.23	.13	.04	.04	.05	.27	.57
3.99	5.97	3.45	3.84	4.55	3.53	3.83	4.02	2.08	7.48	7.62	9.20
52.50	75.79	47.53	40.57	47.68	40.76	24.68	16.64	12.47	13.29	.09	.86
32.58	32.19	16.41	17.64	19.69	17.82	23.77	20.11	19.30	32.23	28.03	17.90
.73	.56	.35	.32	.18	.31	.21	.22	.54	.60	1.98	1.80
16.87	29.16	21.76	24.95	26.43	18.83	17.90	15.96	10.34	20.03	3.81	1.54
9.20	9.87	7.58	8.49	9.93	8.17	9.51	7.43	8.64	12.63	3.83	3.52
.41	.50	.27	.25	.39	.20	.25	.17	.01	.02	.07	.11
56.16	61.31	31.08	33.89	35.06	31.06	40.13	33.28	30.00	45.31	16.00	7.48
7.14	7.80	6.57	6.61	4.74	4.26	3.32	2.67	3.79	2.61	1.53	.82
11.54	10.27	7.85	8.09	9.38	7.38	7.49	5.06	5.59	4.52	.61	.41

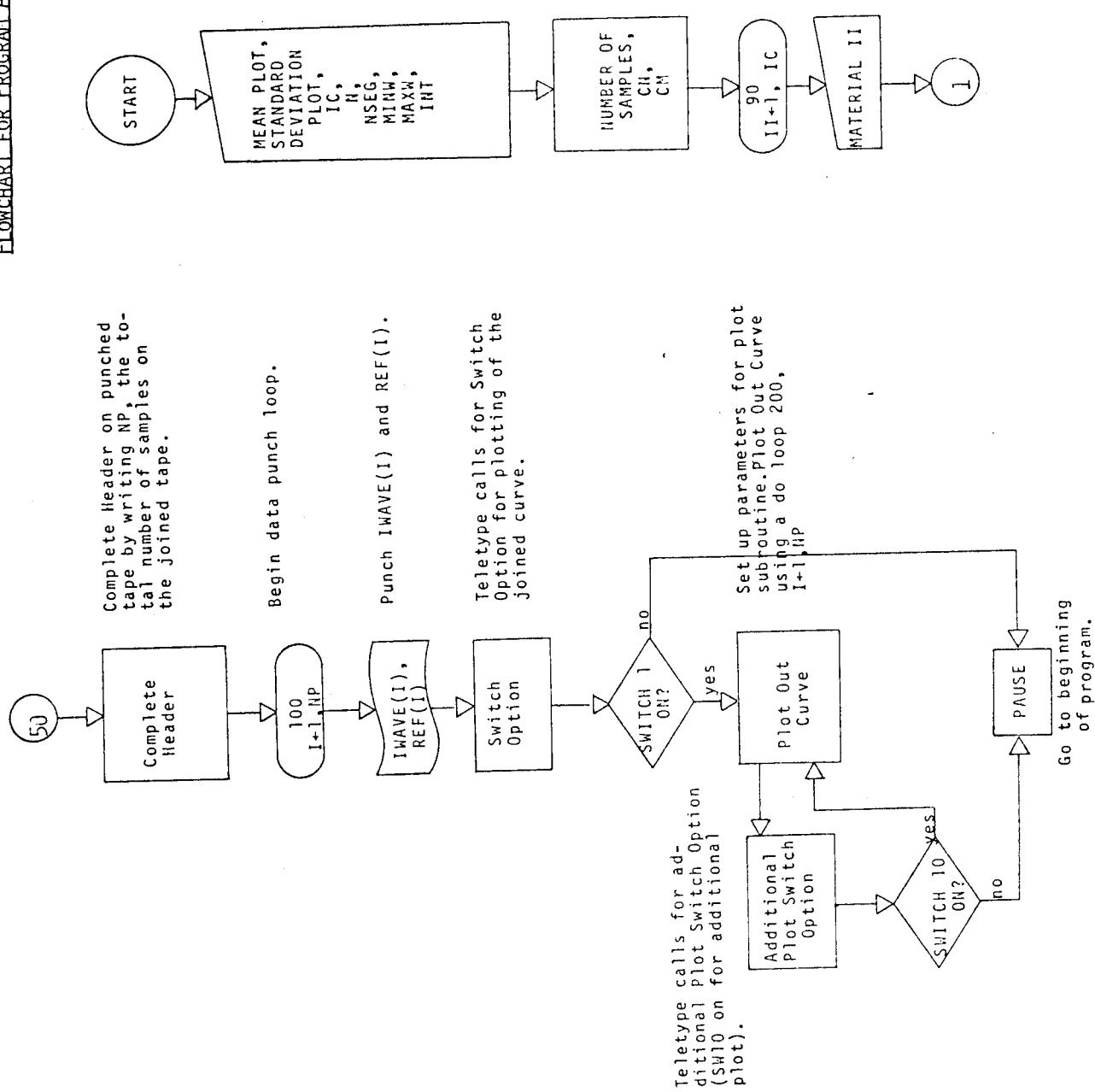
OUTPUT FROM PROGRAM OPTIM

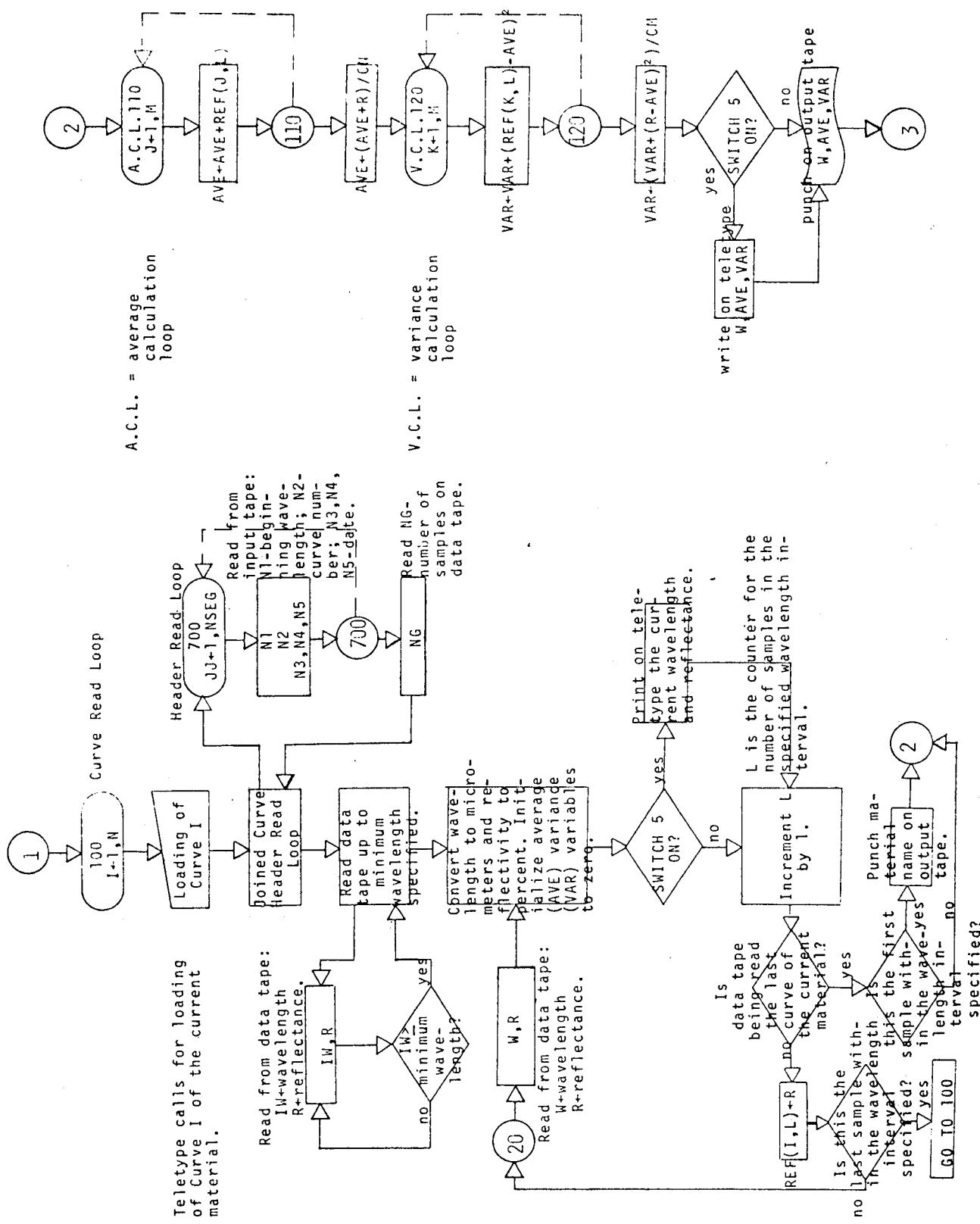
APPENDIX F: FORTRAN PROGRAM FLOW DIAGRAMS

FLOWCHART FOR PROGRAM JOLI



FLOWCHART FOR PROGRAM AVER





MANUFACTURE OF OPTICAL GLASS

